

Gravitational Astronomy

ISGWA-University of Delhi, December 2010

B.S. Sathyaprakash
Cardiff University



Resources for the Lecture

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- S1, S2, S3, ... stand for the first, second, third, ..., science runs of the LSC and Virgo

Standard Signs

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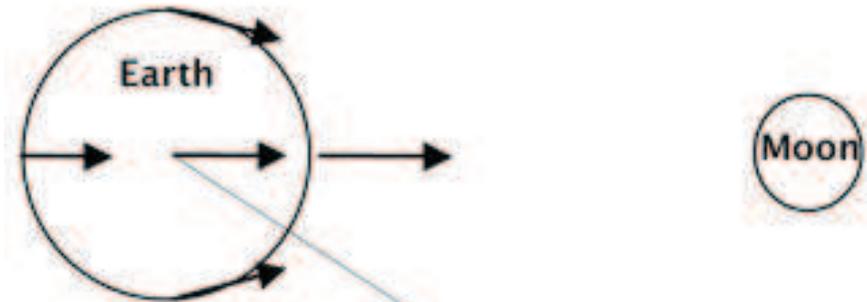
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- Here $\bar{h}_{\alpha\beta} = h_{\alpha\beta} - \frac{1}{2}\eta_{\alpha\beta}\eta^{\mu\nu}h_{\mu\nu}$ is the trace-reverse tensor.

Tidal Gravitational Forces of GW

Acceleration of the Moon's gravity on Earth.
Length of arrow indicates size of acceleration.



The acceleration at the **center** is the mean acceleration with which the solid Earth will fall. The acceleration of gravity due to the Moon is larger near the Moon and smaller further away.

Residual acceleration of the Moon's gravity,
after subtracting the mean acceleration of the Earth.

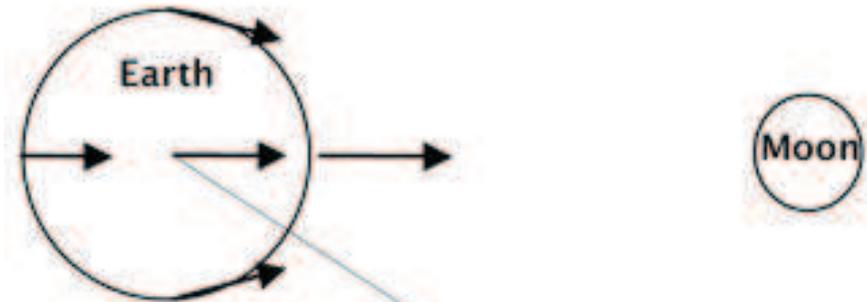


Arrows represent the tidal forces on the Earth.

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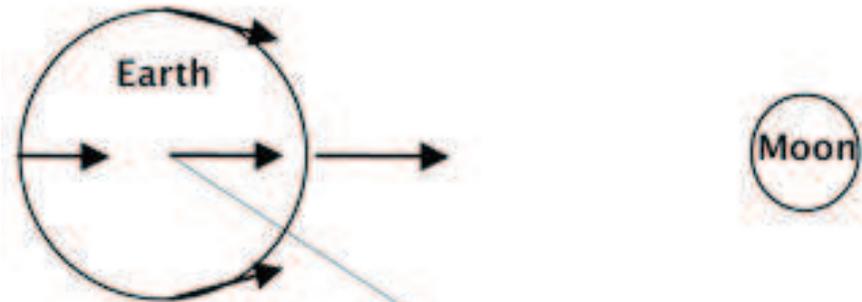


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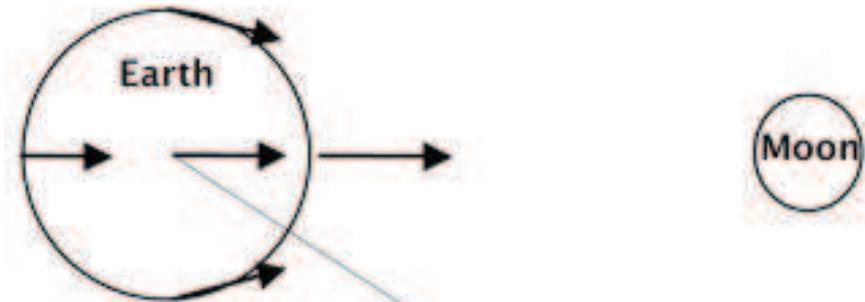


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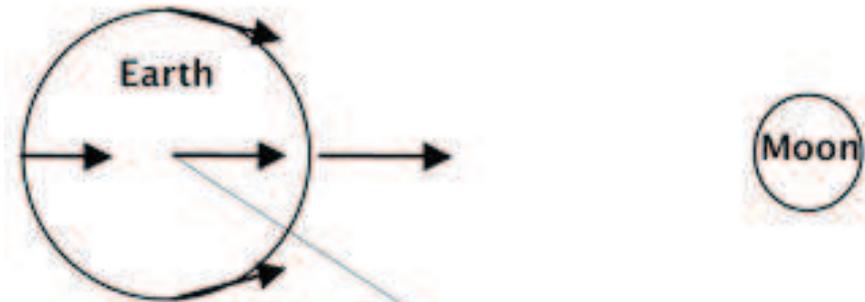


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Tidal Gravitational Forces of GW

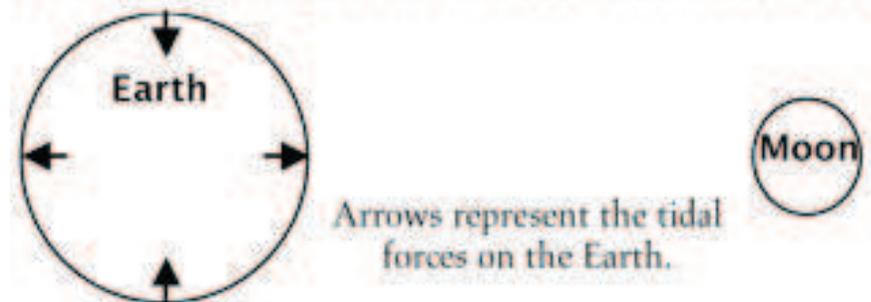
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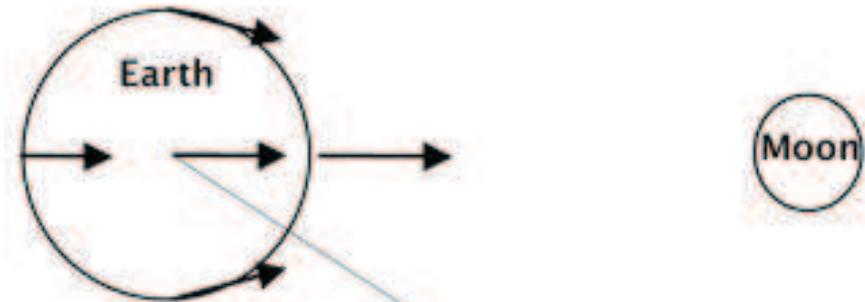


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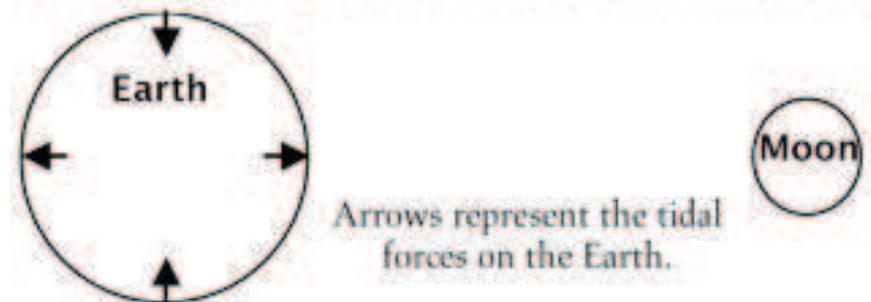
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- Gravitational waves also cause a tidal effect the only difference is that the effect falls off as $1/r$

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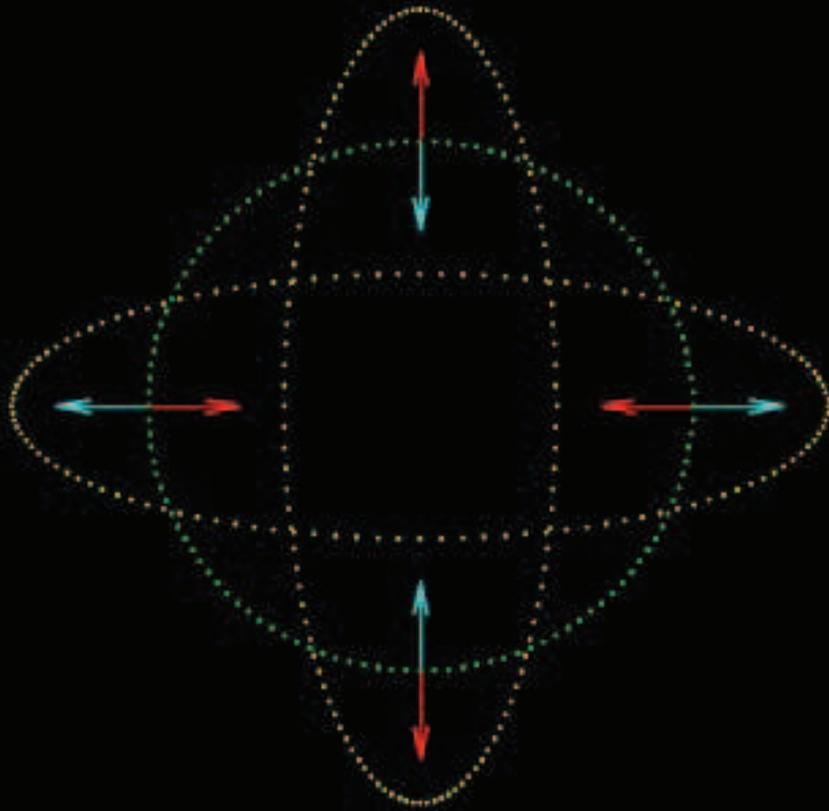
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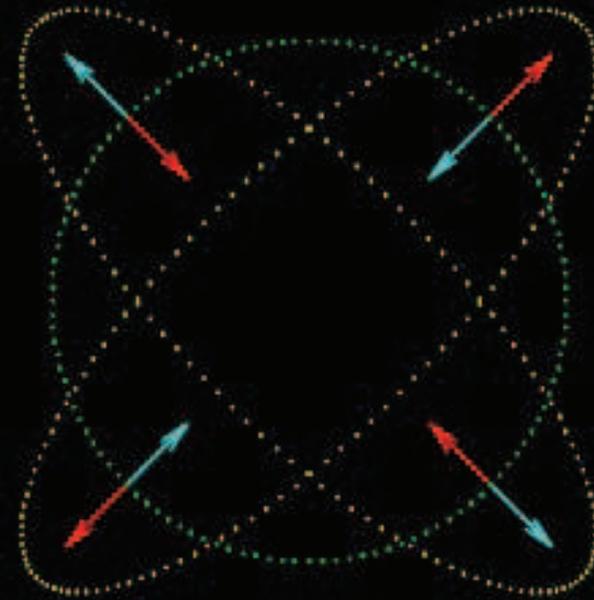
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Tidal Action of Gravitational Waves

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Plus polarization



Cross polarization

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- **GW Polarization**
 - In Einstein's theory **two polarizations** - plus and cross

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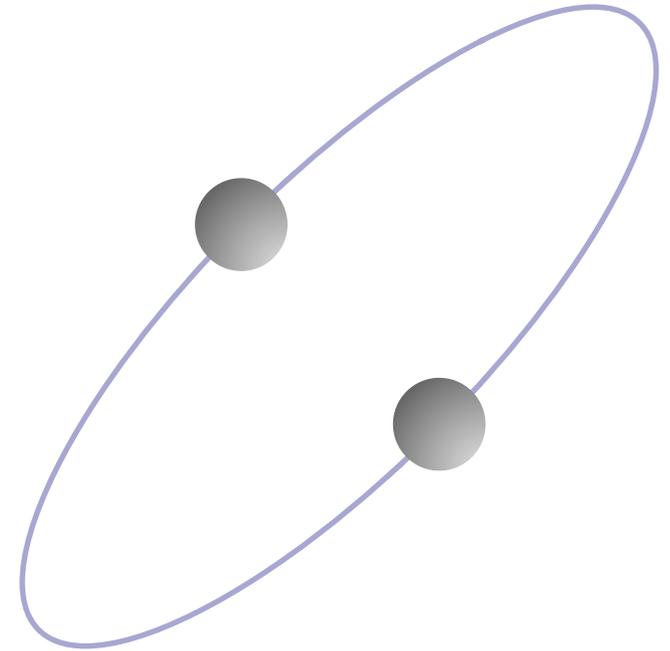
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- GW detectors are sensitive to the amplitude of the radiation
- Sensitive to wide areas over the sky

A persistent source of GW

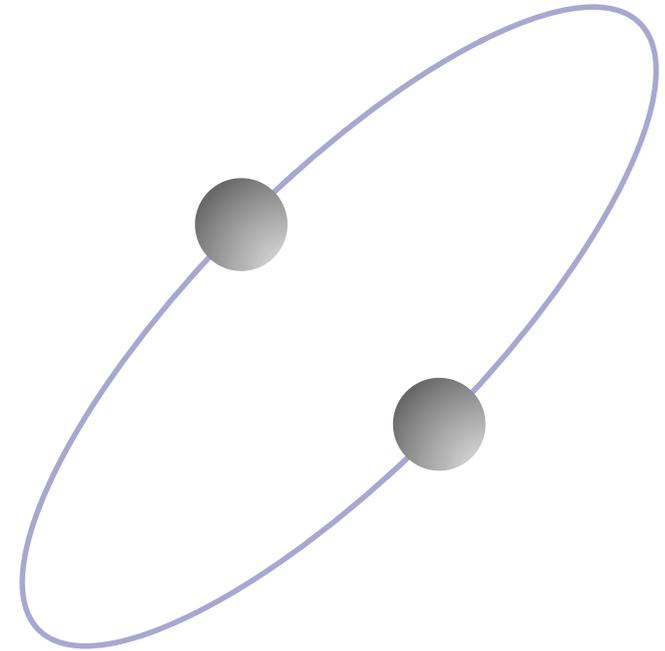
PSR 1913+16



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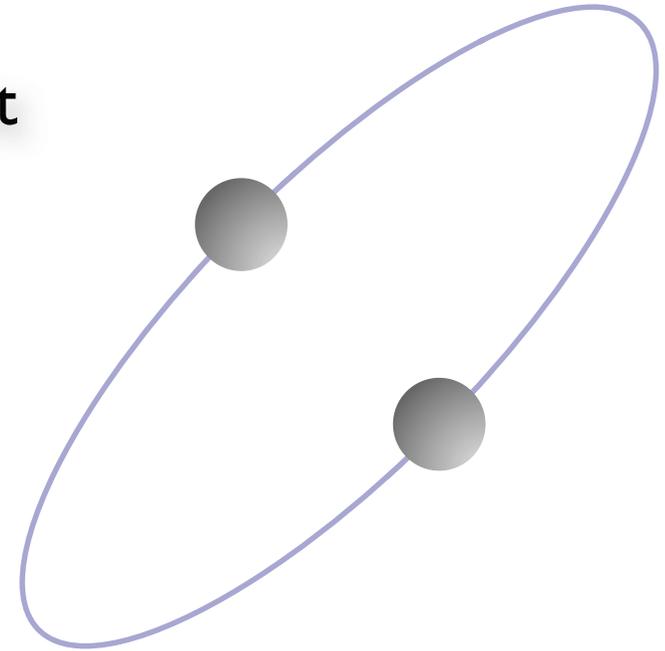
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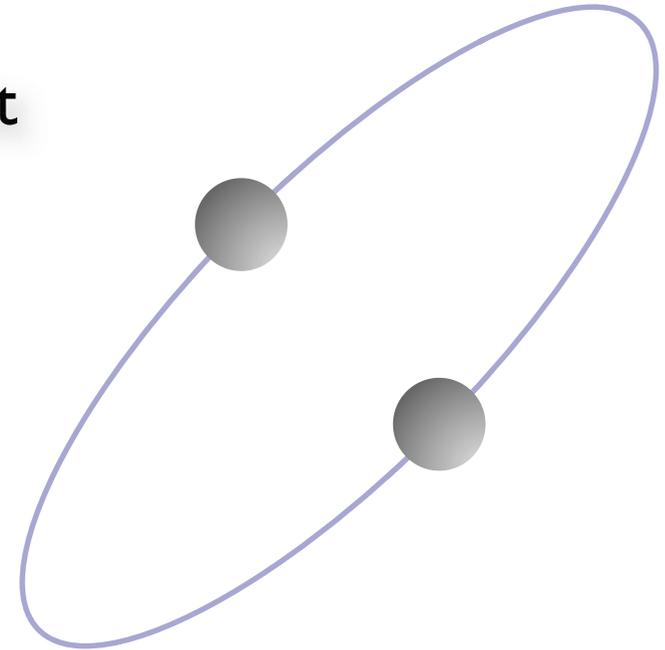
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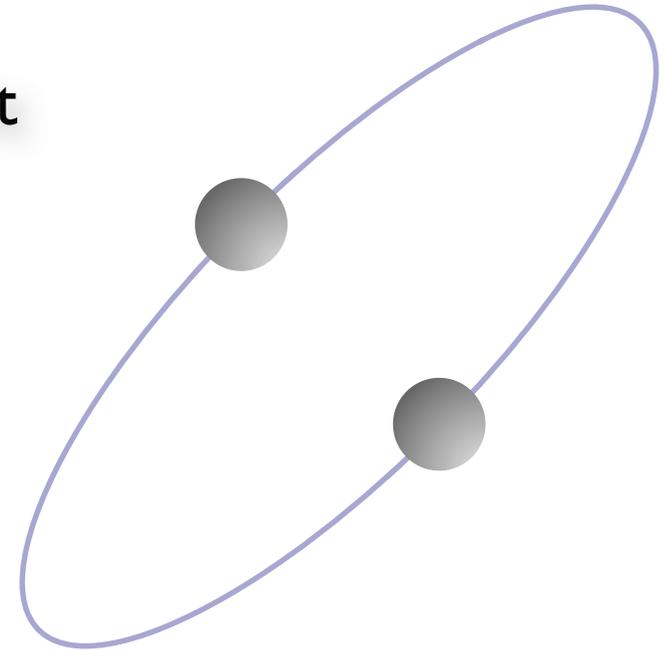
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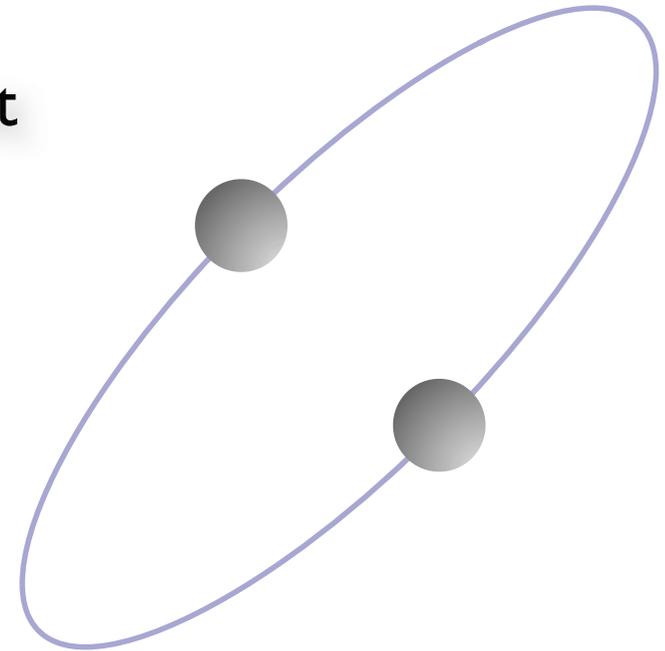
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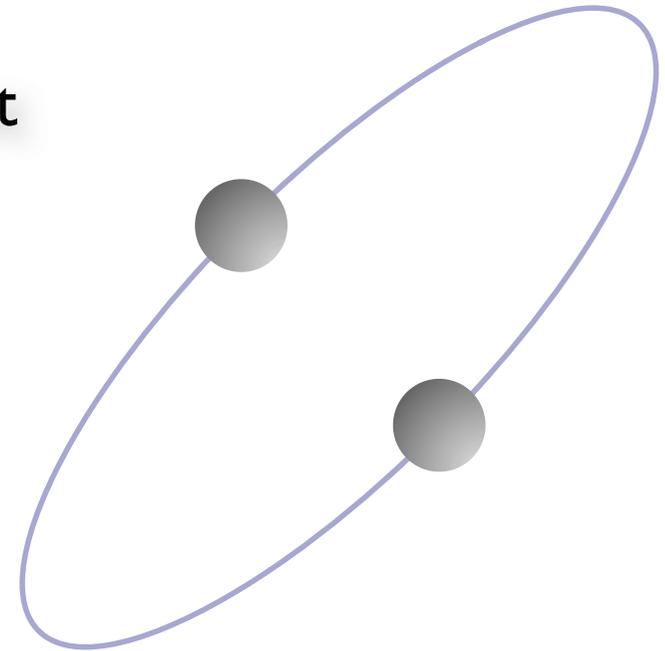
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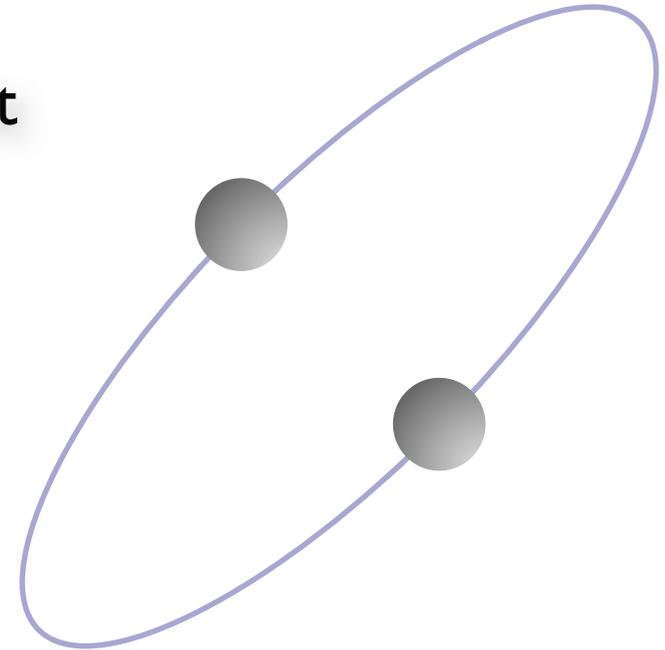
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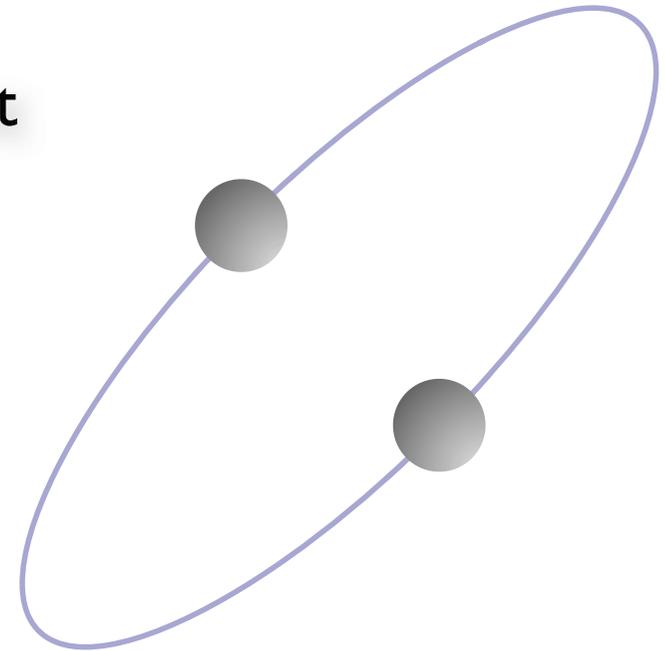
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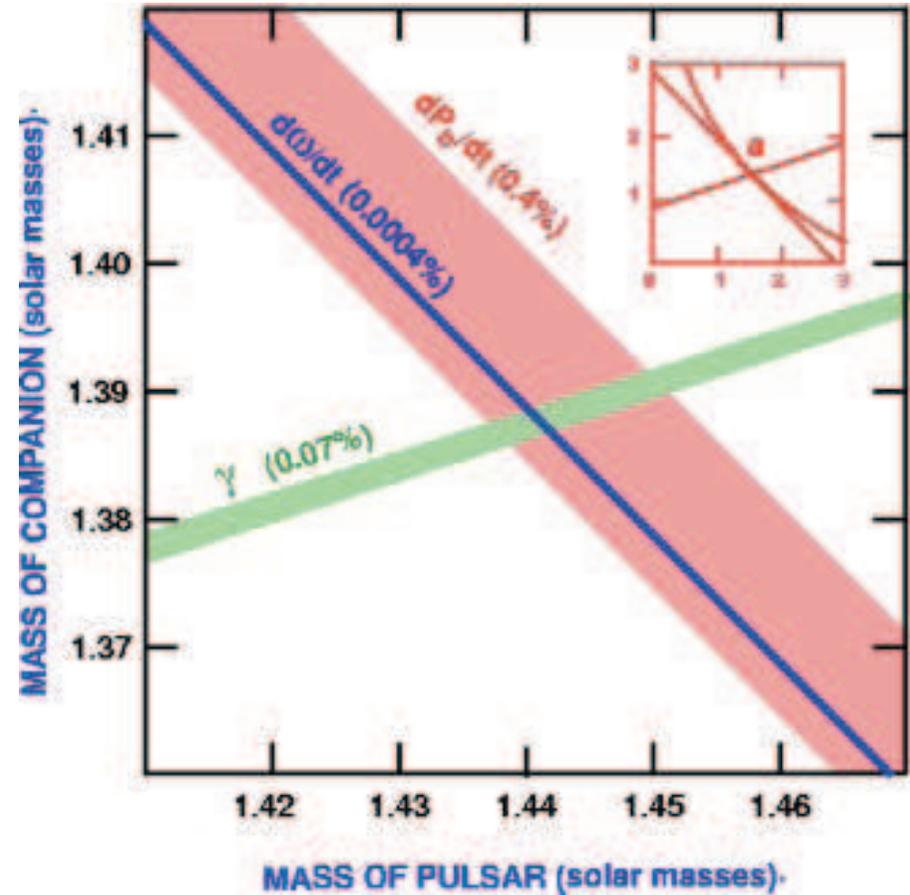
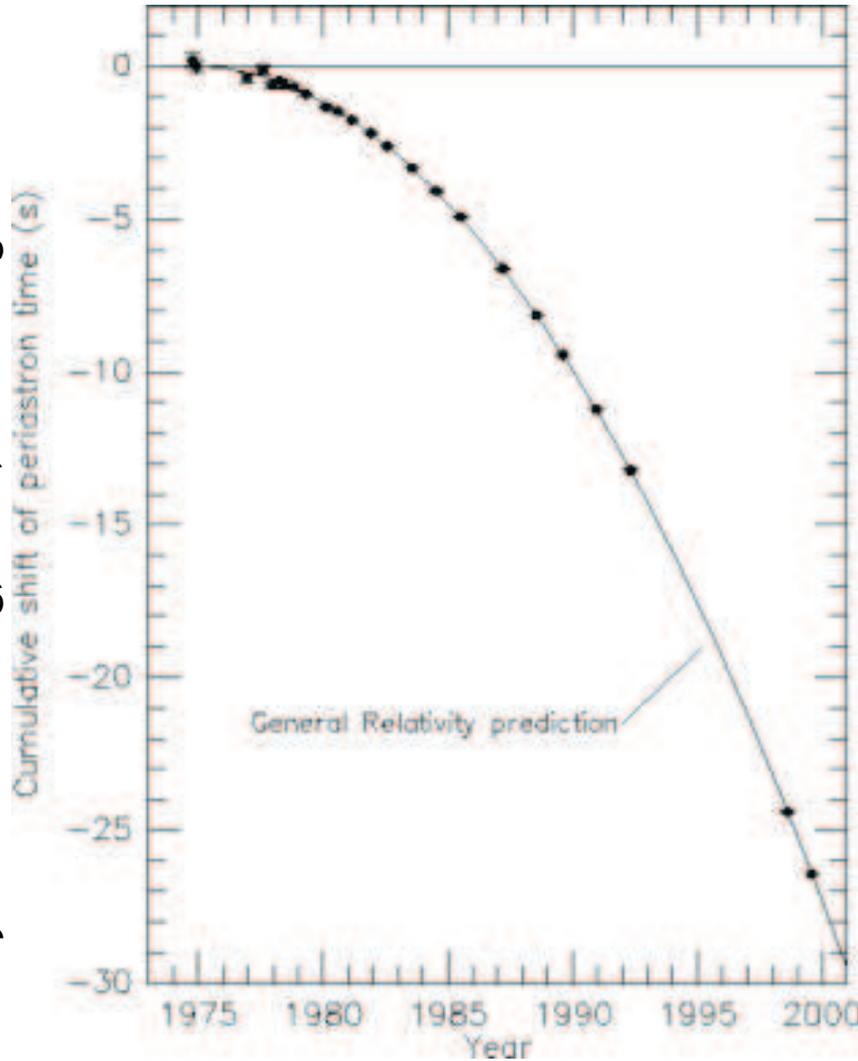
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 - The stars spiral in toward each other, causing a decrease in the period
 - Observed decrease in period - about 10 micro seconds per year - is in agreement with Einstein's theory to fraction of a percent



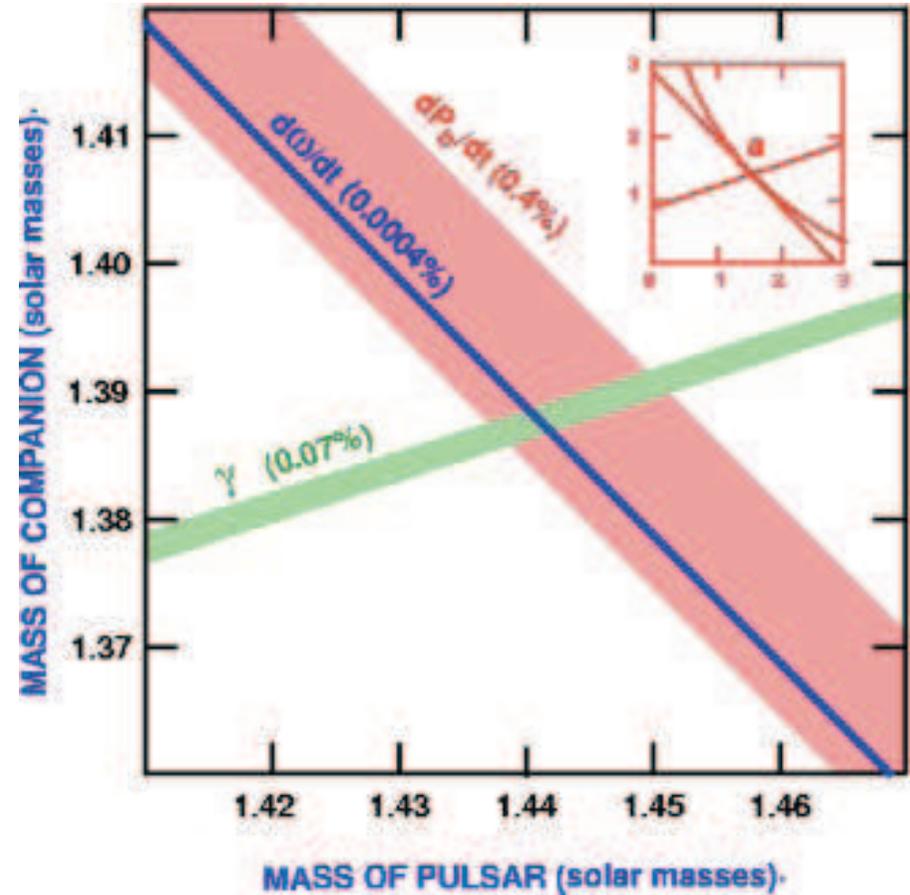
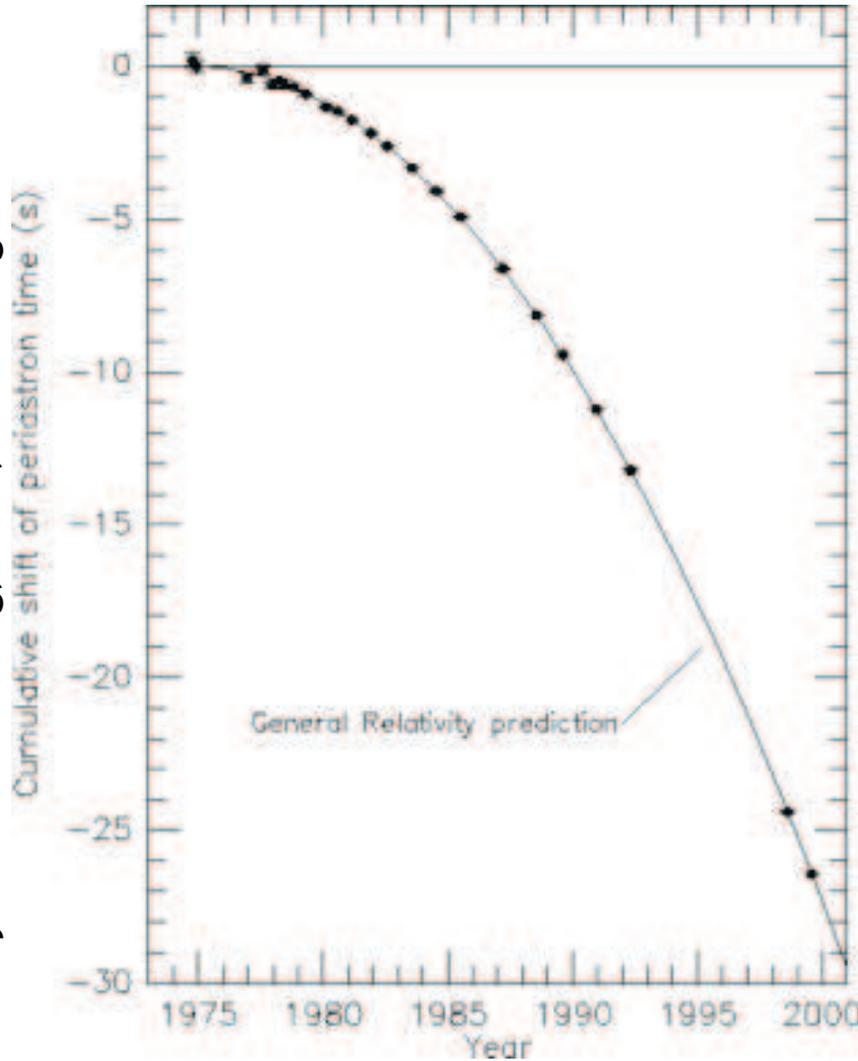
Accumulated orbital phase shift in PSR 1913+16

Taylor and Weisberg, 2000, Will Living Review



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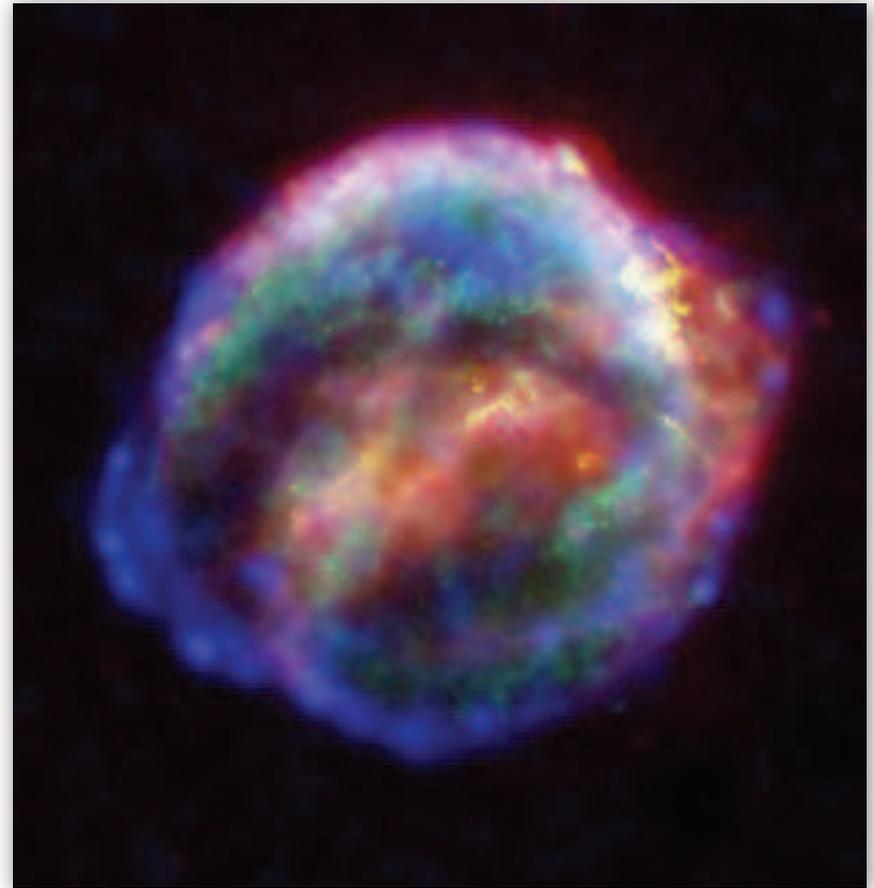


Eventually the two stars will coalesce, but that will take another 100 million years

Sources of Gravitational Waves

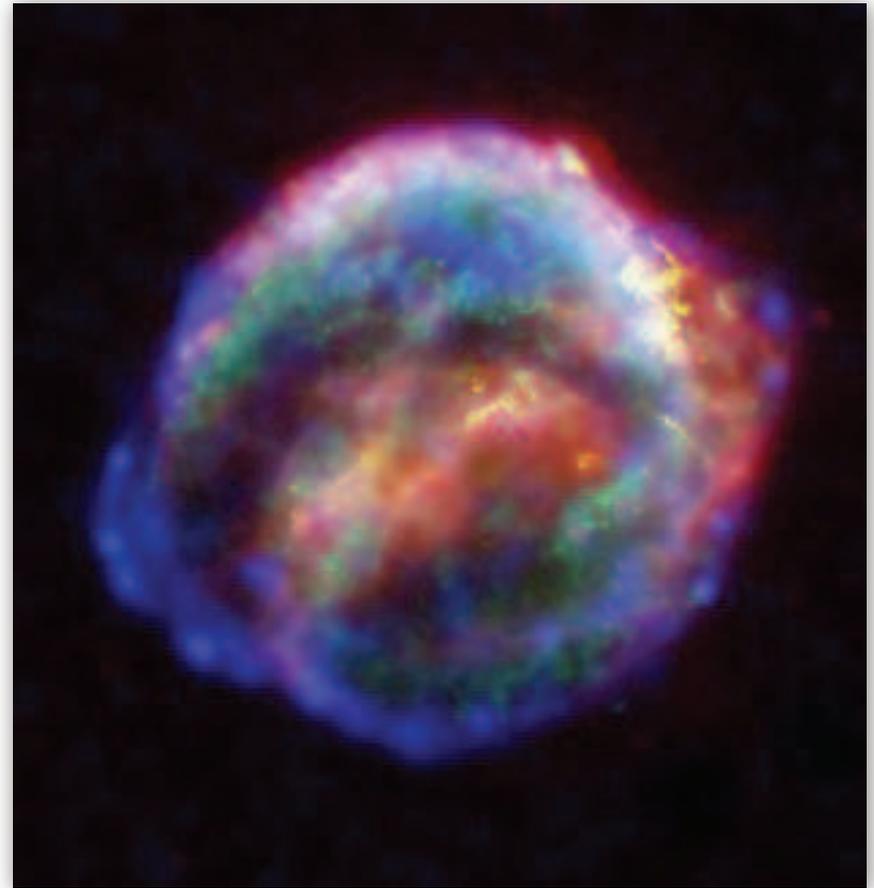


Burst Sources



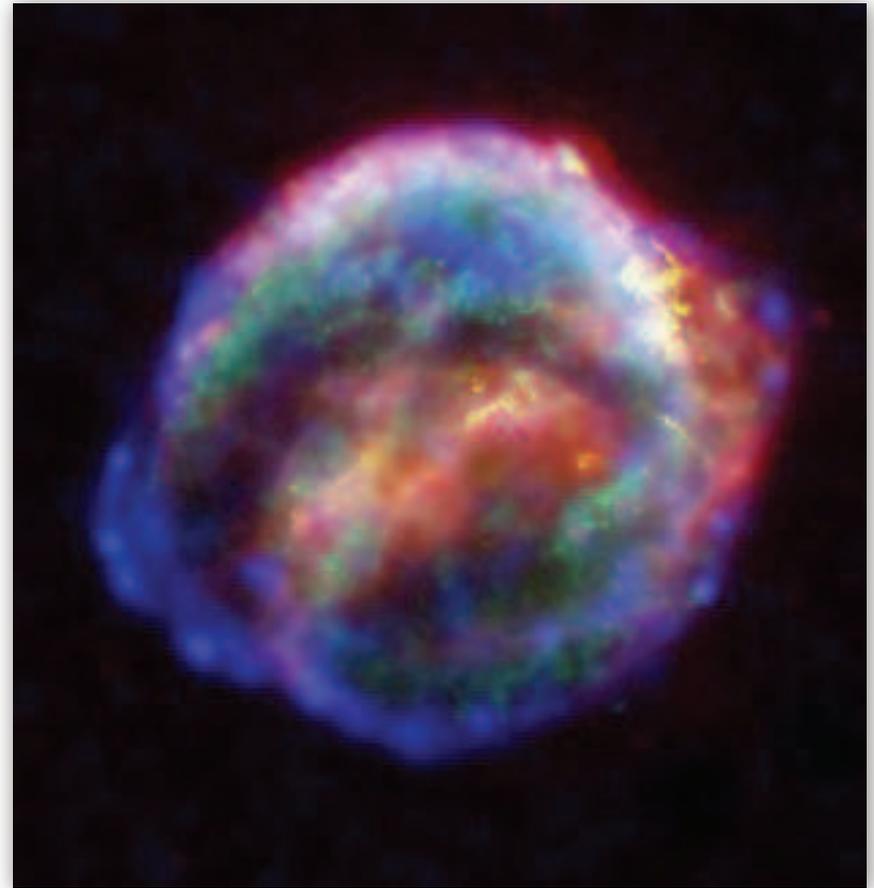
Burst Sources

- Gravitational wave bursts



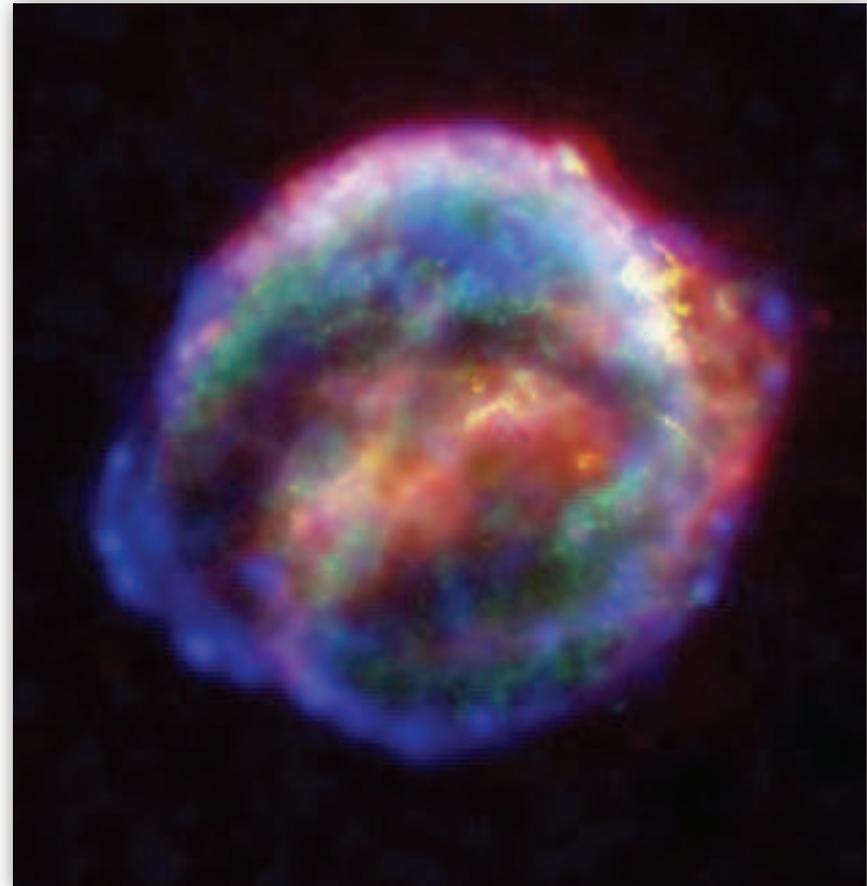
Burst Sources

- Gravitational wave bursts
- Black hole collisions



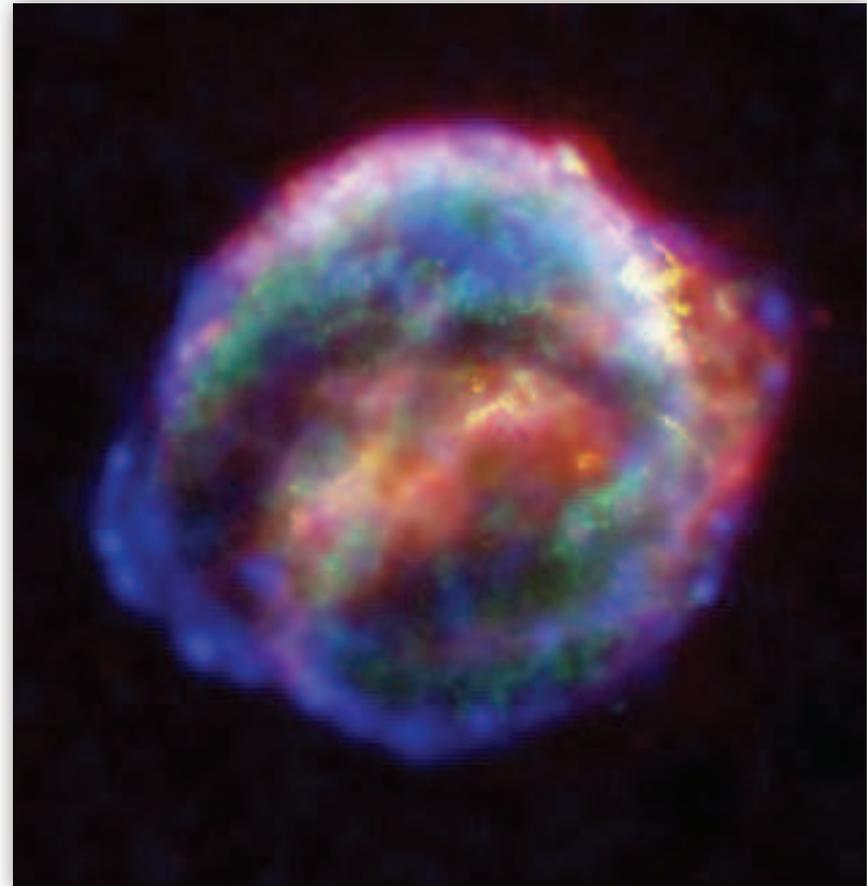
Burst Sources

- Gravitational wave bursts
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 - Supernovae



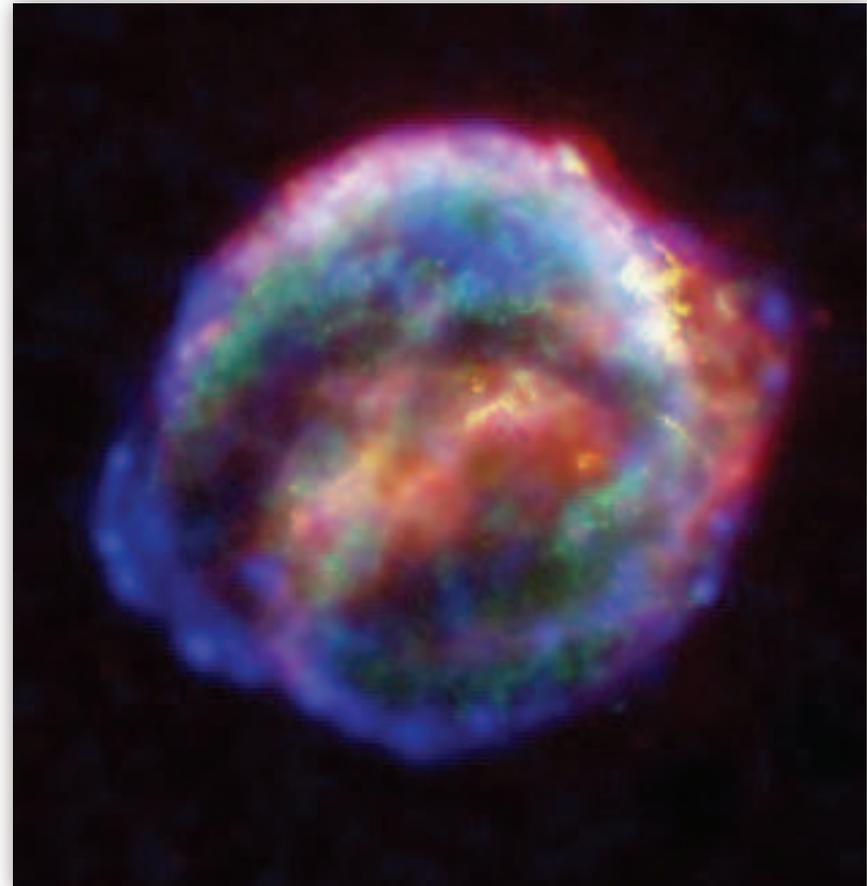
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 - gamma-ray bursts (GRBs)



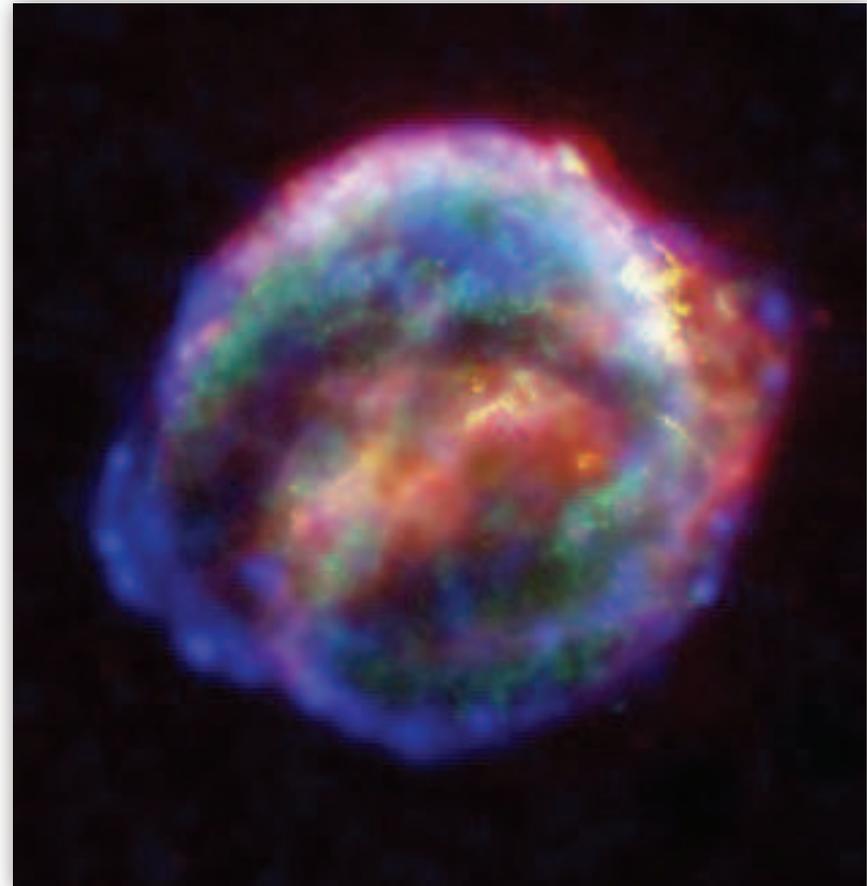
Burst Sources

- Gravitational wave bursts
 - Black hole collisions
 - Supernovae
 - gamma-ray bursts (GRBs)
- Short-hard GRBs



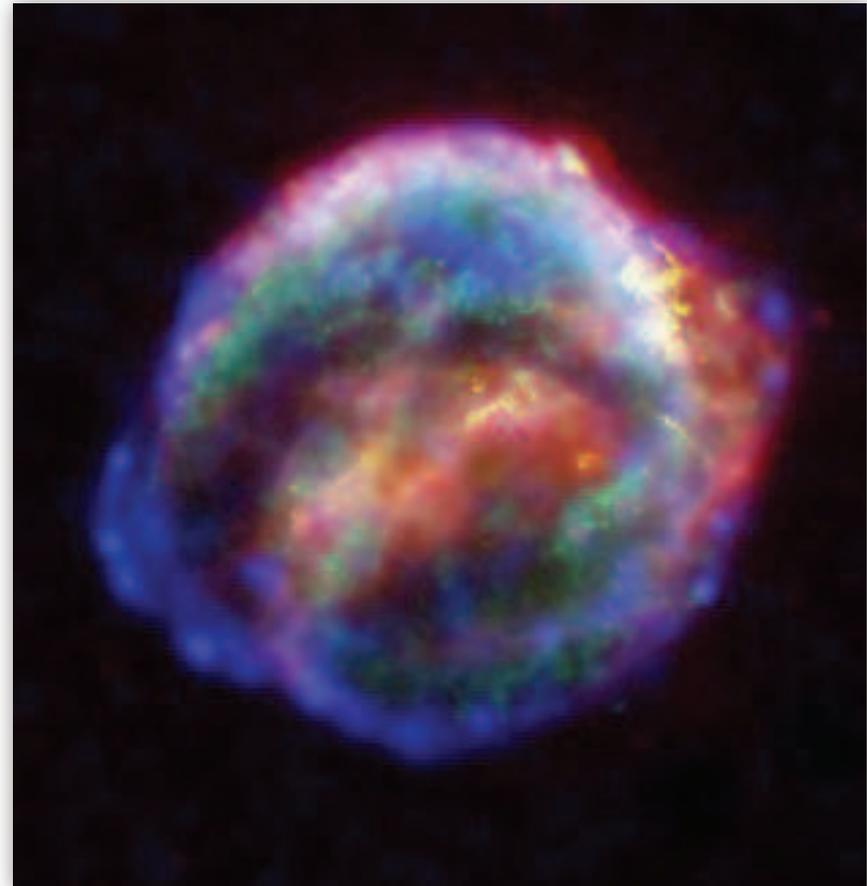
Burst Sources

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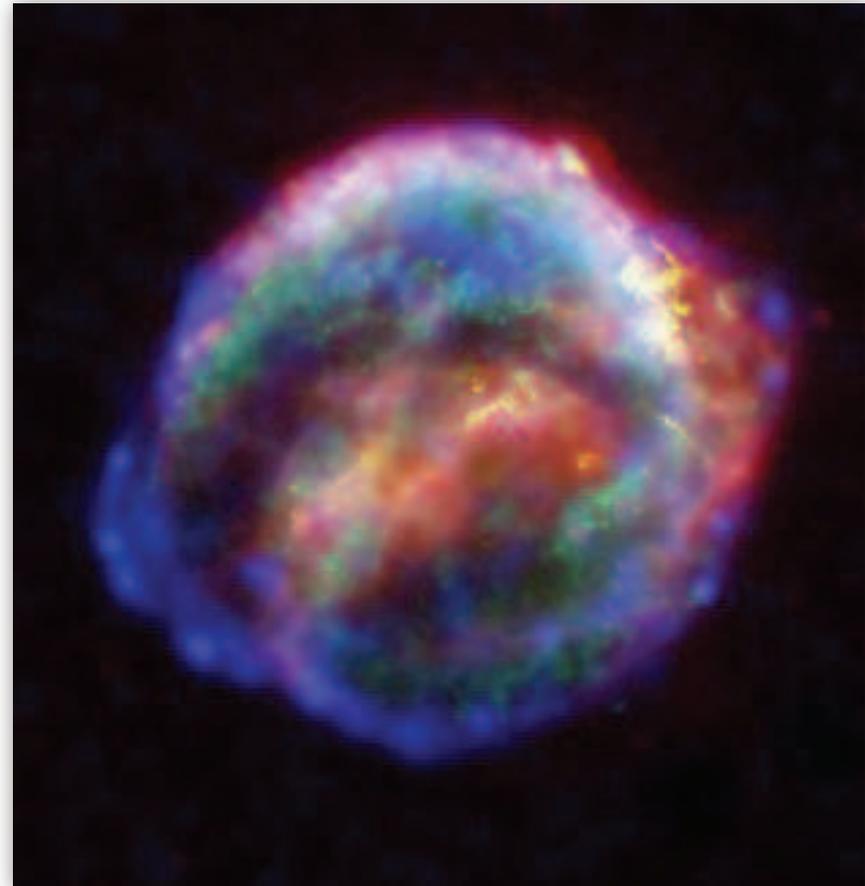
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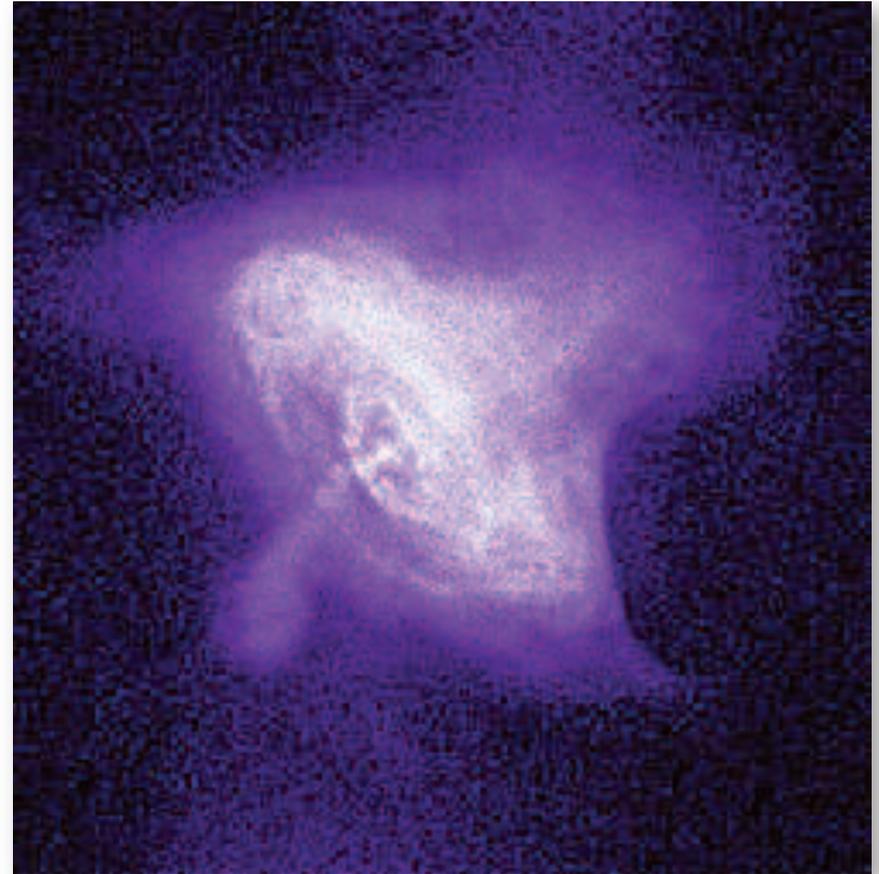


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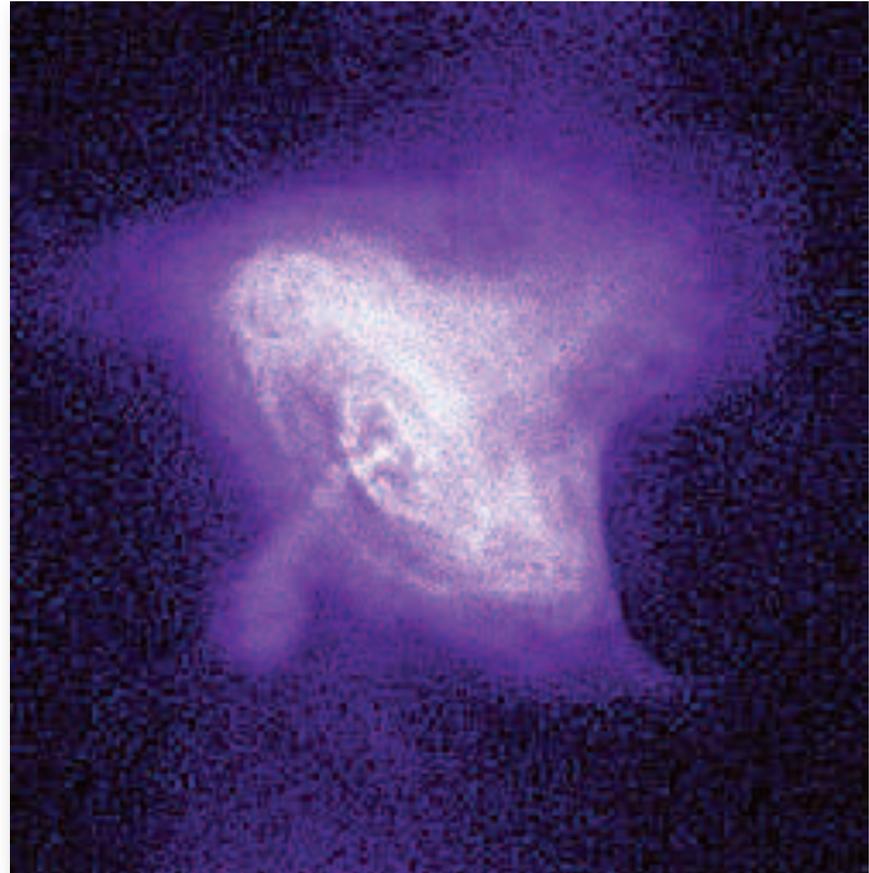


Continuous Wave Sources



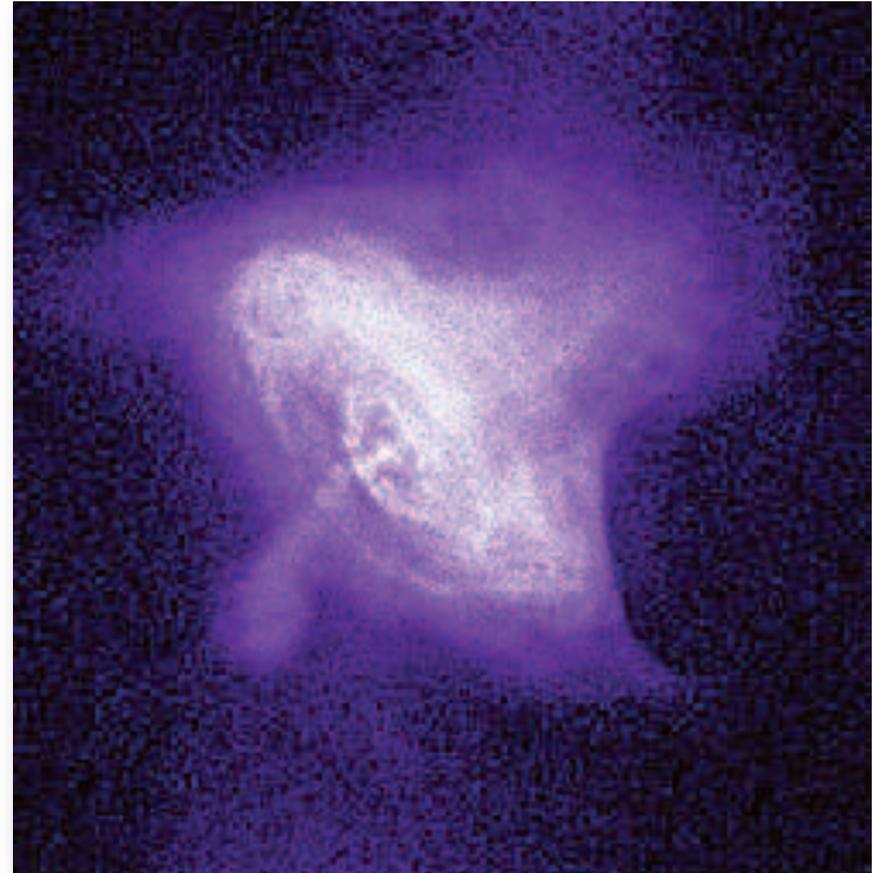
Continuous Wave Sources

- Rapidly spinning neutron stars or other objects



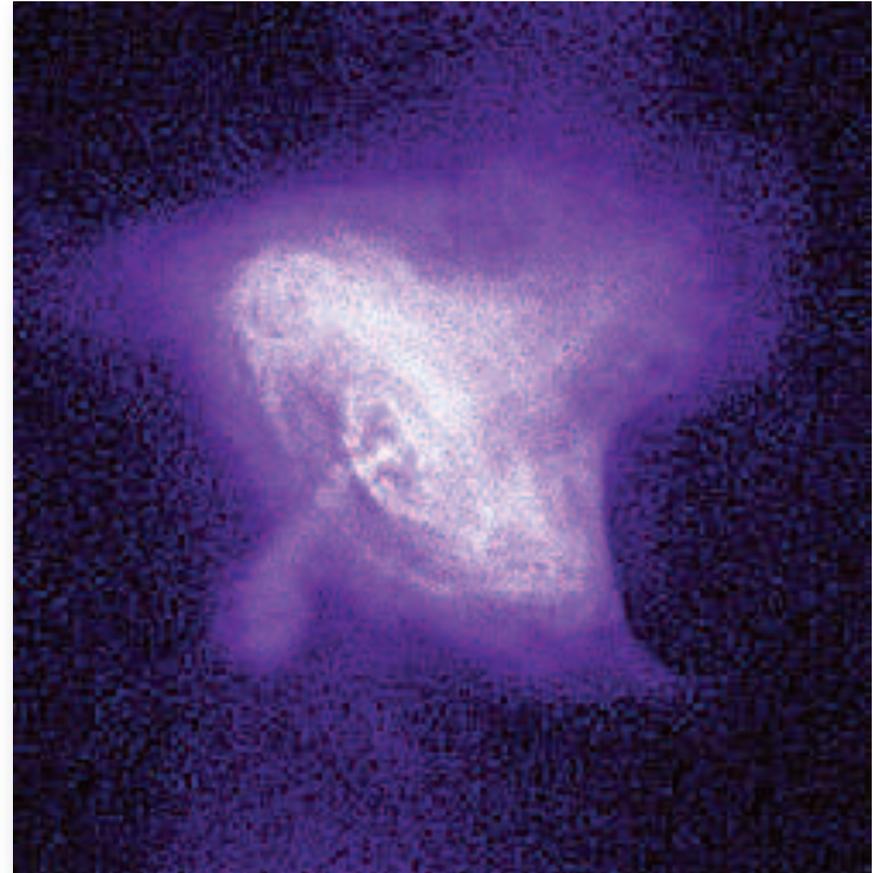
Continuous Wave Sources

- Rapidly spinning neutron stars or other objects
- Mountains on neutron stars



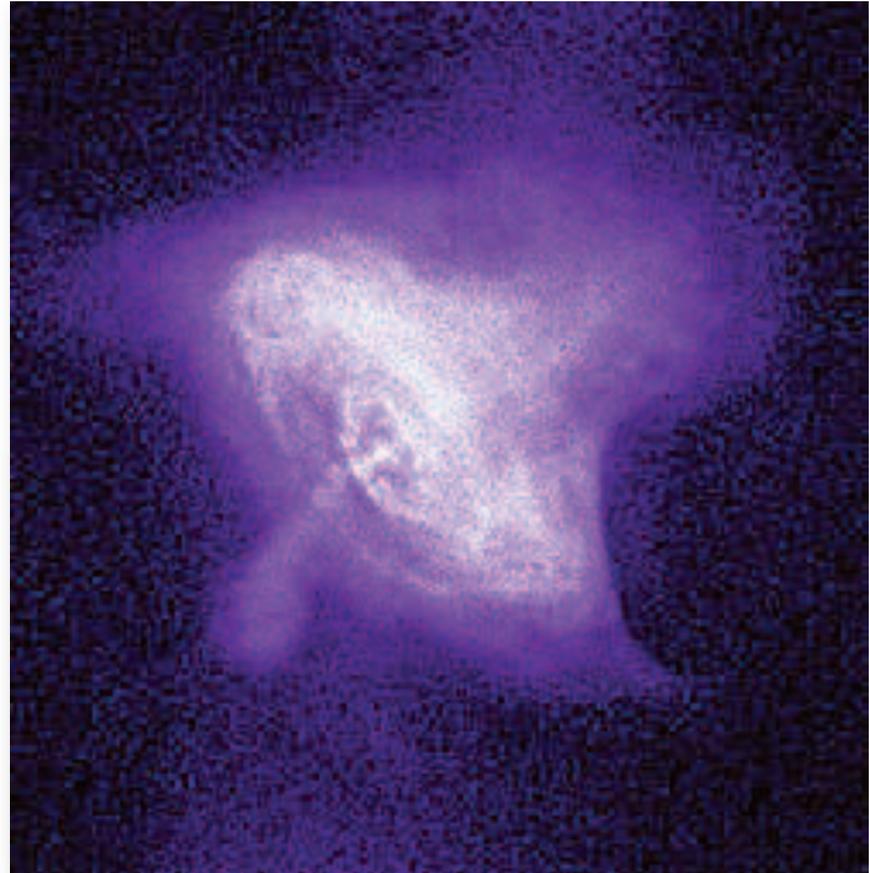
Continuous Wave Sources

- Rapidly spinning neutron stars or other objects
- Mountains on neutron stars
- Low mass X-ray binaries



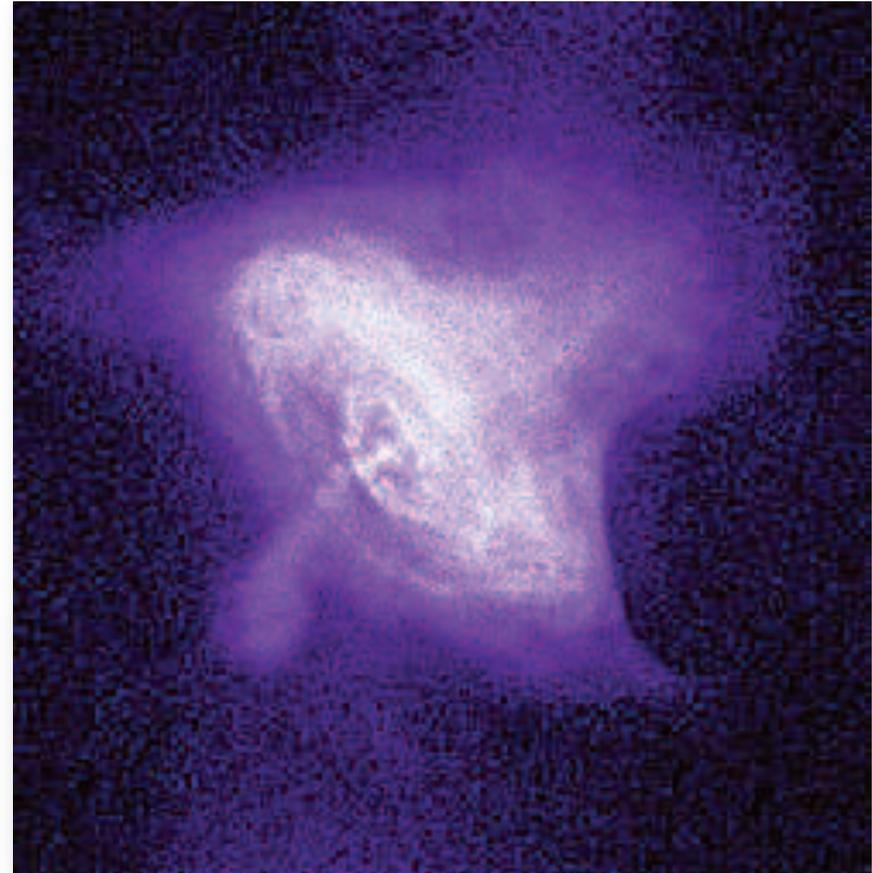
Continuous Wave Sources

- Rapidly spinning neutron stars or other objects
- Mountains on neutron stars
- Low mass X-ray binaries
- Accretion induced asymmetry



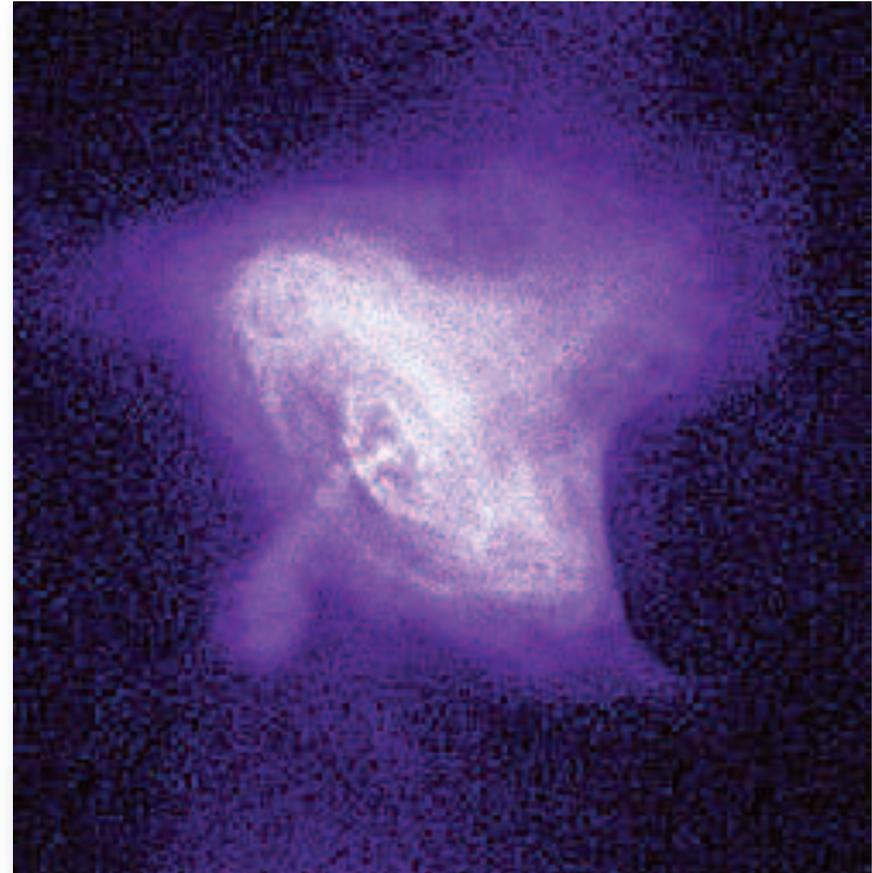
Continuous Wave Sources

- Rapidly spinning neutron stars or other objects
- Mountains on neutron stars
- Low mass X-ray binaries
- Accretion induced asymmetry
- Magnetars and other compact objects



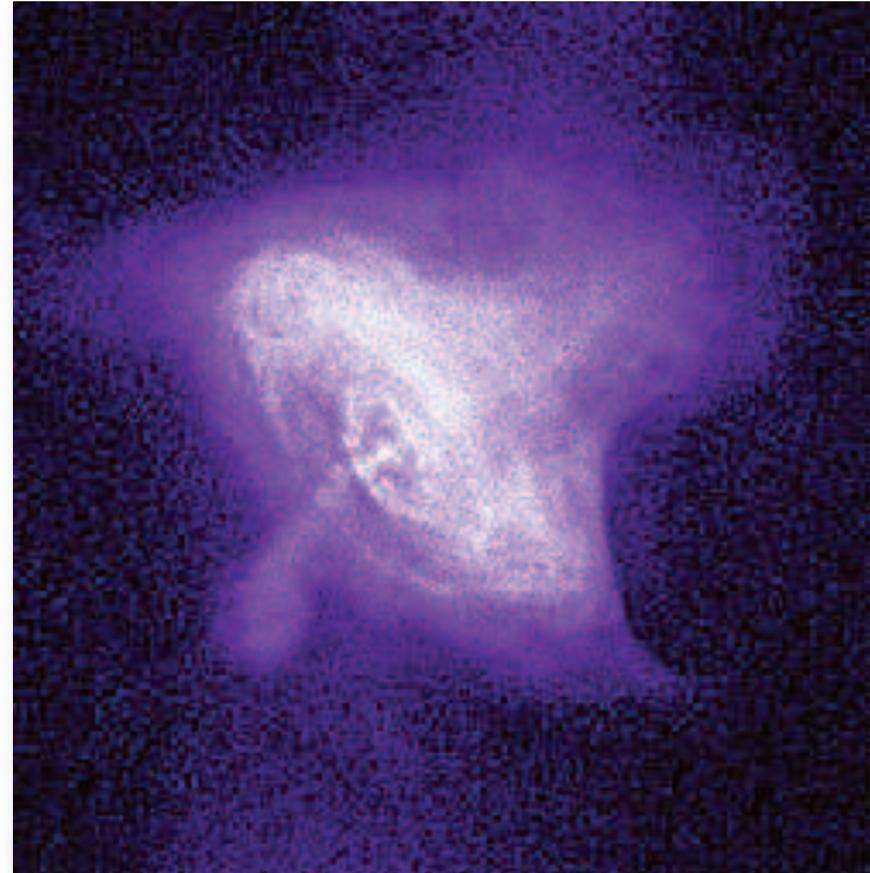
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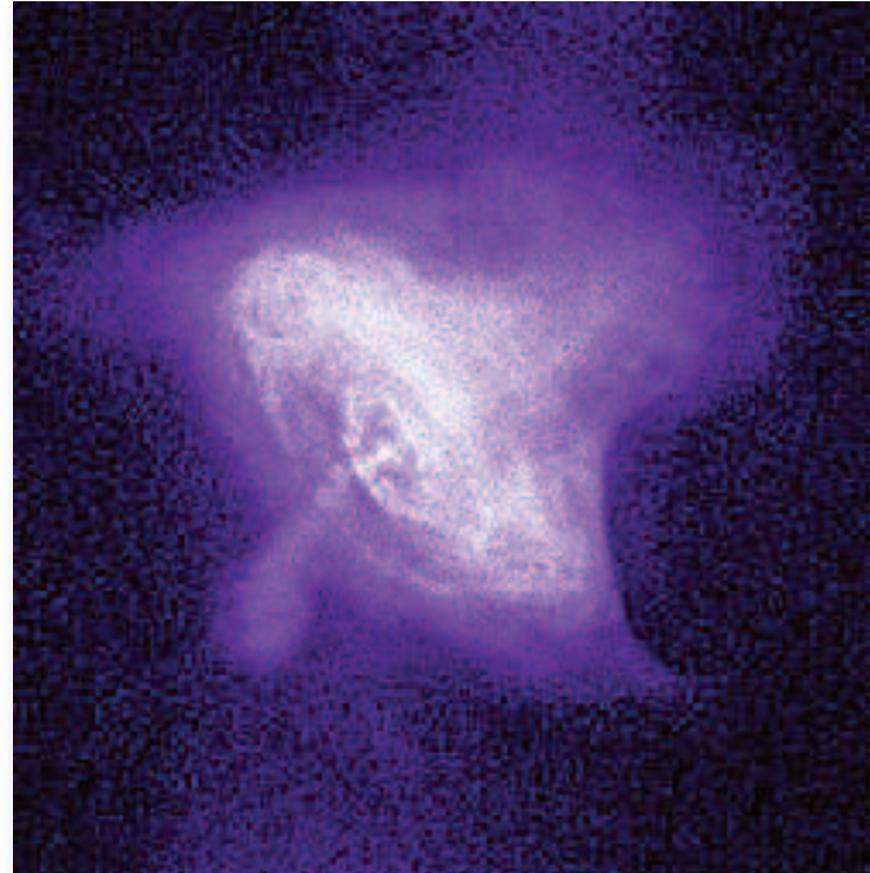
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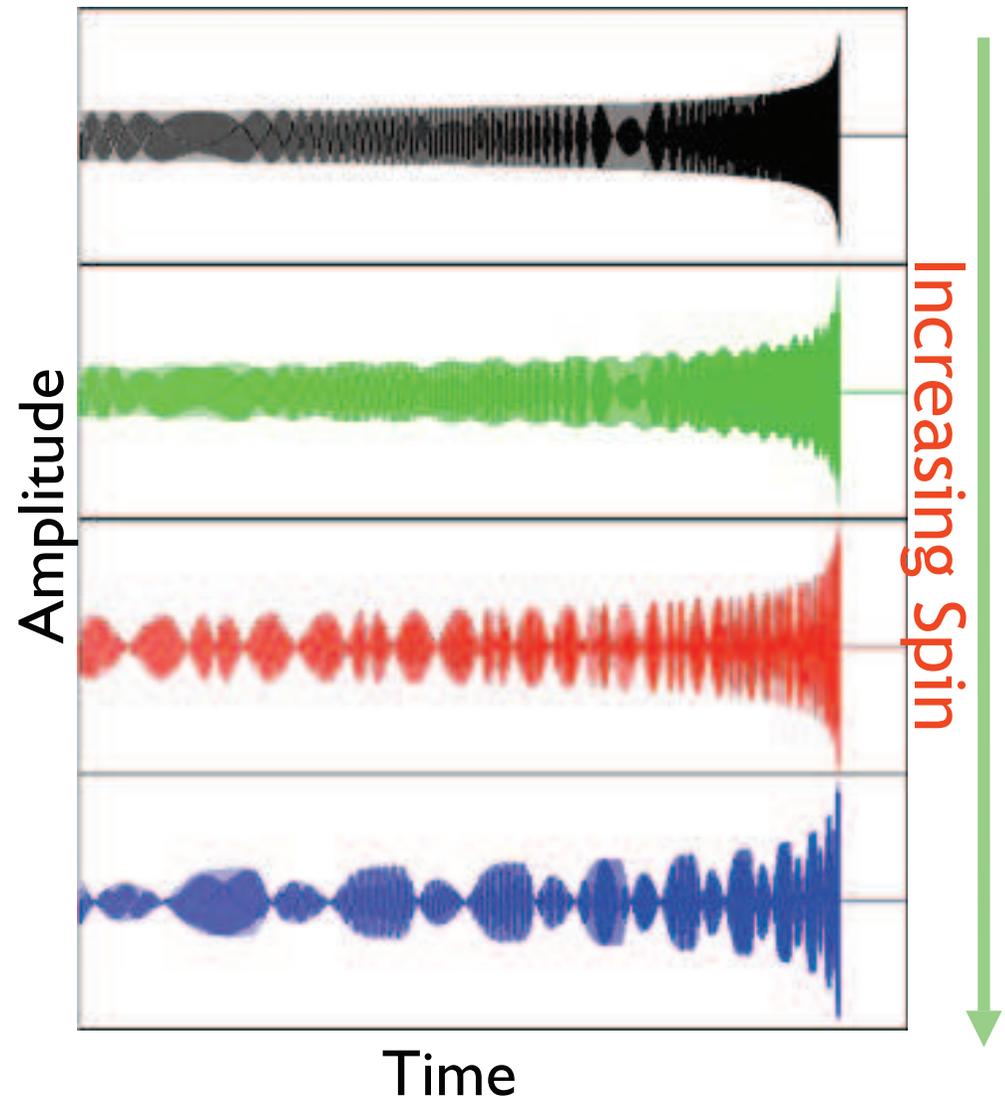


Continuous Wave Sources

- Rapidly spinning neutron stars or other objects
- Mountains on neutron stars
- Low mass X-ray binaries
- Accretion induced asymmetry
- Magnetars and other compact objects
- Magnetic field induced asymmetries
- Relativistic instabilities
- r-modes, etc.

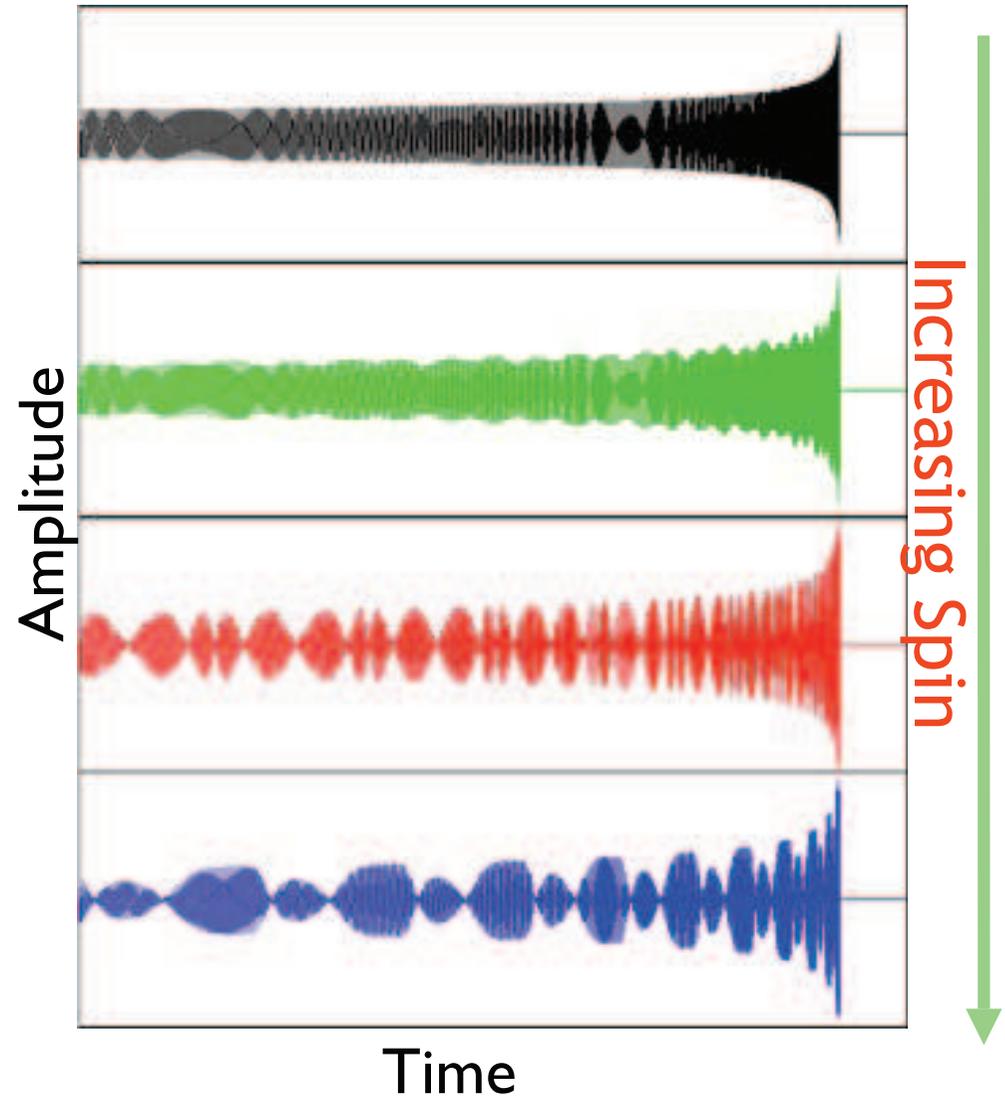


Waveforms from Inspiralling Binaries



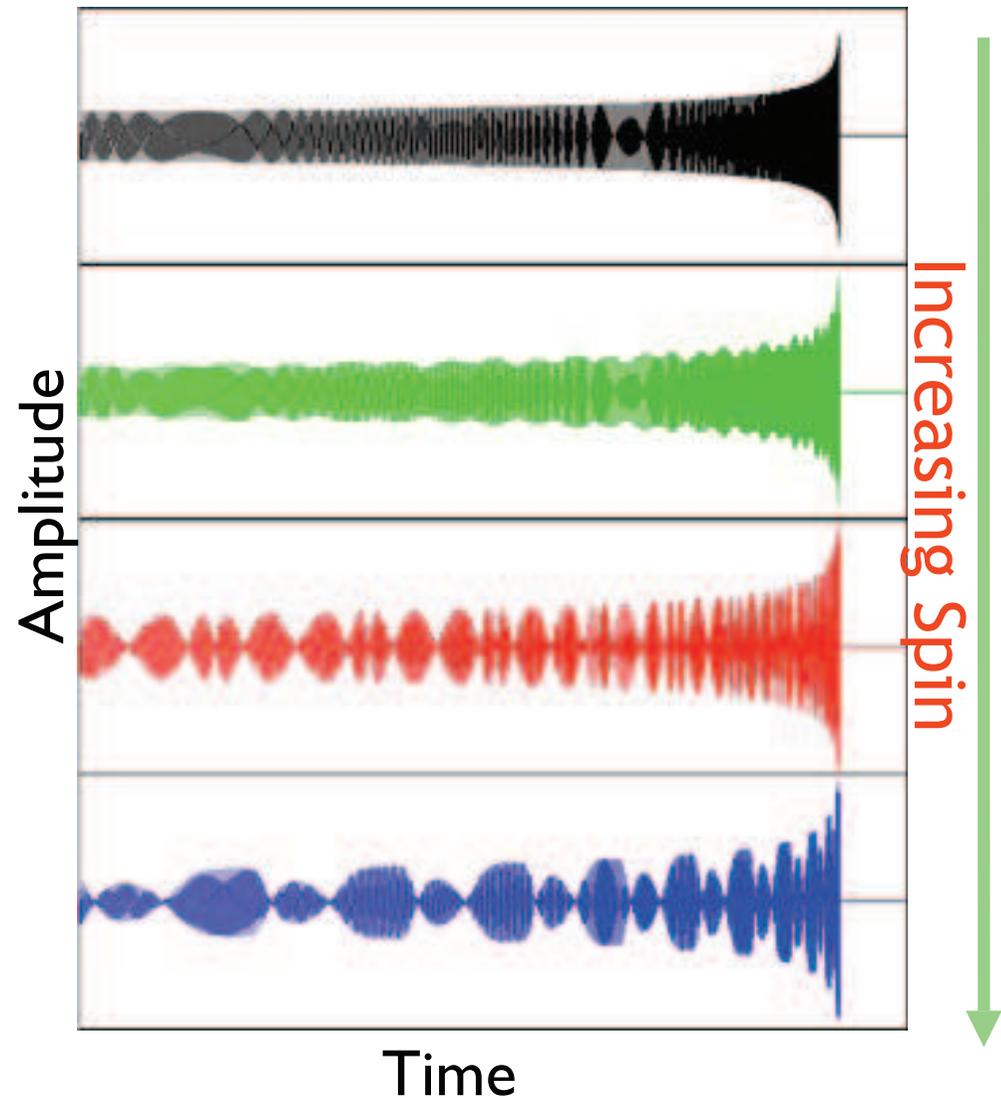
Waveforms from Inspiralling Binaries

- Late-time dynamics of compact binaries is highly relativistic, dictated by **non-linear general relativistic effects**



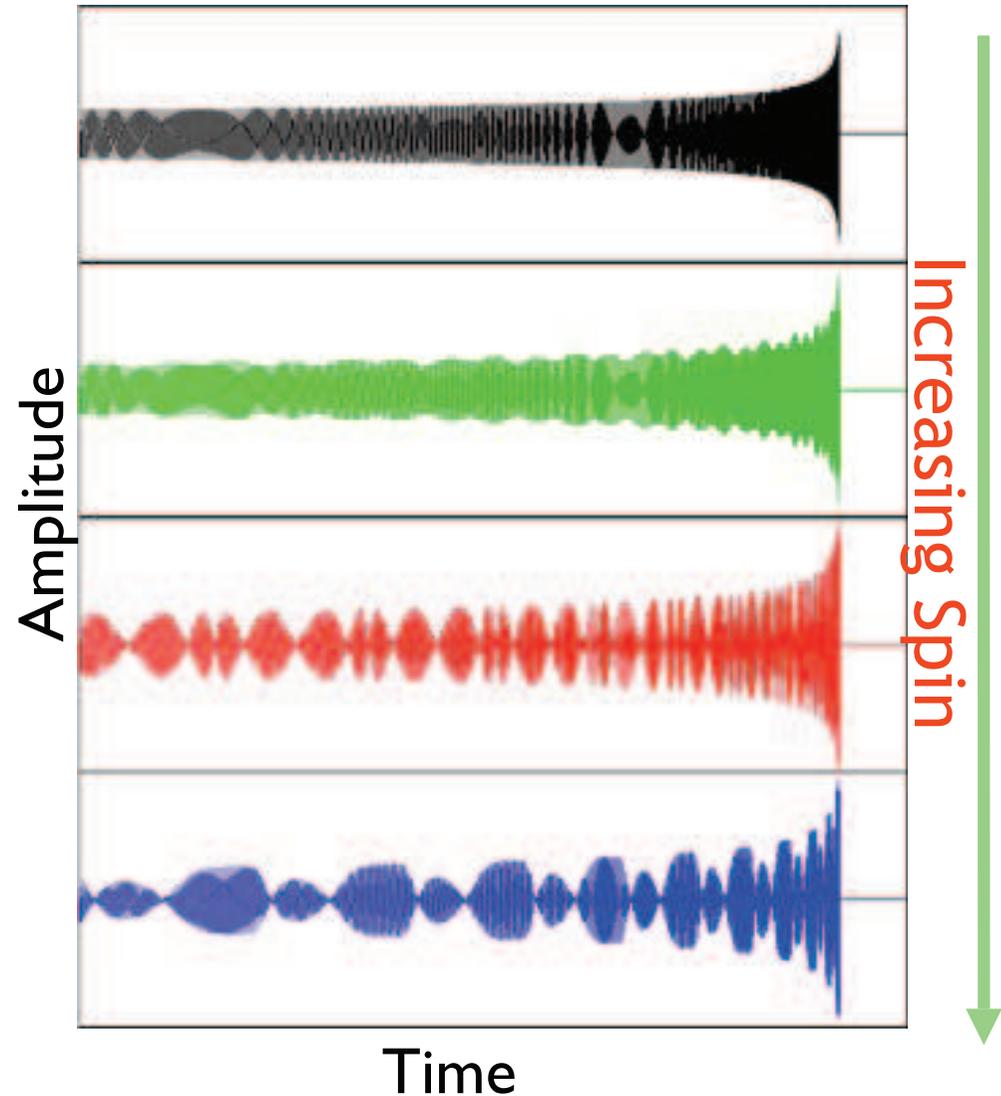
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Waveforms from Inspiralling Binaries

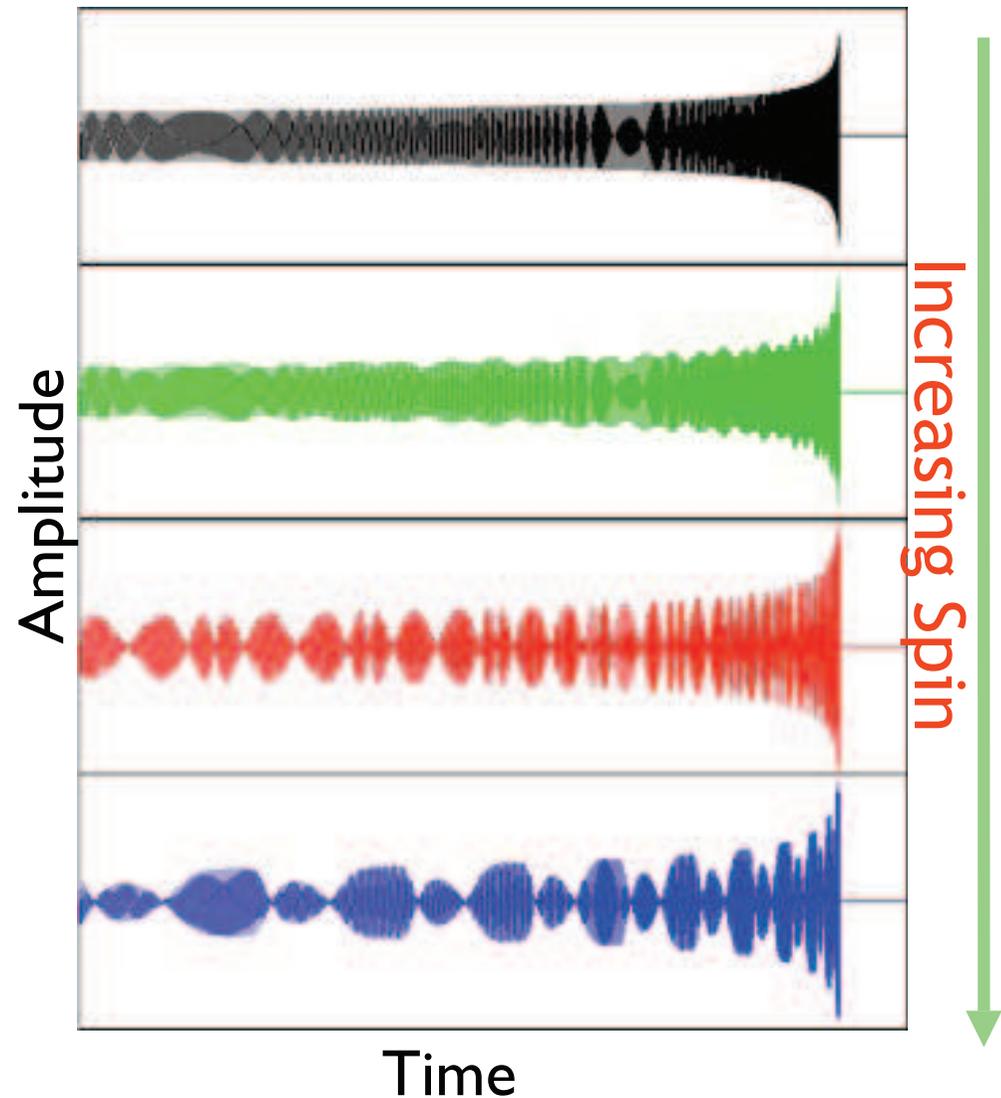
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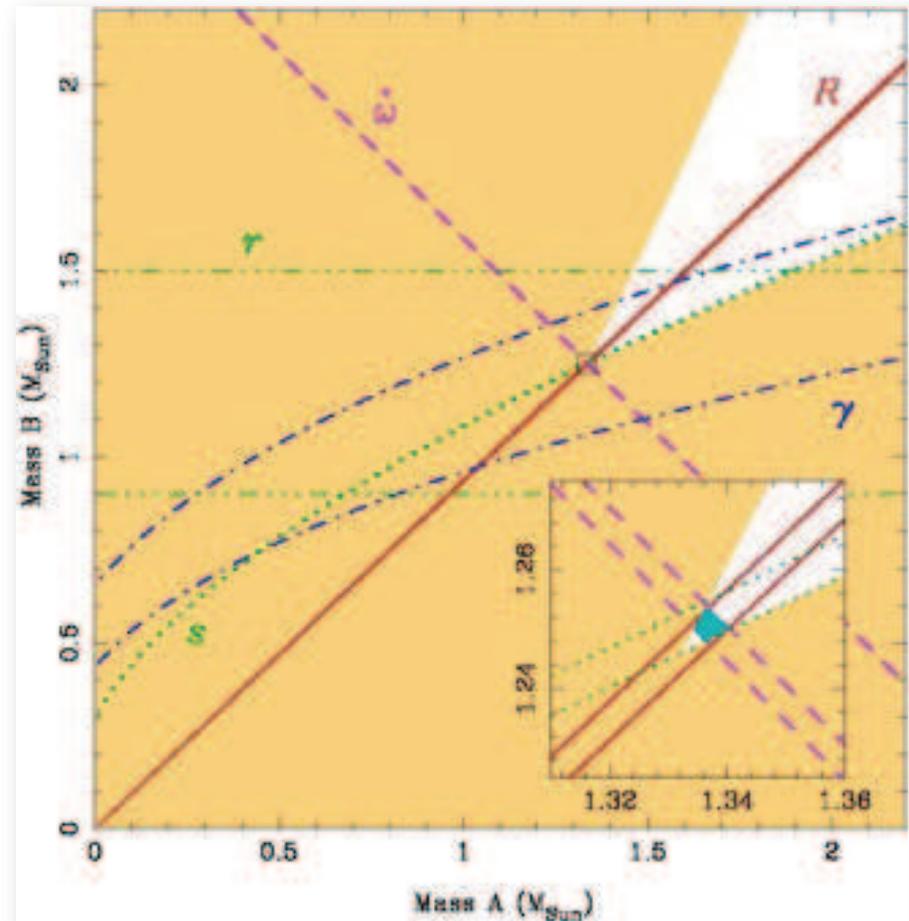
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$$h(t) = 4\eta \frac{M}{D} \frac{M}{r(t)} \cos 2\varphi(t)$$



Examples of Merging Neutron Star Binaries

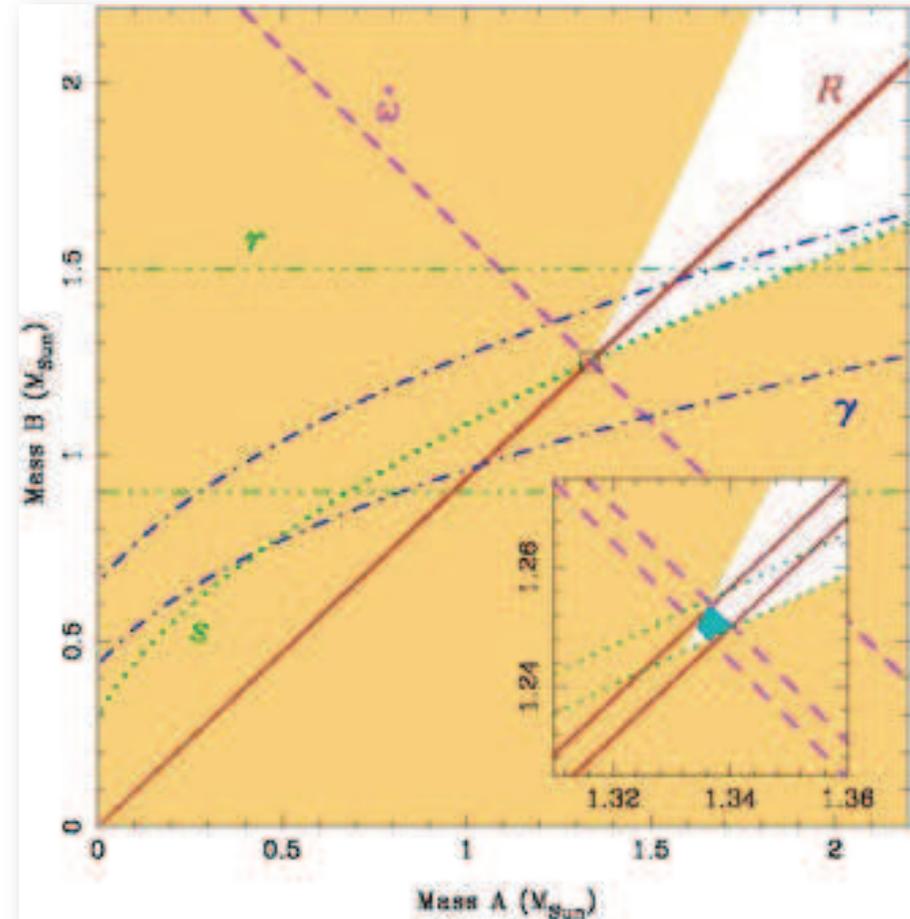
Burgay et al Nature 2003



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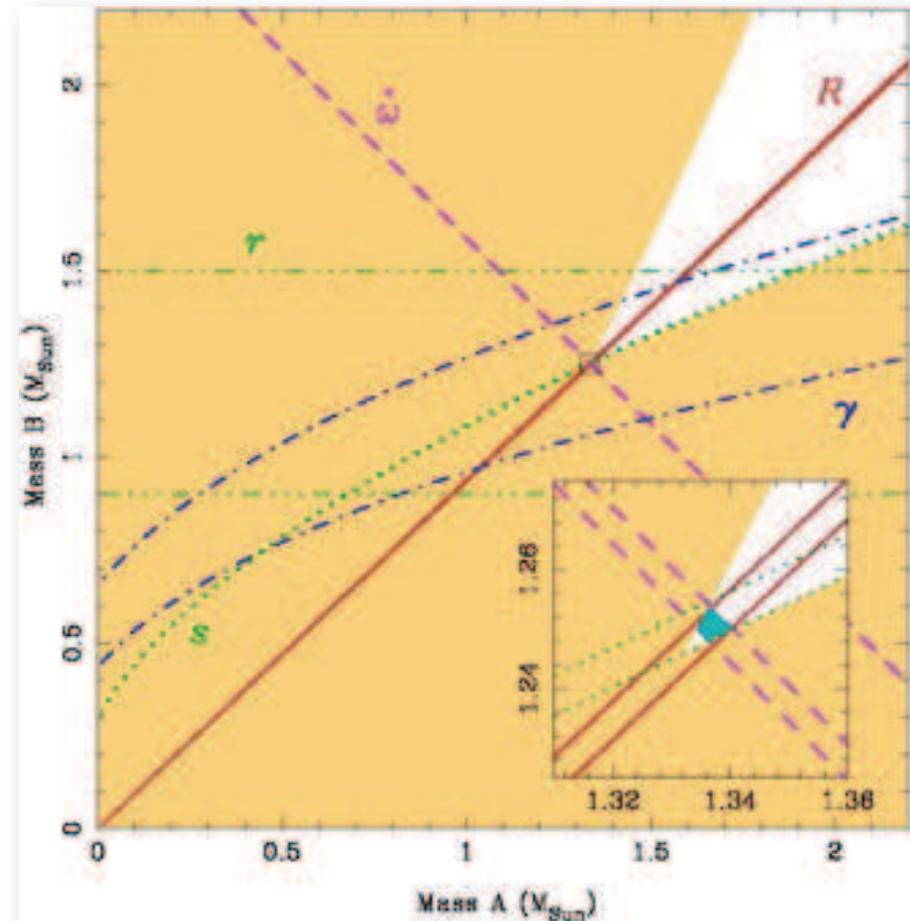
• PSR 1913+16, J0737-3039



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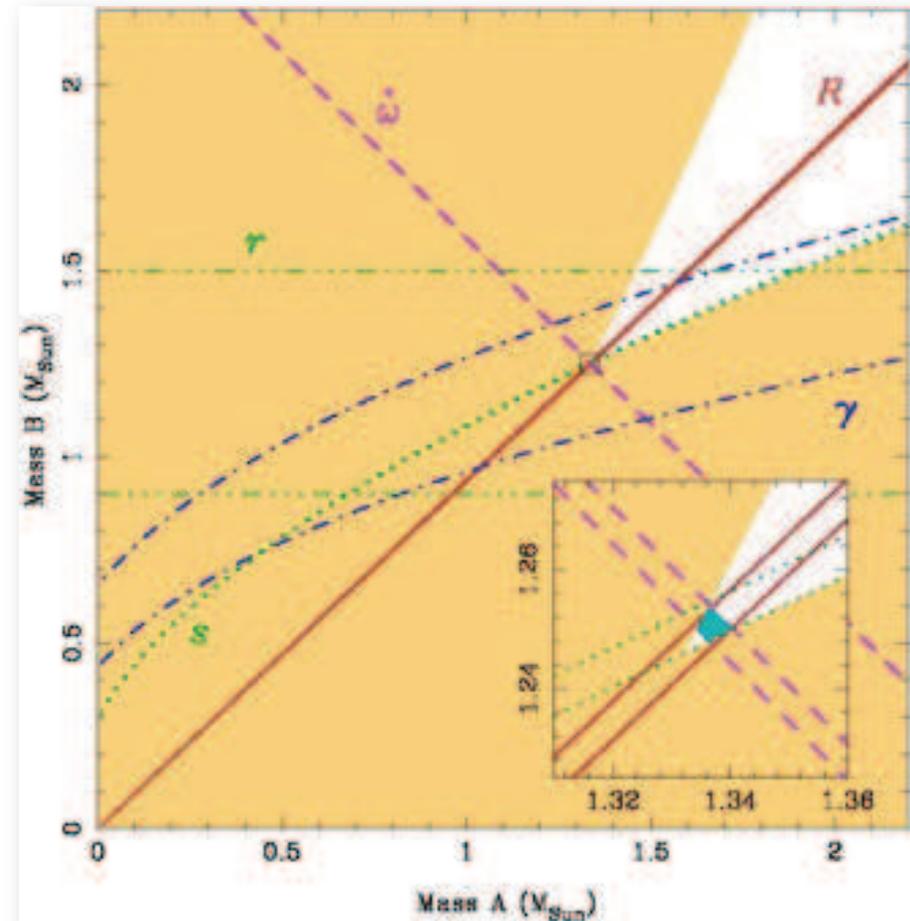
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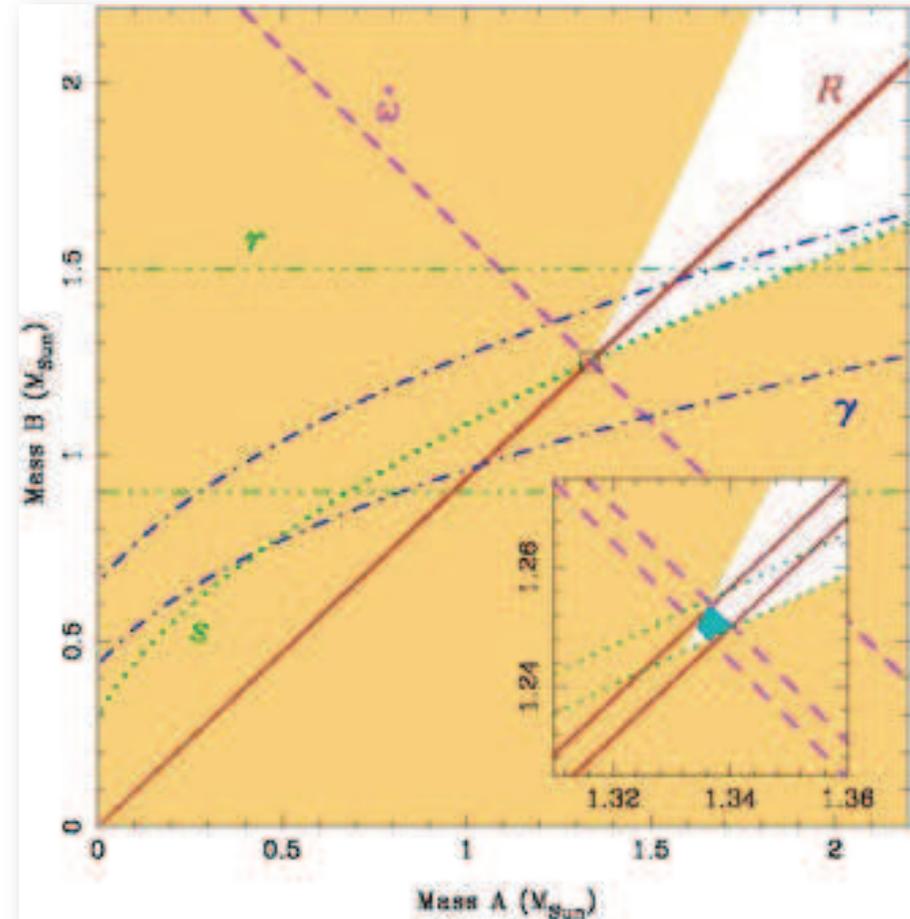
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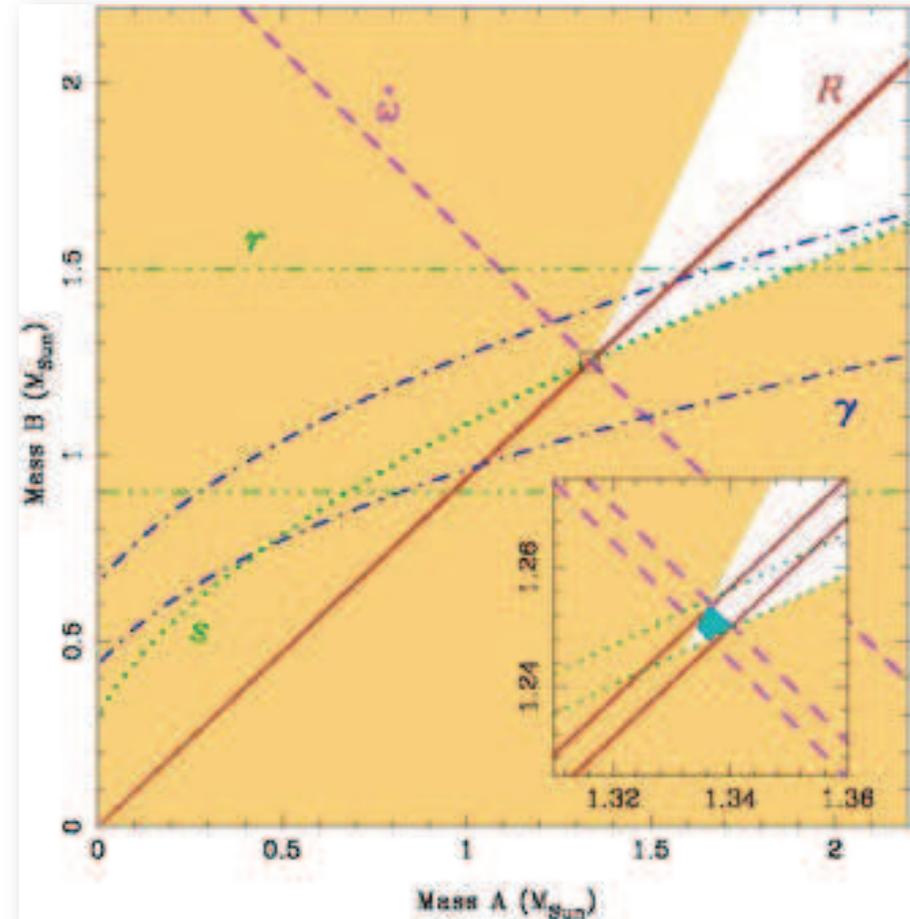
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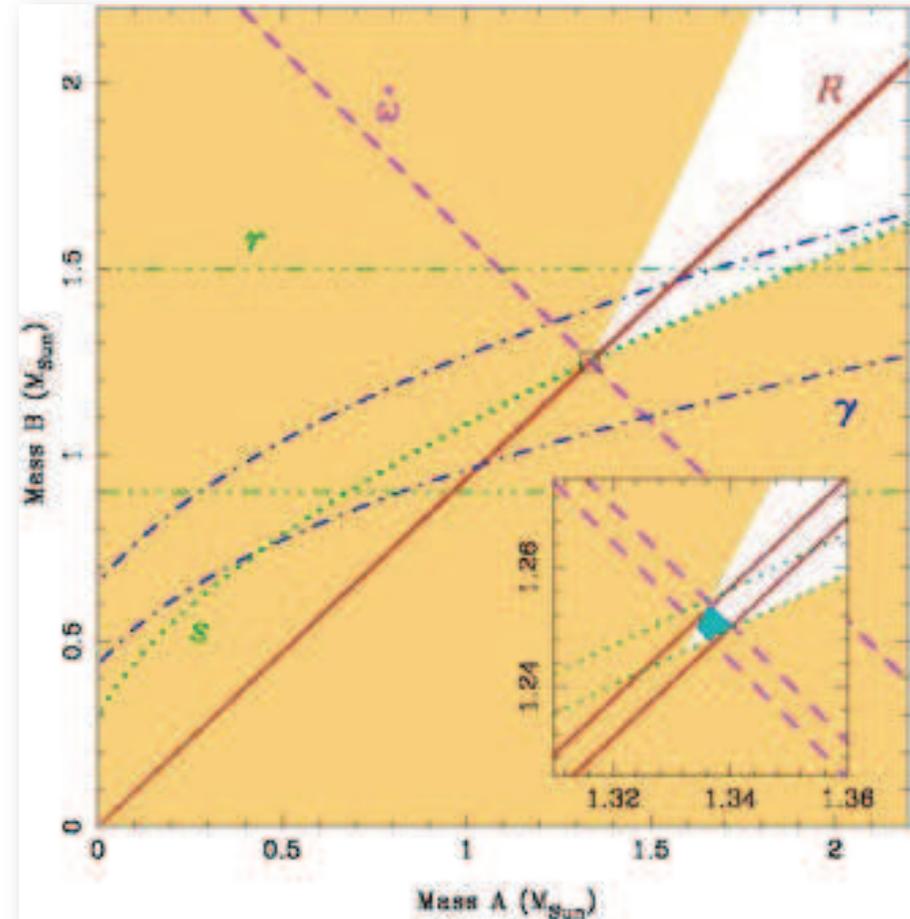
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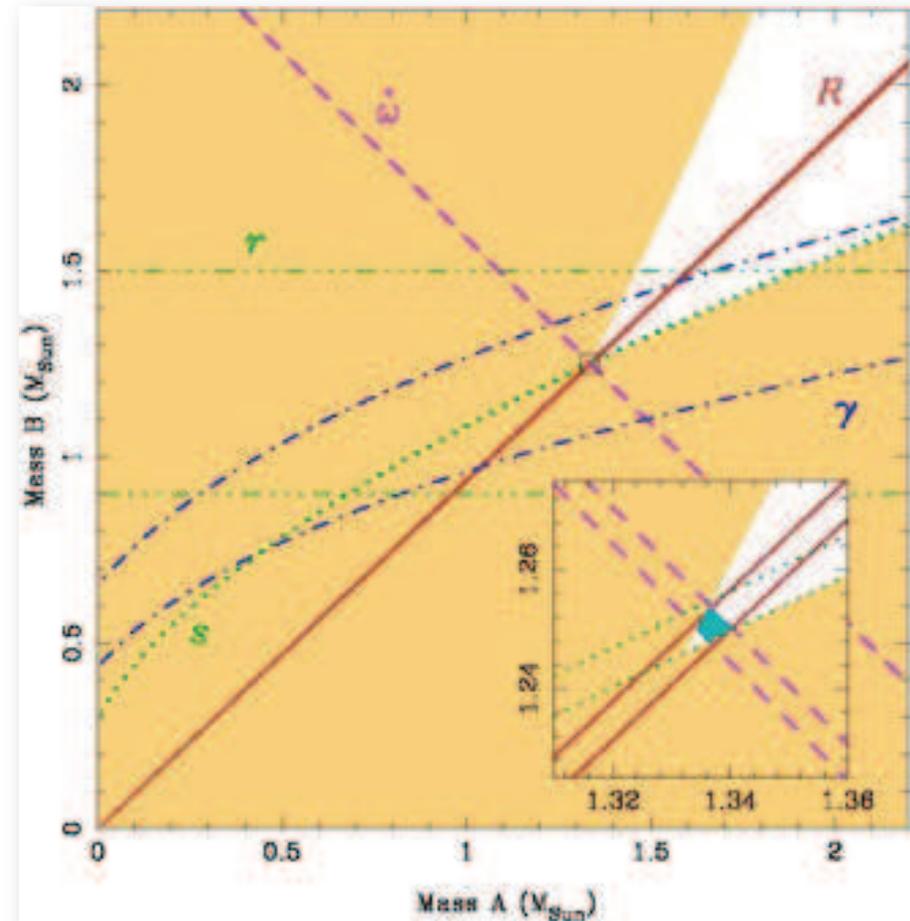
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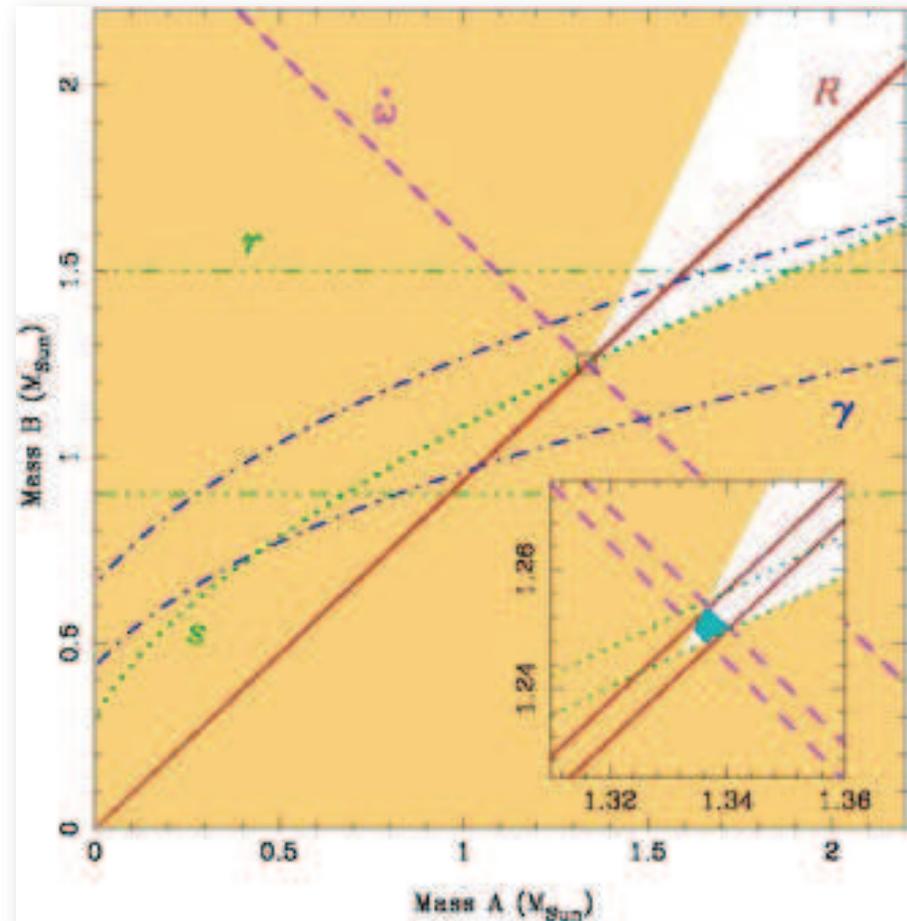
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 - Greatest periastron advance: $d\omega/dt$: 16.8 degrees per year (almost entirely general relativistic effect), compared to relativistic part of Mercury's perihelion advance of 42 sec per century
 - Orbit is shrinking by a few millimeters each year due to gravitational radiation reaction



Structure of the waveform

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- ✿• Radiation is emitted not just at twice the orbital frequency but at all other harmonics too

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$$h(t) = \frac{2M\eta}{D_L} \sum_{k=1}^7 \sum_{n=0}^5 A_{(k,n/2)} \cos [k\Psi(t) + \phi_{(k,n/2)}] x^{\frac{n}{2}+1}(t)$$

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- ✂ These amplitude corrections have a lot of additional structure
 - ✂ Increased mass reach of detectors
 - ✂ Greatly improved parameter estimation accuracies

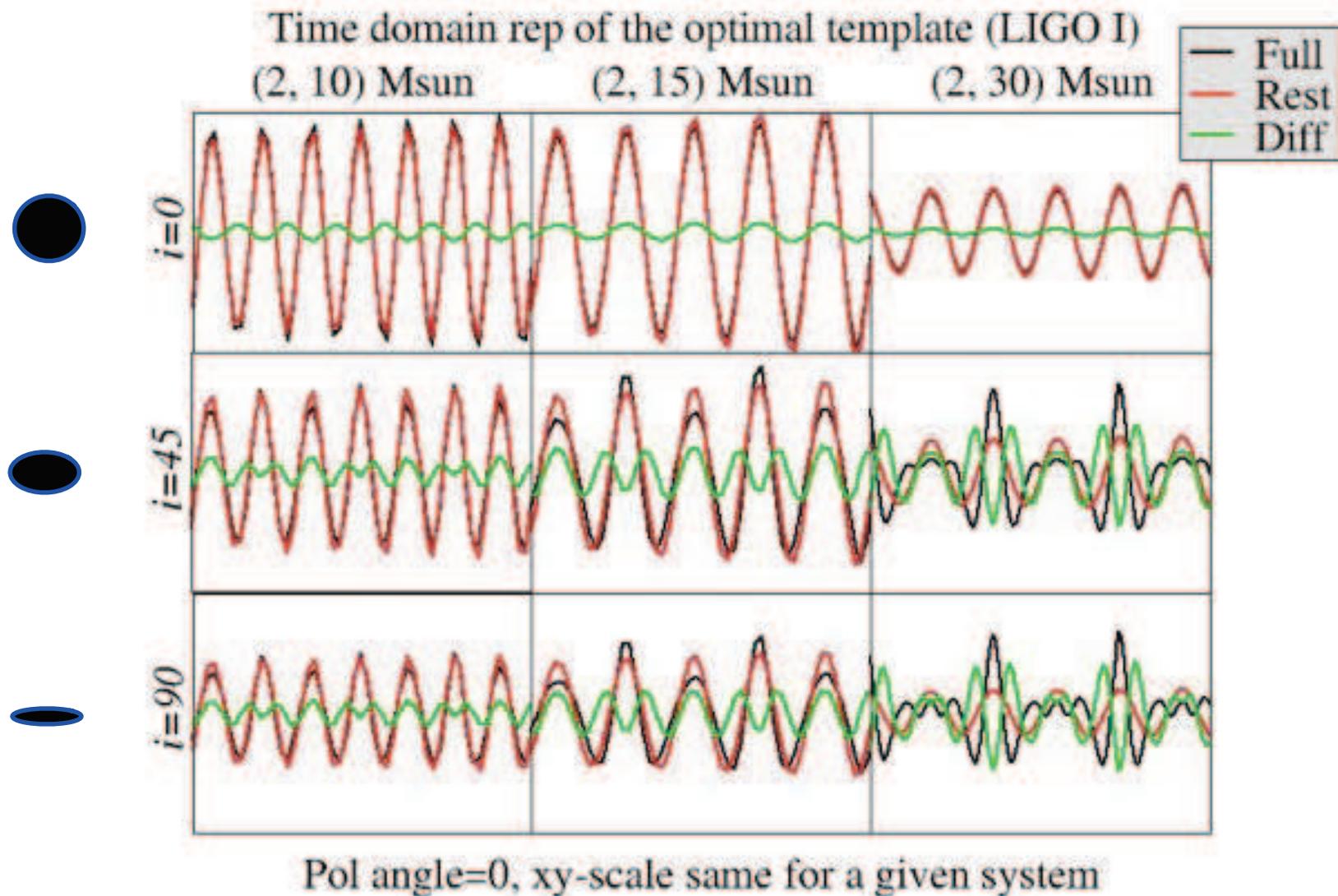
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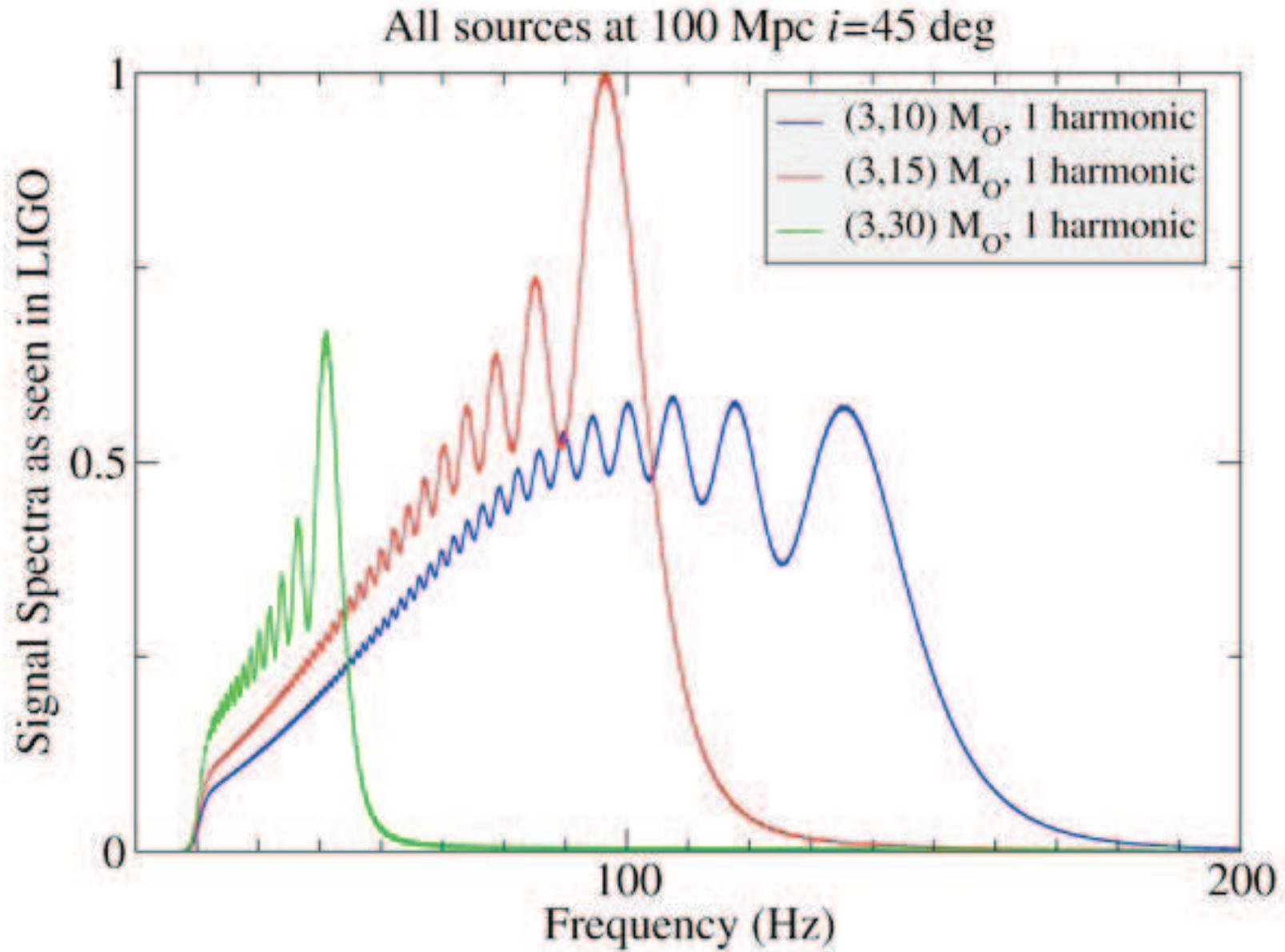
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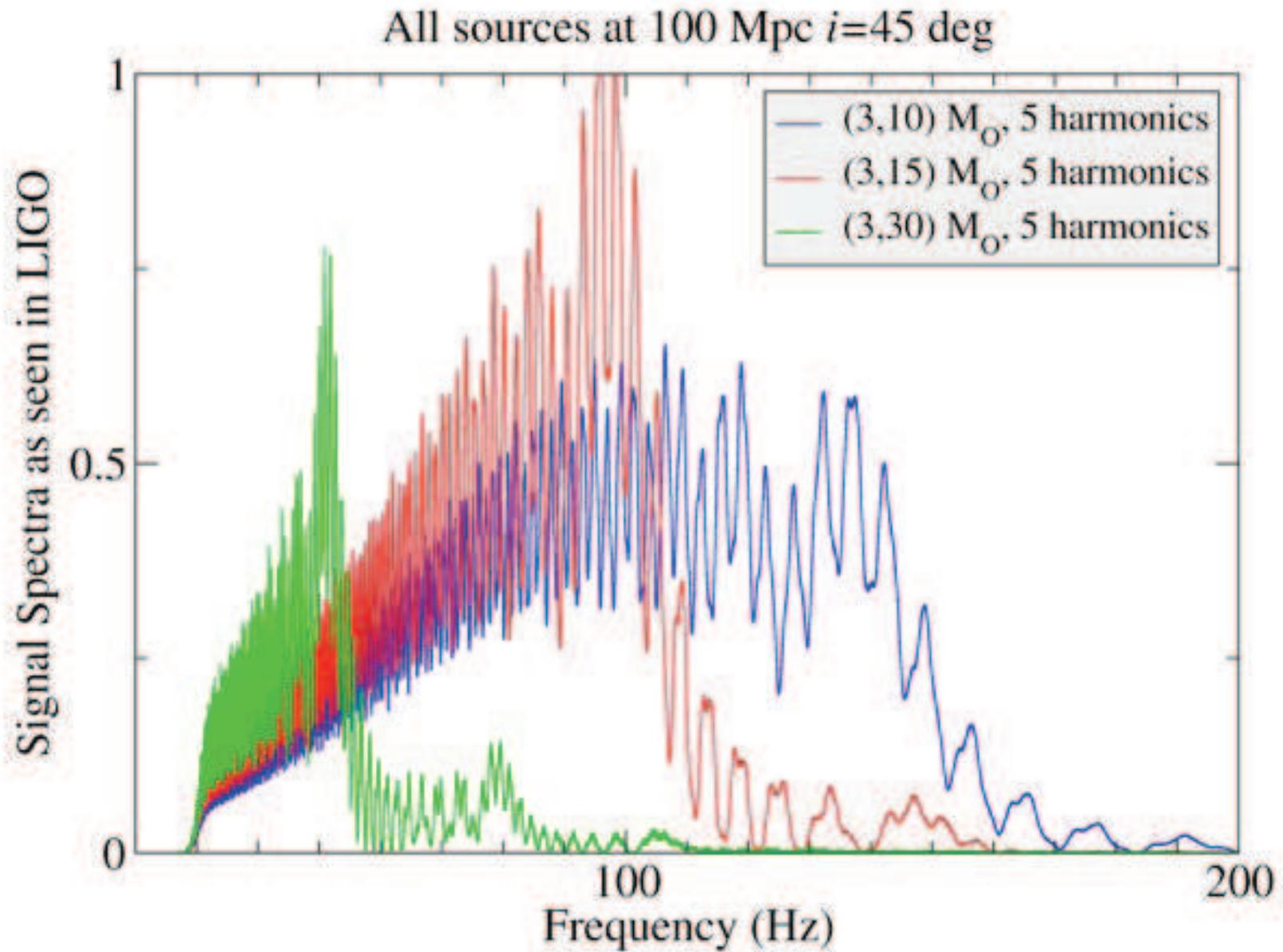
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- ✂ Blanchet, Damour, Iyer, Jaranowski, Schaefer, Will, Wiseman
- ✂ Andrade, Arun, Buonanno, Gopakumar, Joguet, Esposito-Farase, Faye, Kidder, Nissanke, Ohashi, Owen, Ponsot, Qusailah, Tagoshi ...

Edge-on vs face-on binaries







Black Hole Mergers from Numerical Relativity

A Big Industry: Golm, Jena (Germany), Maryland, Princeton, Rochester, Baton Rouge, Georgia Tech, Caltech, Cornell (USA), Canada, Mexico, Spain, Cardiff

Black Hole Mergers from Numerical Relativity

- After several decades NR is now able to compute accurate waveforms for use in extracting signals and science

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Black Hole Mergers from Numerical Relativity

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- New physics - e.g. super-kick velocities
- Analytical understanding of merger dynamics
- We should be able to see further and more massive objects

A Big Industry: Golm, Jena (Germany), Maryland, Princeton, Rochester, Baton Rouge, Georgia Tech, Caltech, Cornell (USA), Canada, Mexico, Spain, Cardiff

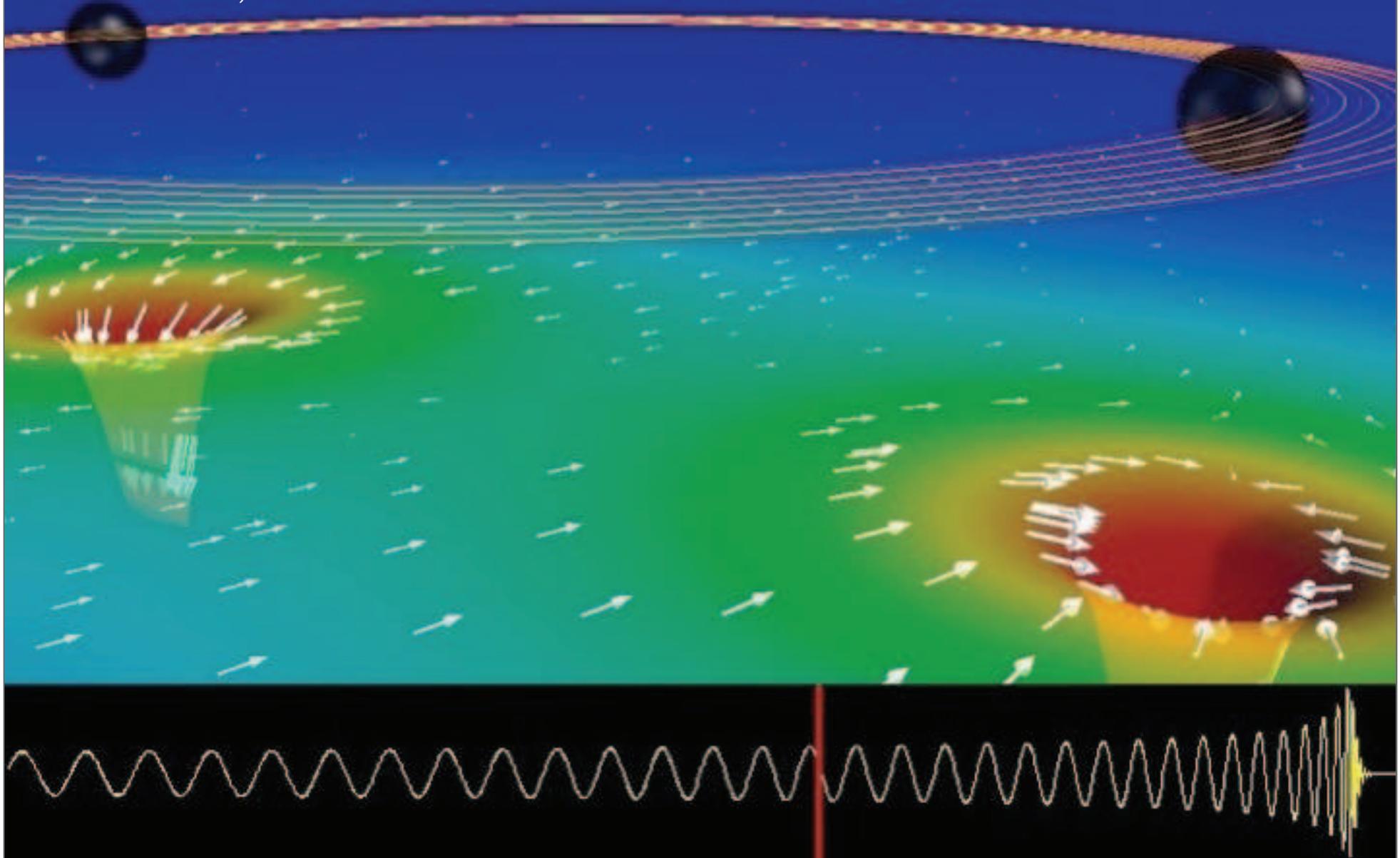
Top: 3D view of orbit of black holes

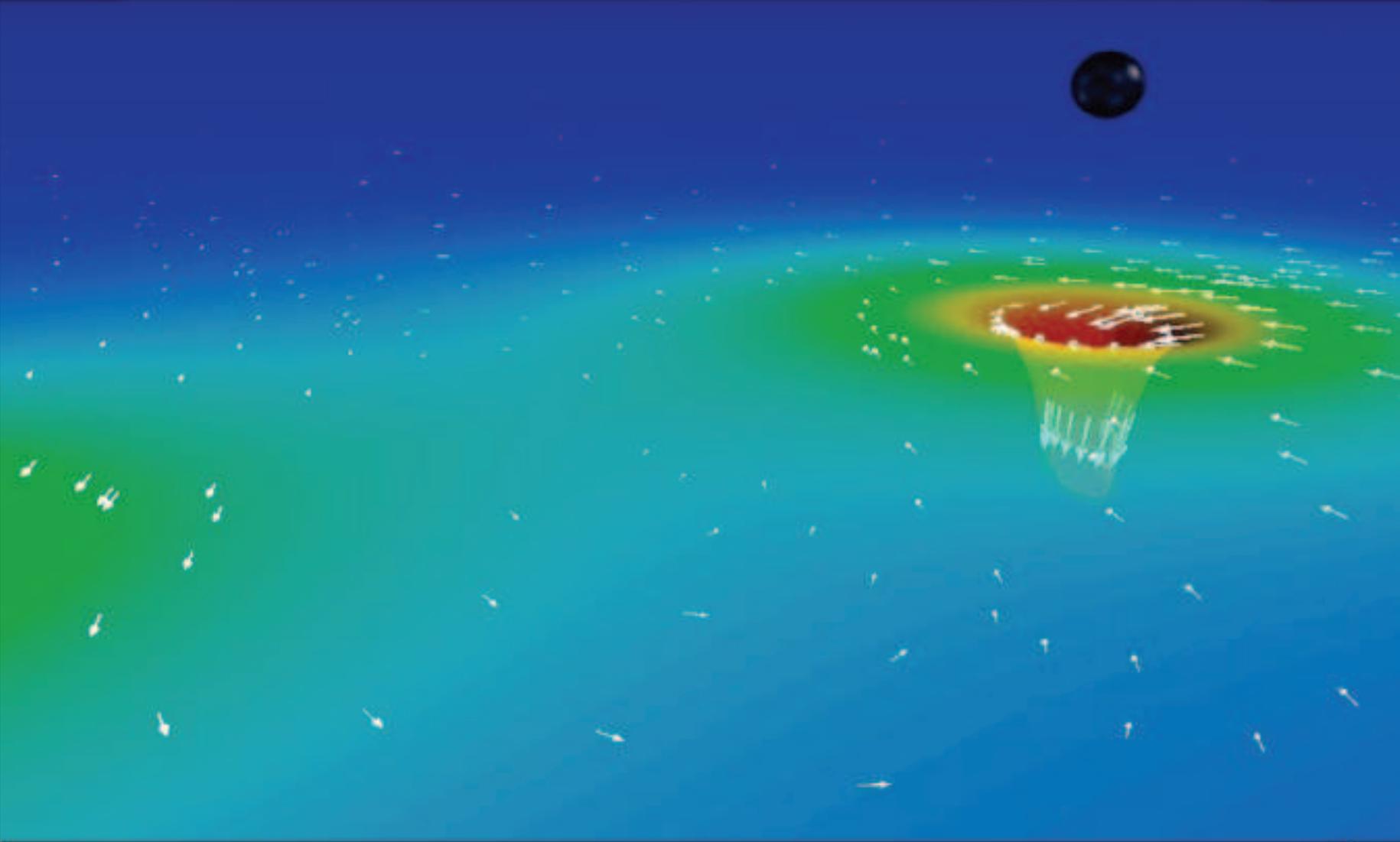
Middle: Depth - Curvature of Spacetime

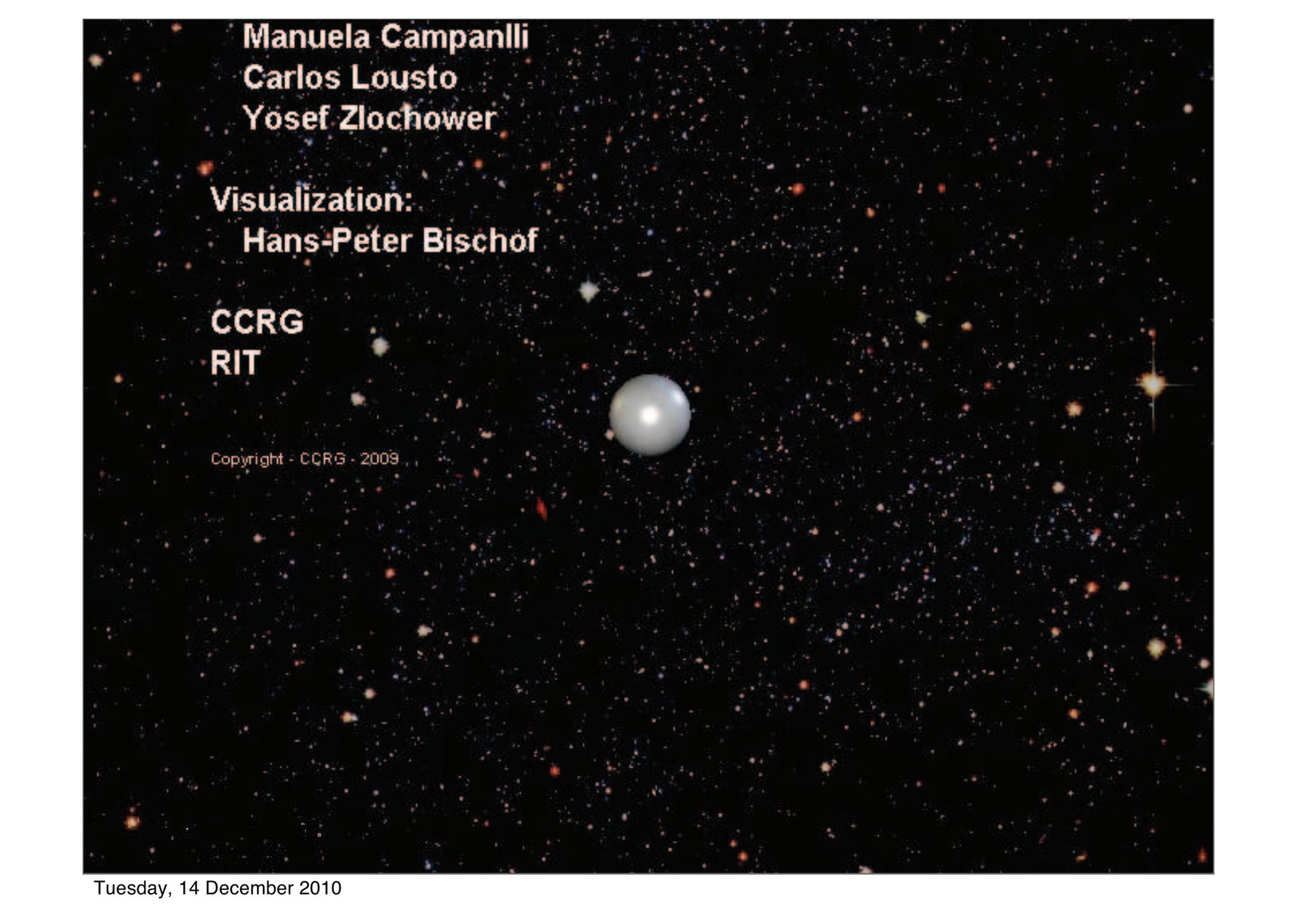
Colors: Rate of flow of time

Arrows: Velocity of flow of space

Bottom: Waveform; red line shows current time







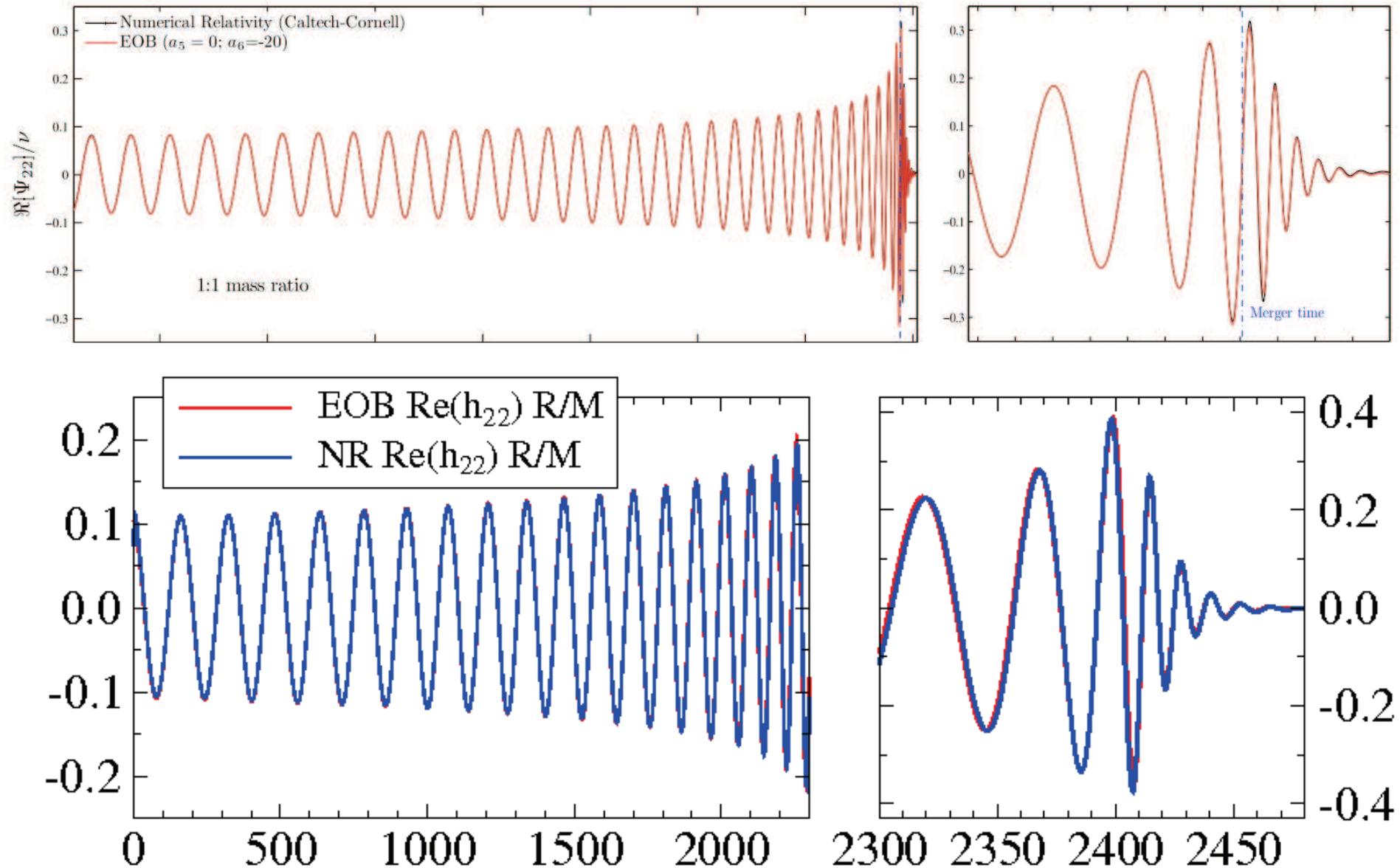
**Manuela Campanlli
Carlos Lousto
Yosef Zlochower**

**Visualization:
Hans-Peter Bischof**

**CCRG
RIT**

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Effective-One-Body Formalism for Inspiral-Merger-Ringdown Dynamics

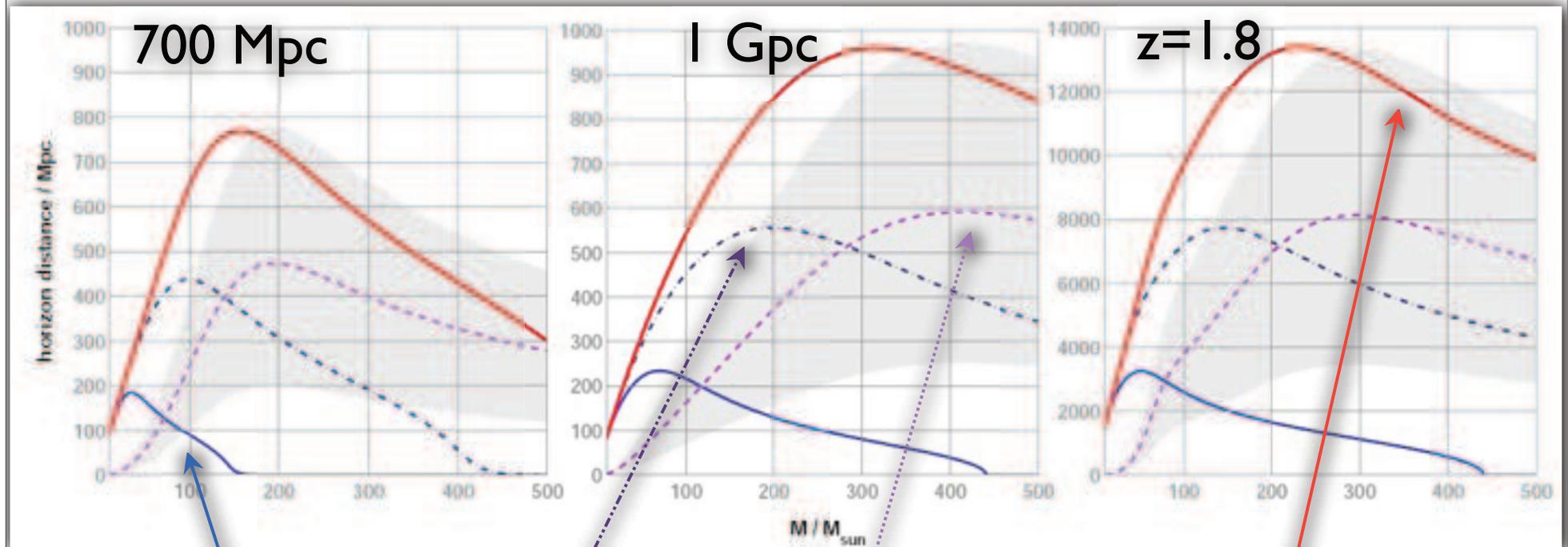


How further can we see with Inspiral, Merger and Ringdown?

Initial LIGO

Virgo design

Advanced LIGO



PN templates

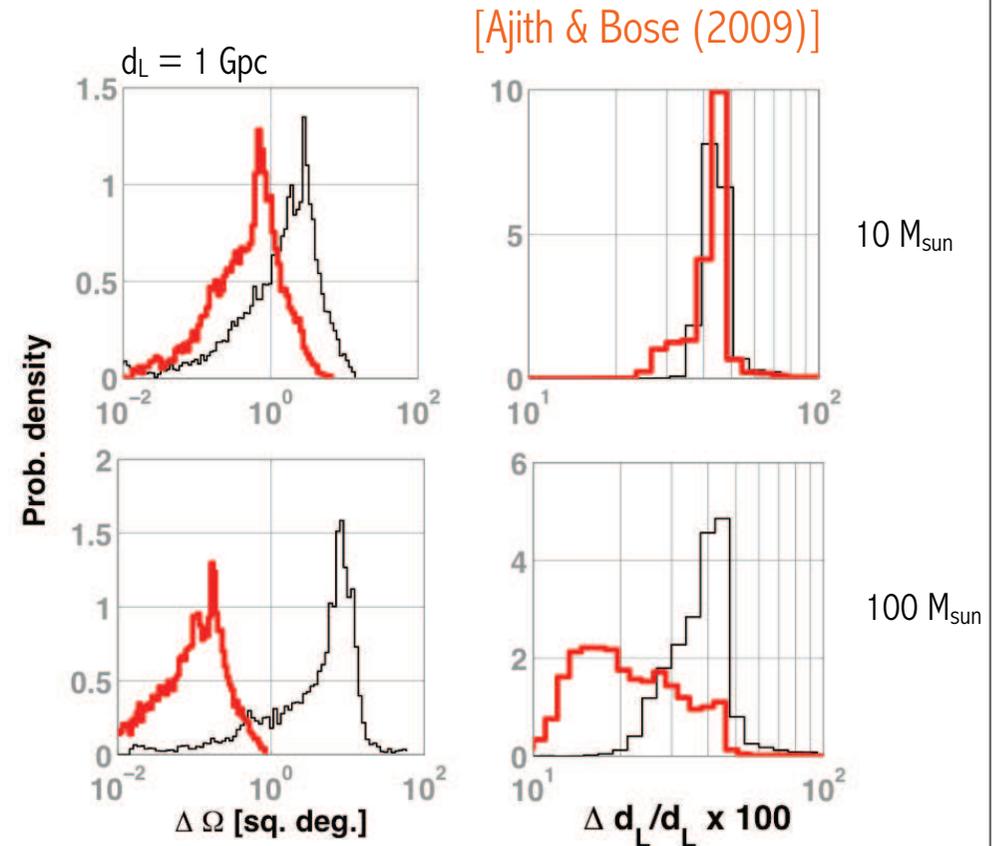
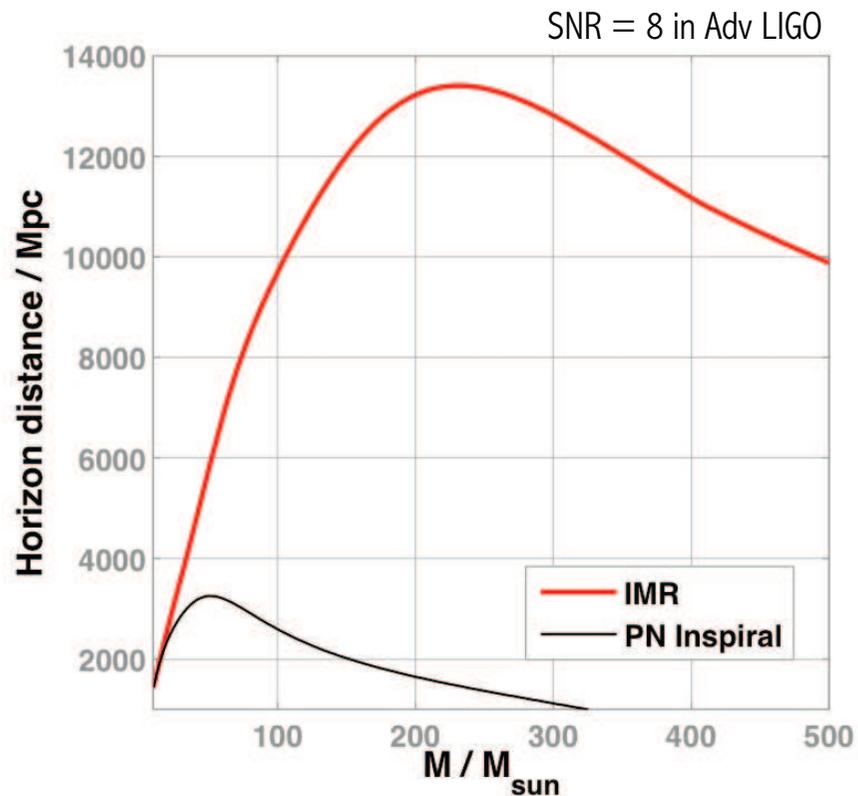
EOB w/o ring-down

Ring-down

IMR/EOBNR

Ajith et al

Comparison of Inspiral and **Inspiral-Merger-Ringdown** waveforms: Distance Reach (left) Parameter Estimation (right)



Astrophysics

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• Unveiling progenitors of short-hard GRBs

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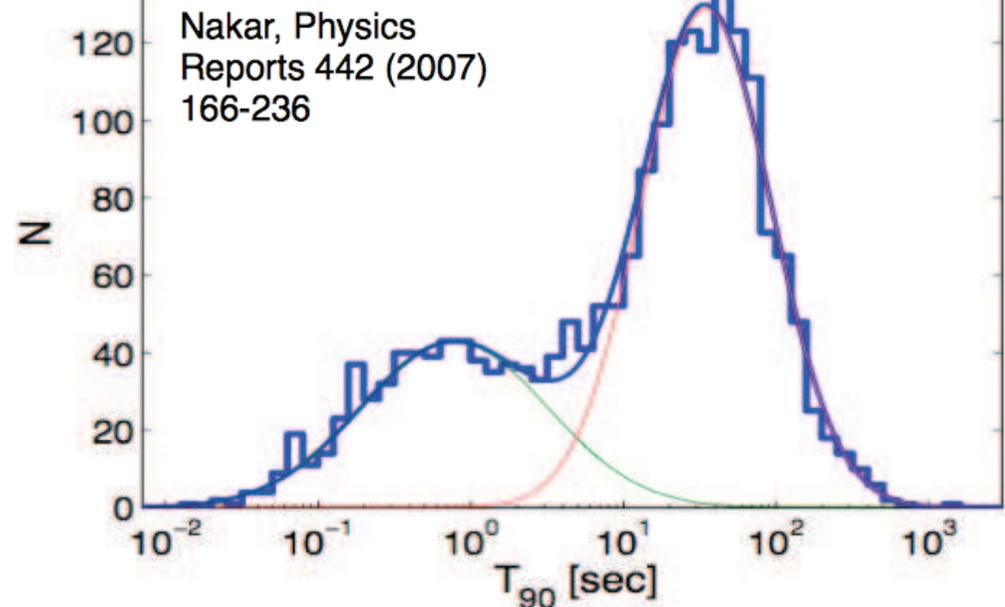
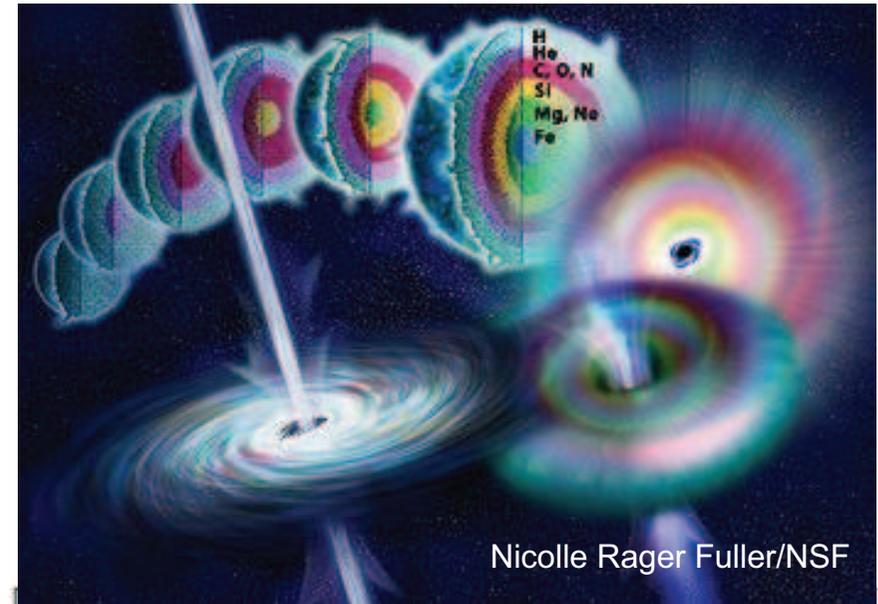
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- NS spin frequencies in LMXBs
 - Why are spin frequencies of neutron stars in low-mass X-ray binaries bounded, CFS instability and r-modes

Expected Annual Coalescence Rates

- Rates are mean of the distribution; in a 95% confidence interval, rates uncertain by 3 orders of magnitude
- Rates are for Binary Neutron Stars (**BNS**) Binary Black Boles (**BBH**) and Neutron Star-Black Hole binaries (**NS-BH**)

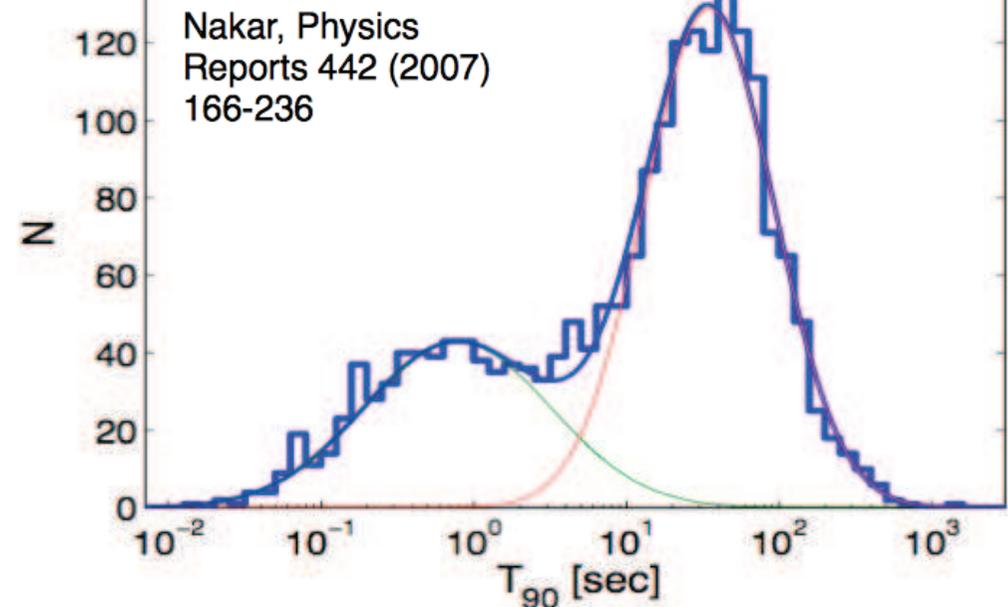
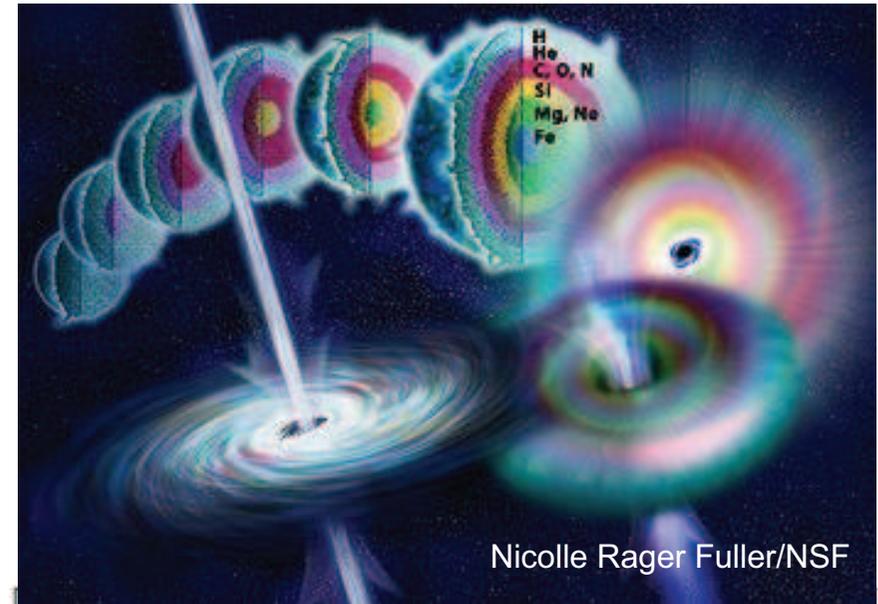
| | BNS | NS-BH | BBH |
|---------------------------|------------|--------------|------------|
| Initial LIGO (2002-06) | 0.02 | 0.006 | 0.01 |
| Adv. LIGO (2014+) | 40 | 10 | 20 |
| ET | Millions | 100,000 | Millions |

GRB Progenitors



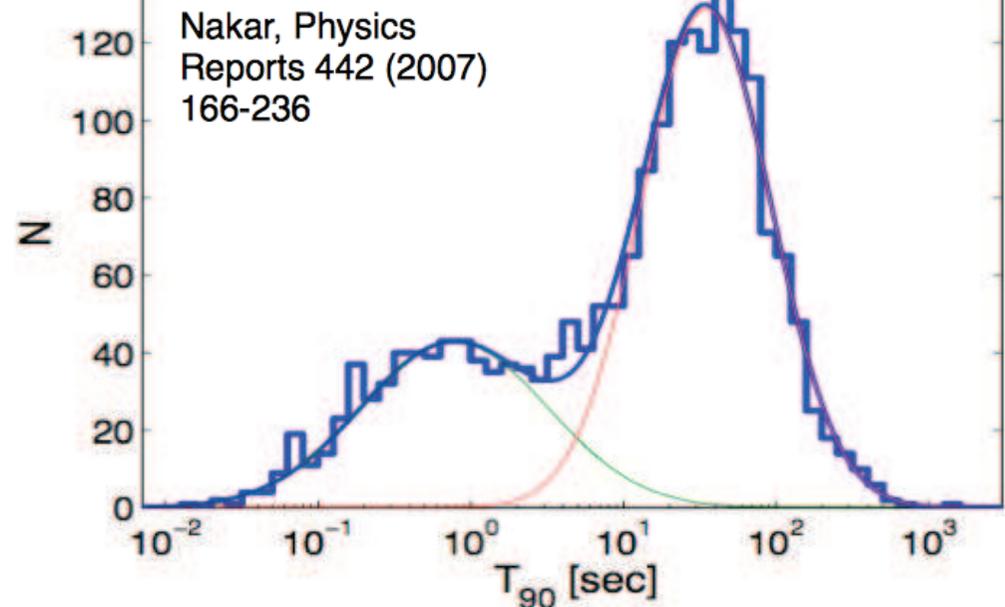
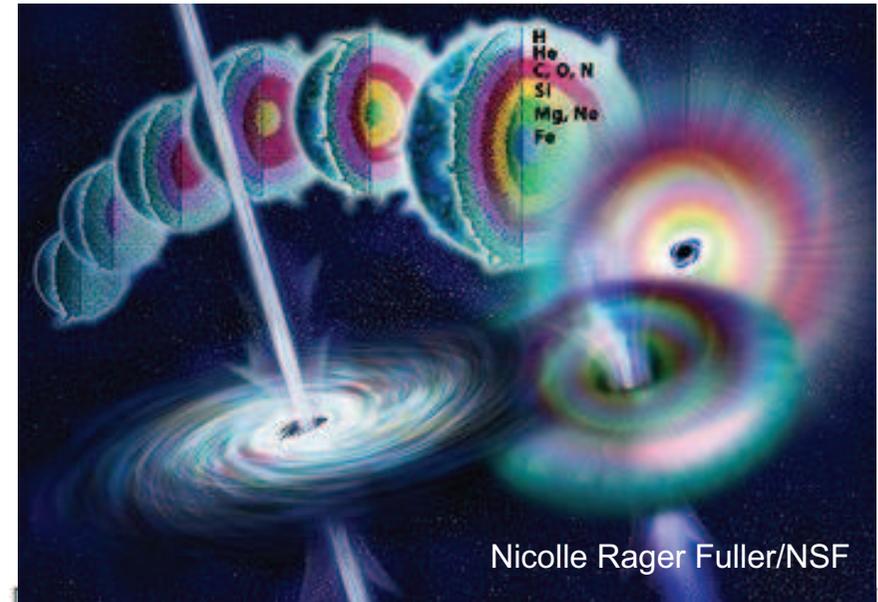
GRB Progenitors

- Intense flashes of gamma-rays:



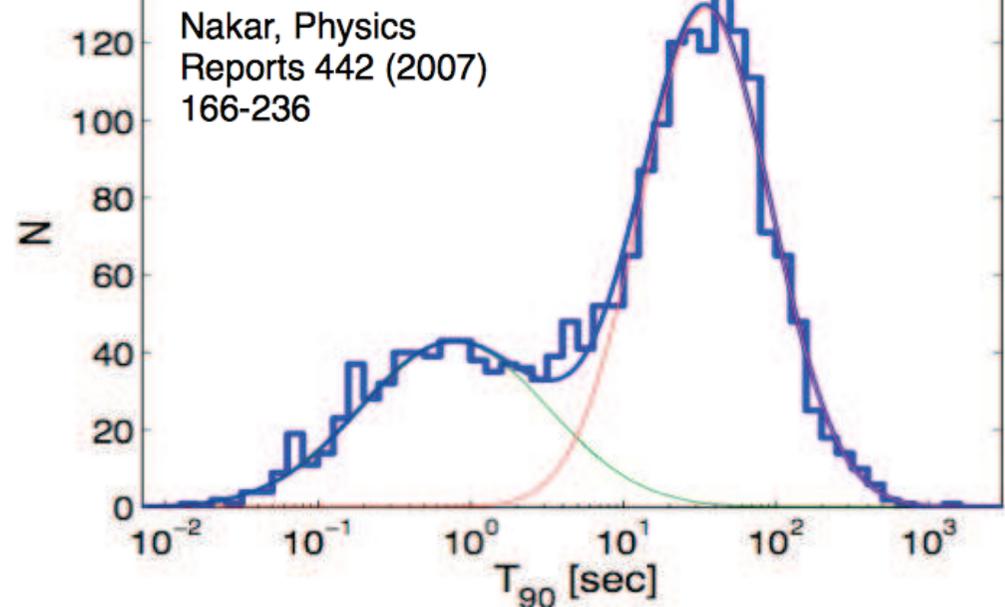
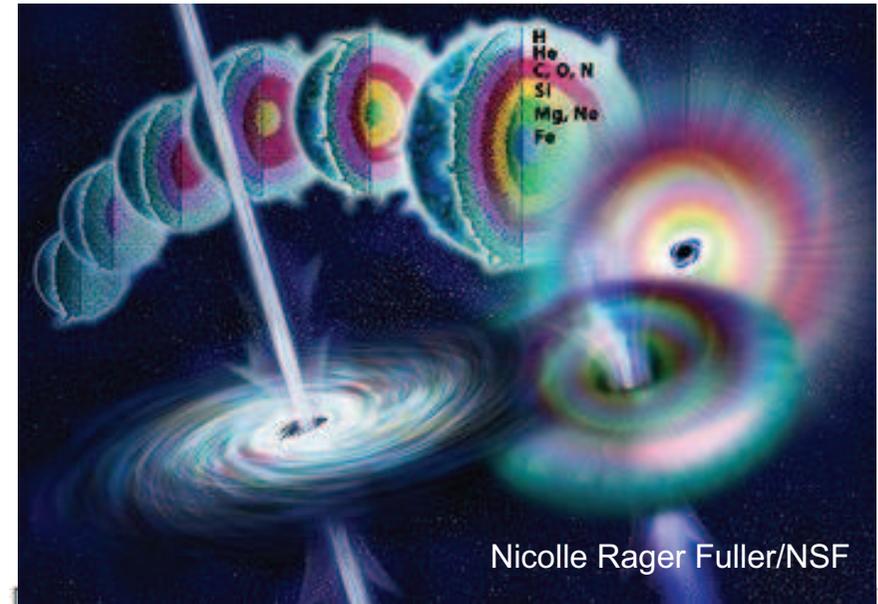
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- Intense flashes of gamma-rays:
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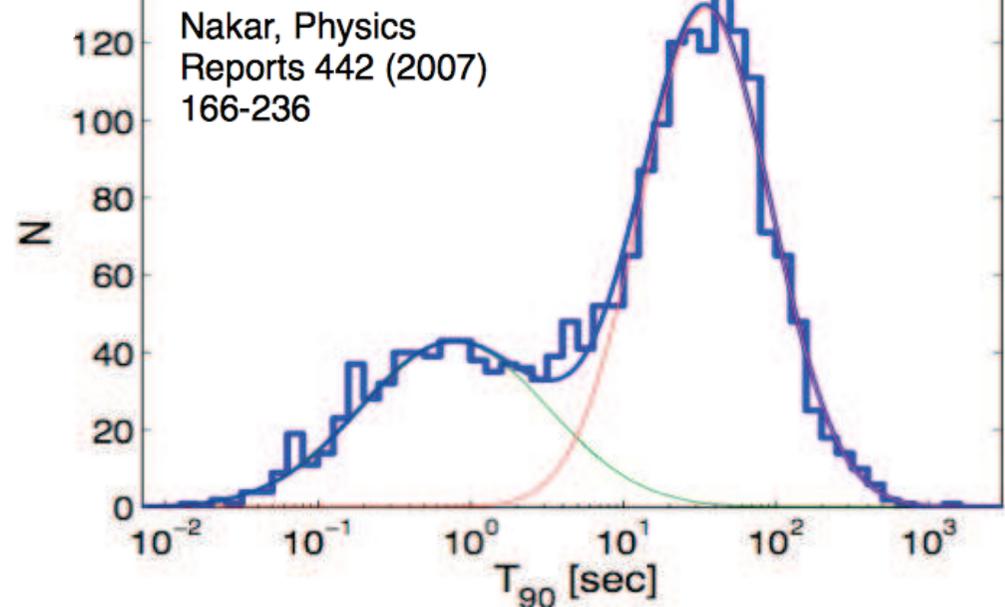
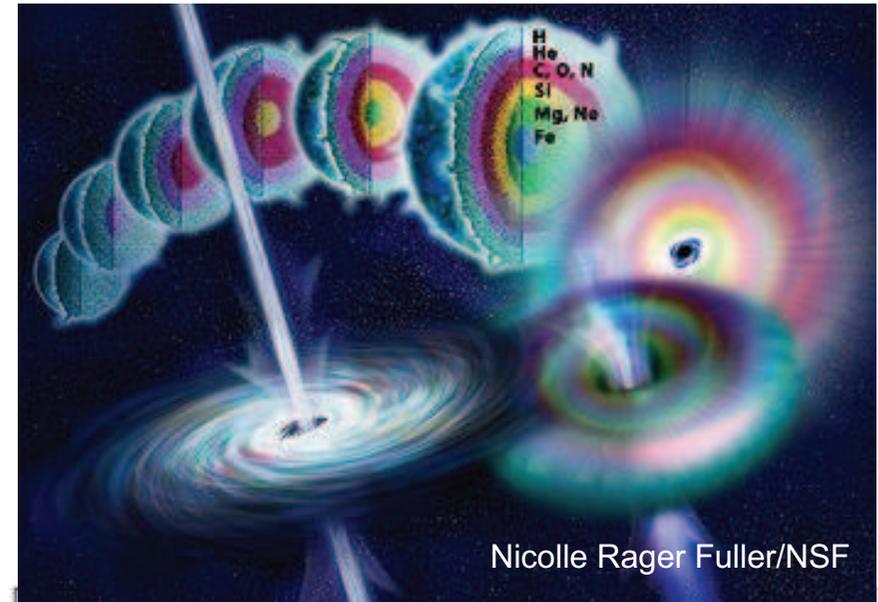
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- X-ray, UV and optical afterglows



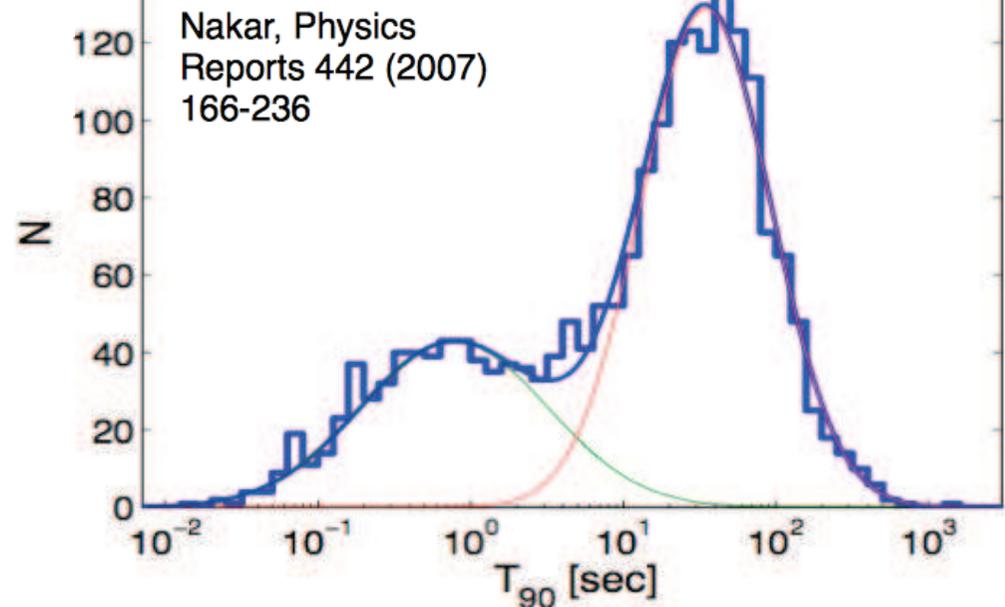
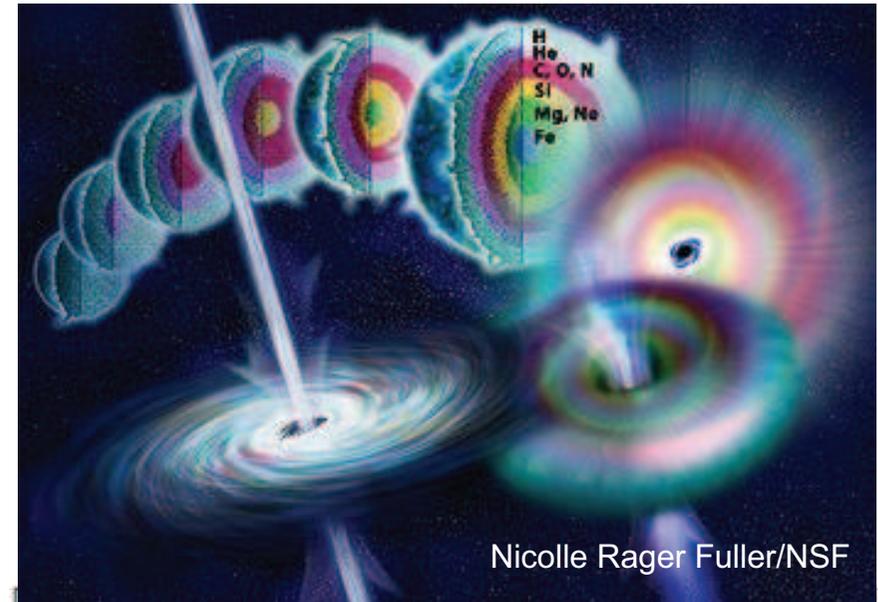
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- Most luminous EM source since the Big Bang
- X-ray, UV and optical afterglows
- Bimodal distribution of durations



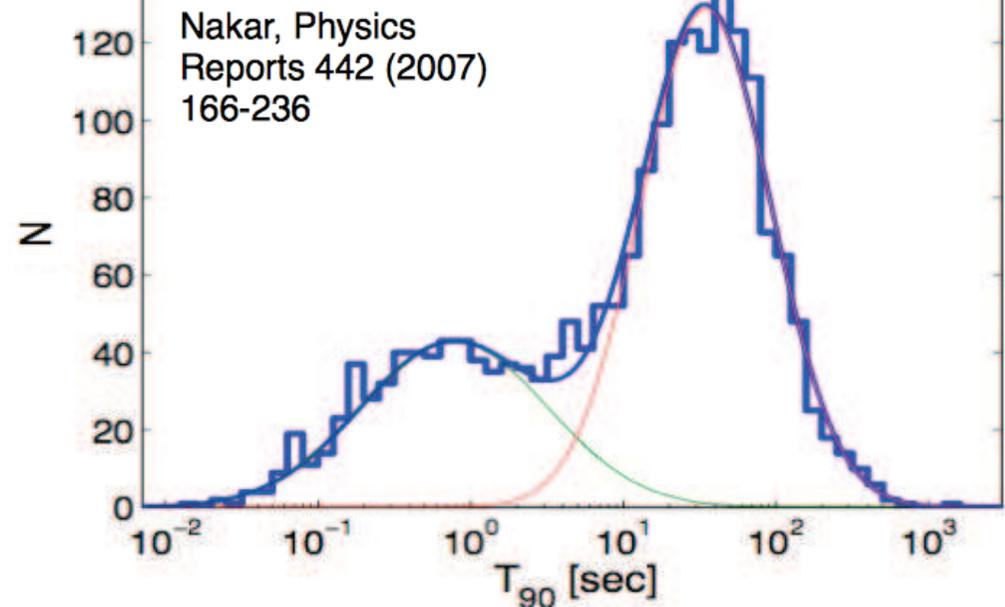
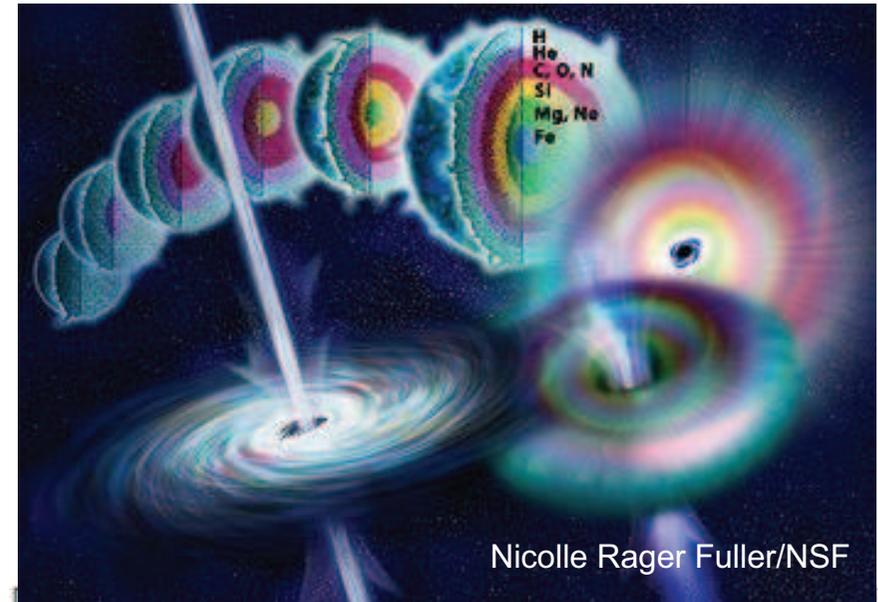
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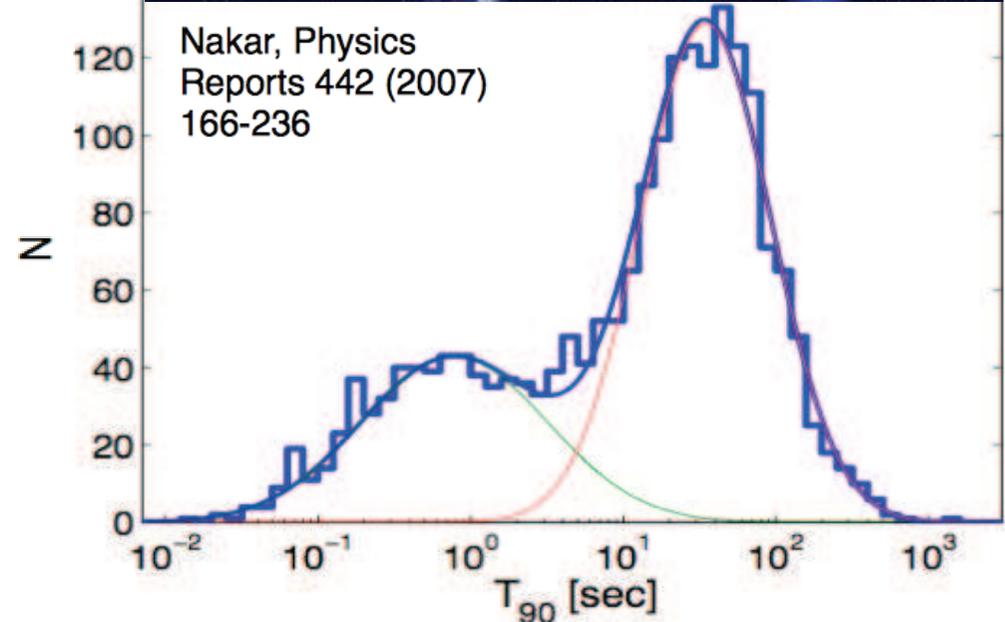
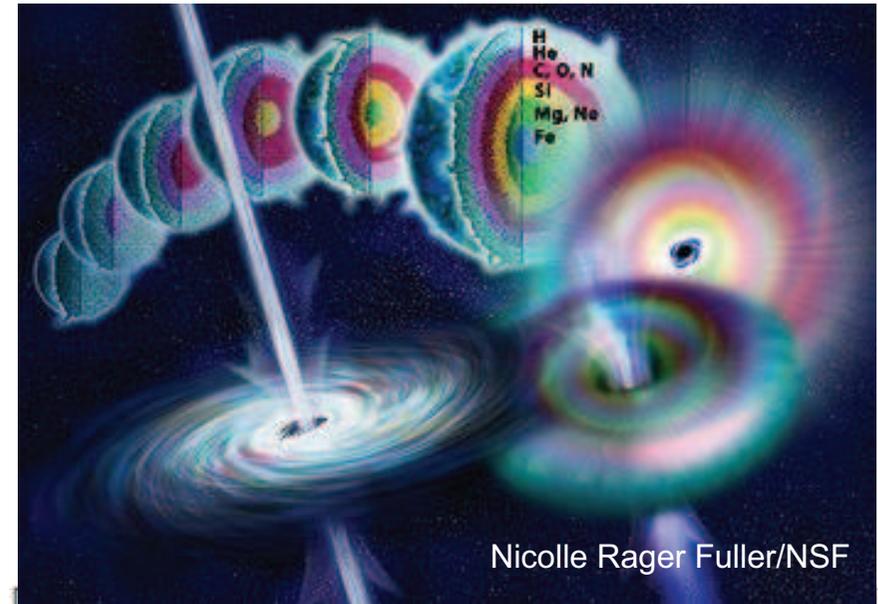
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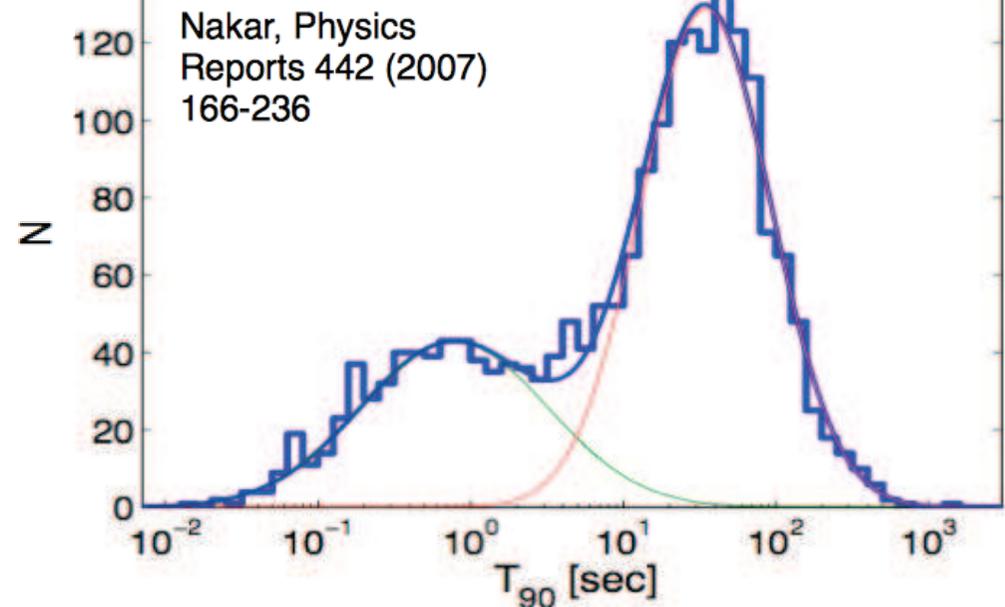
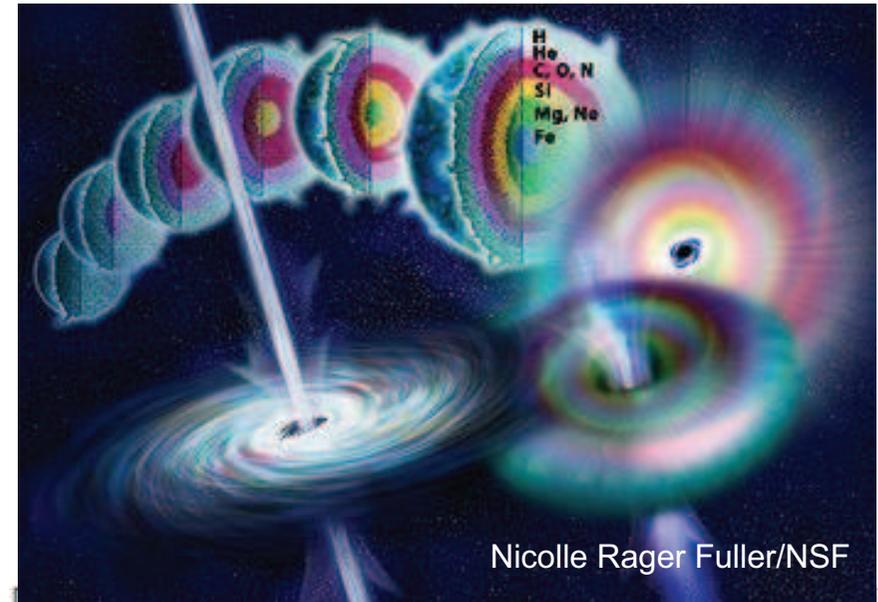
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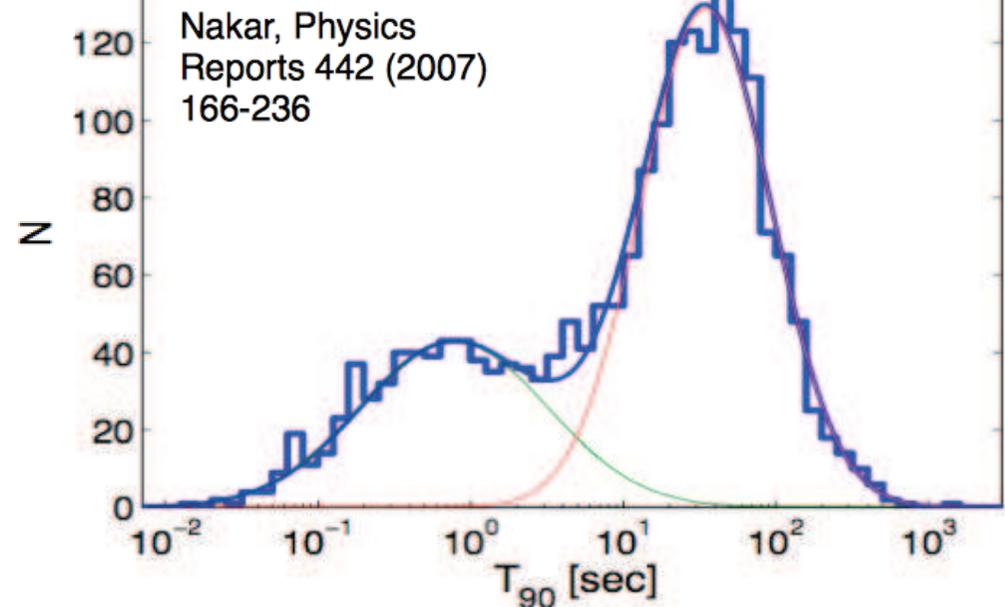
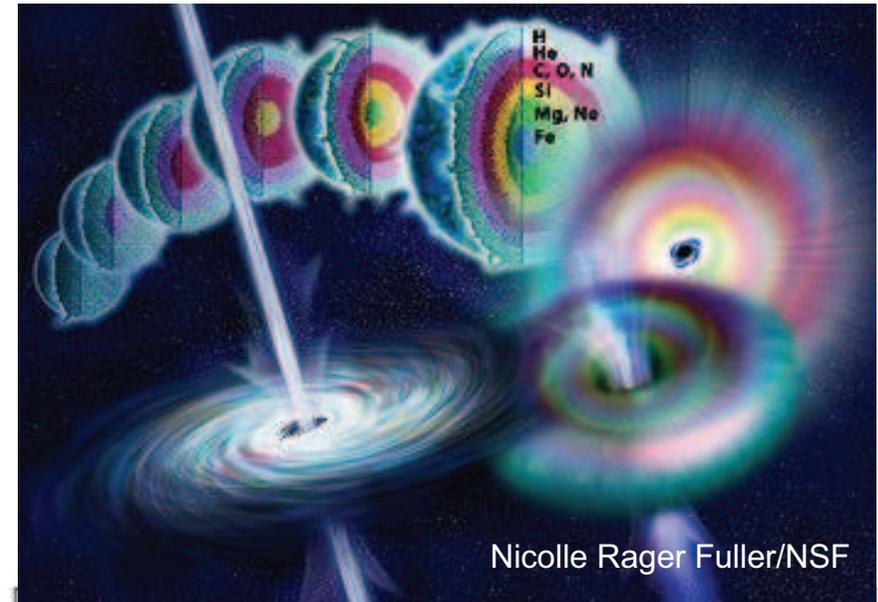
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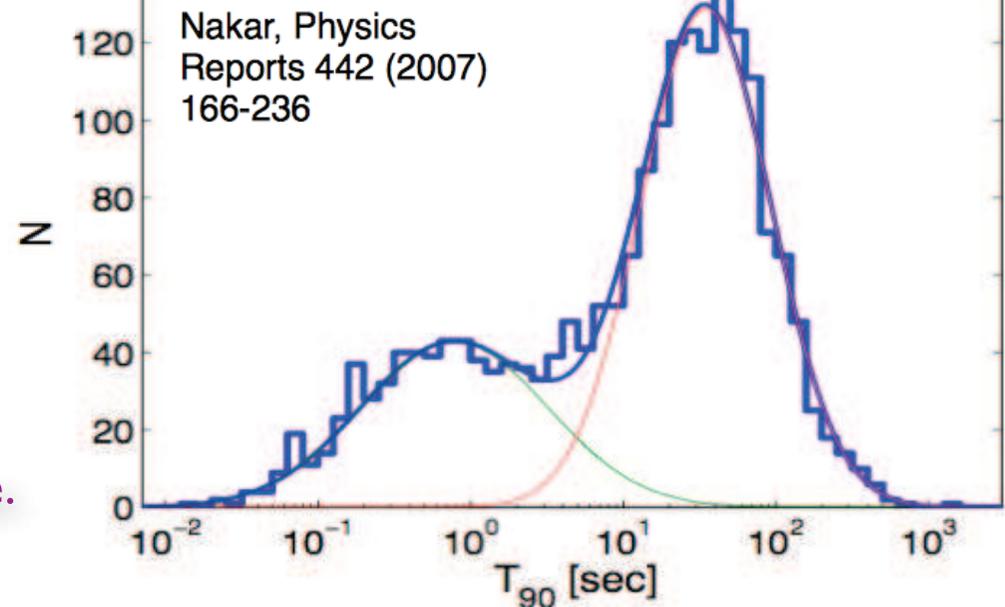
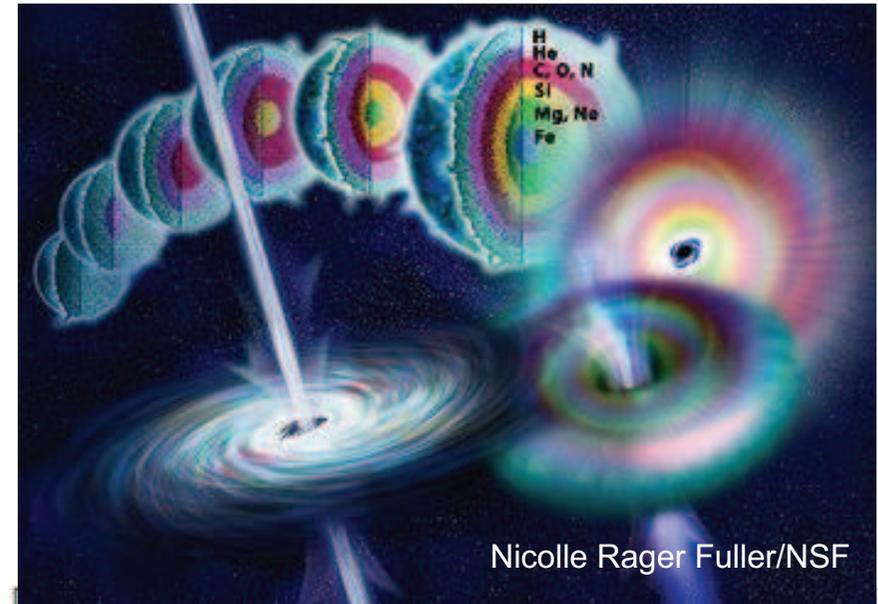
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GRB Progenitors

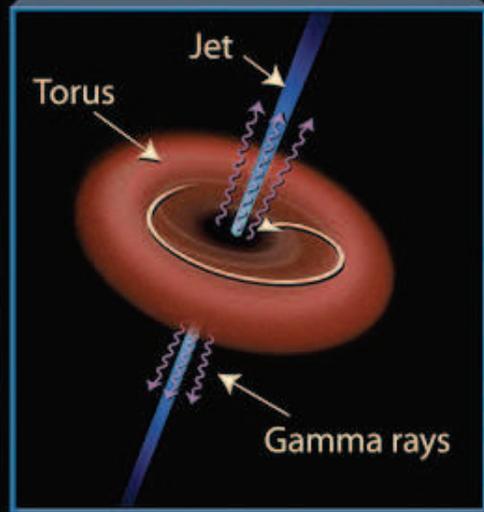
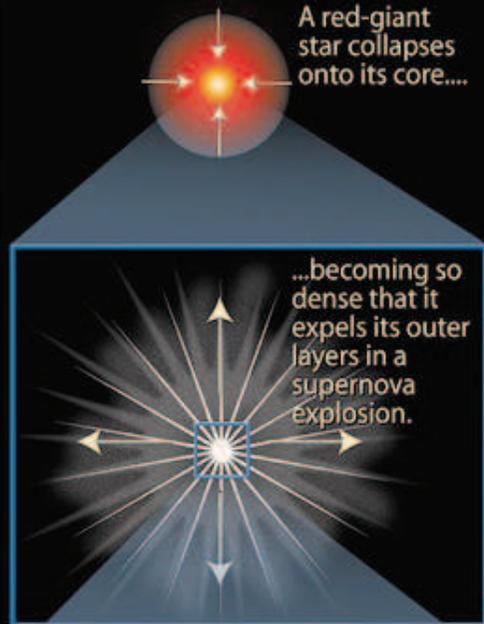
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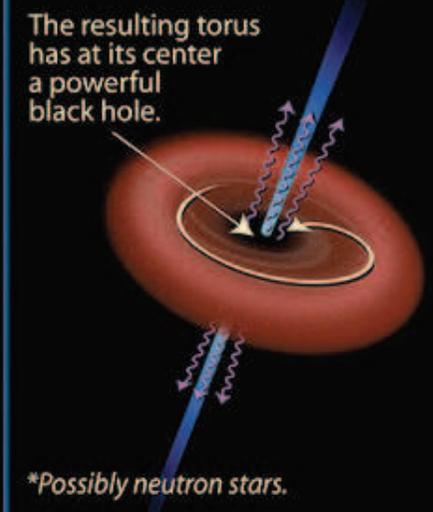
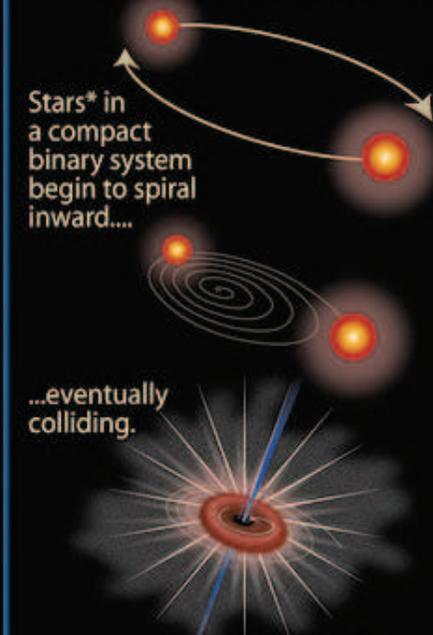
GRBs - The Long and Short of it

Gamma-Ray Bursts (GRBs): The Long and Short of It

Long gamma-ray burst (>2 seconds' duration)



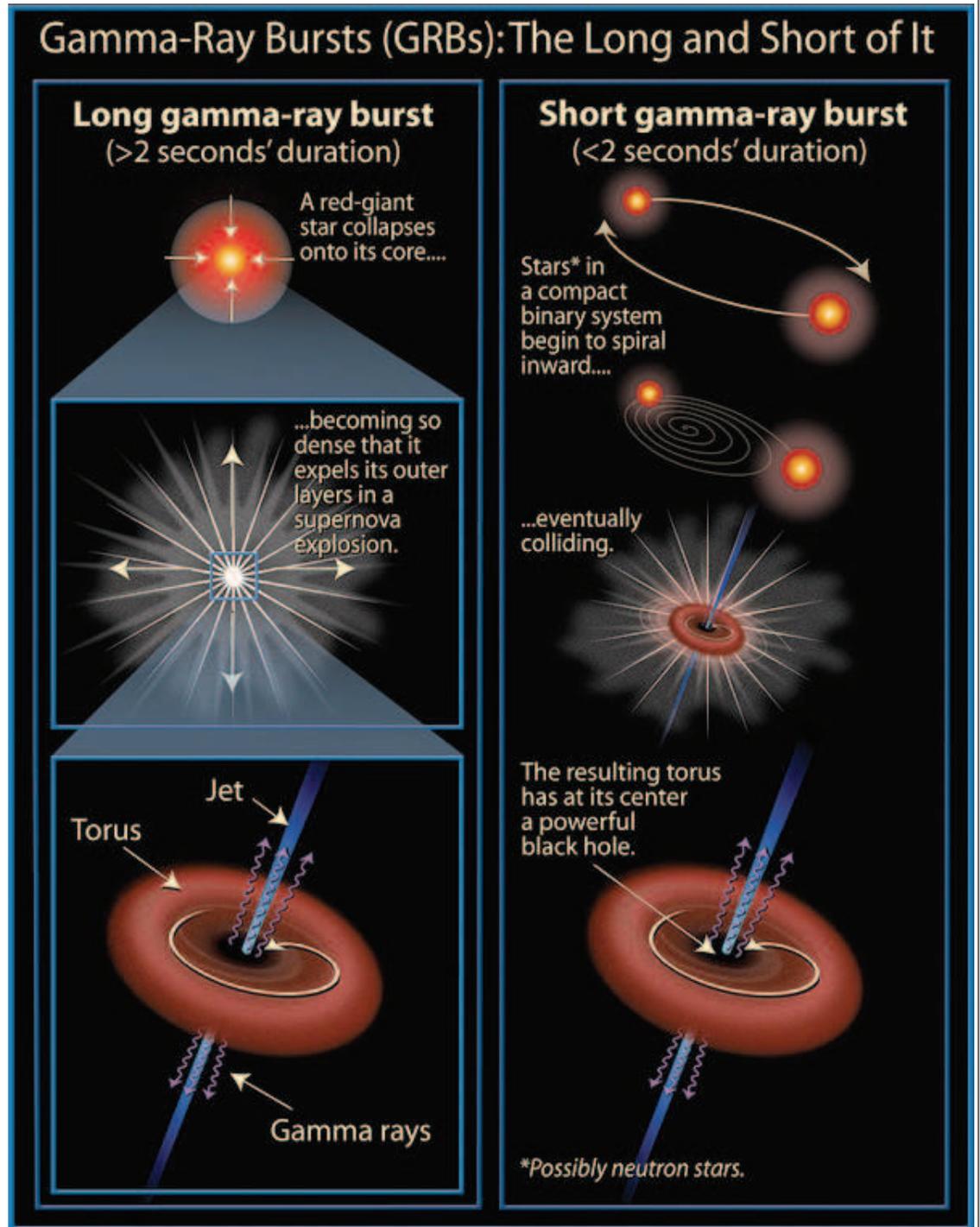
Short gamma-ray burst (<2 seconds' duration)



*Possibly neutron stars.

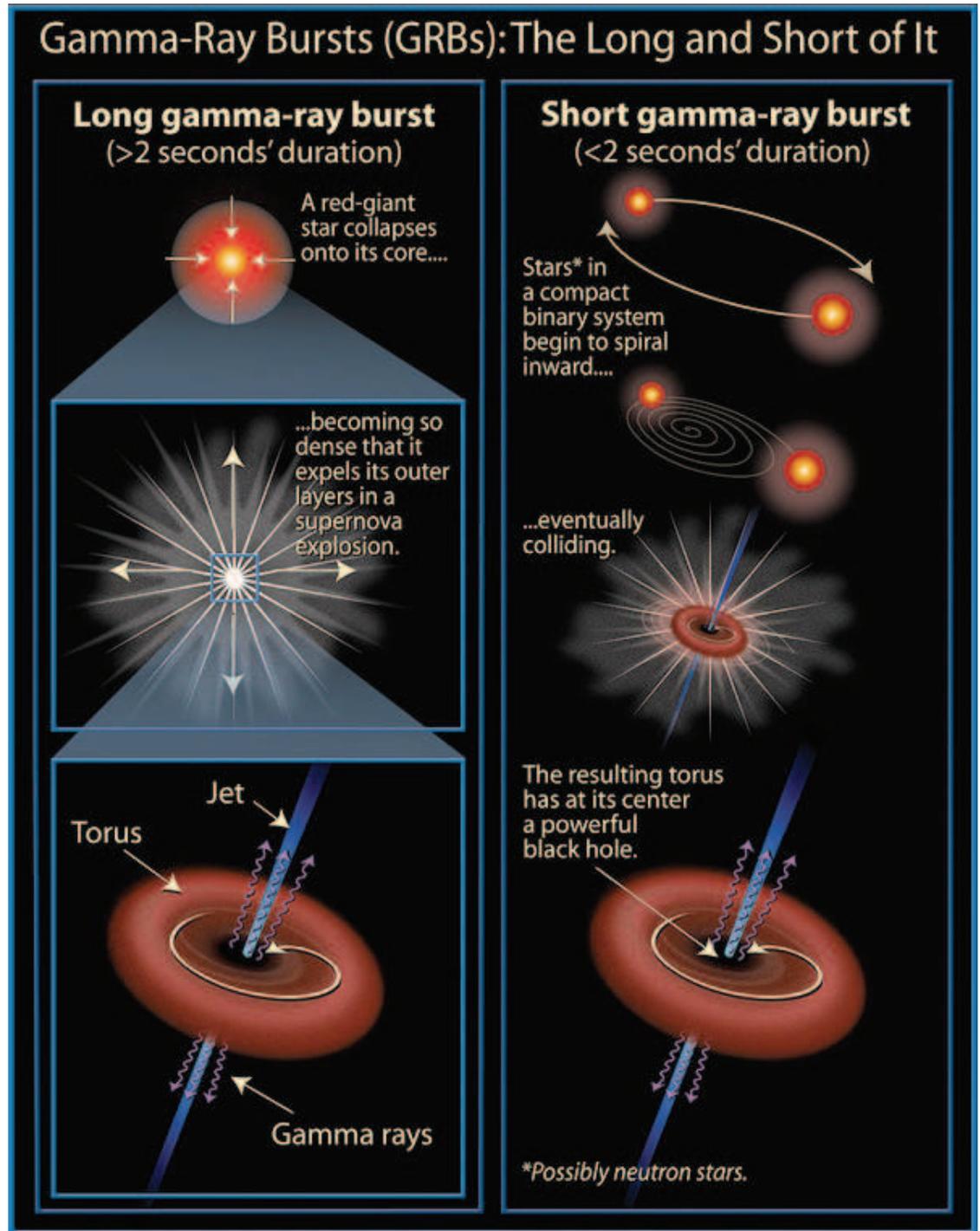
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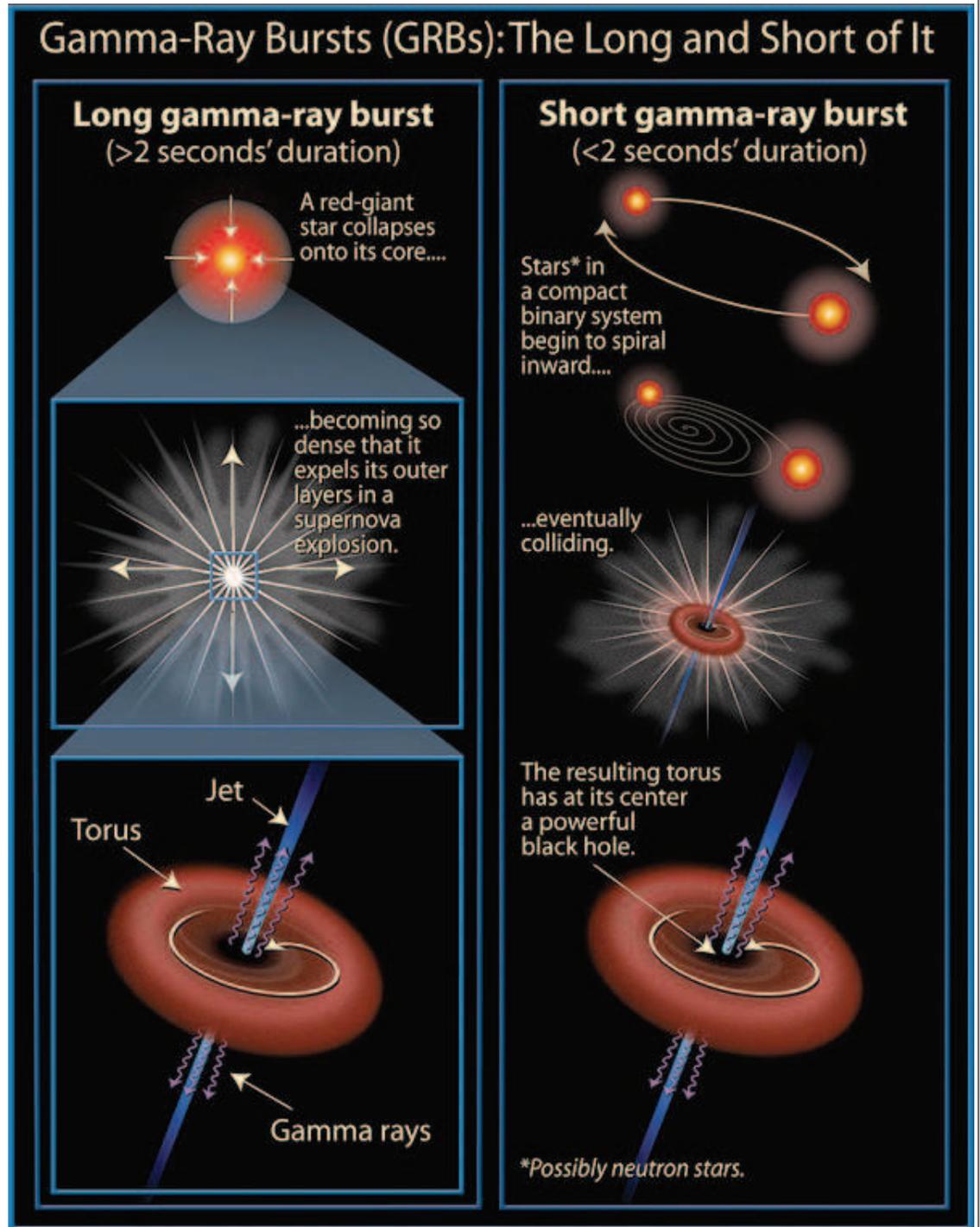
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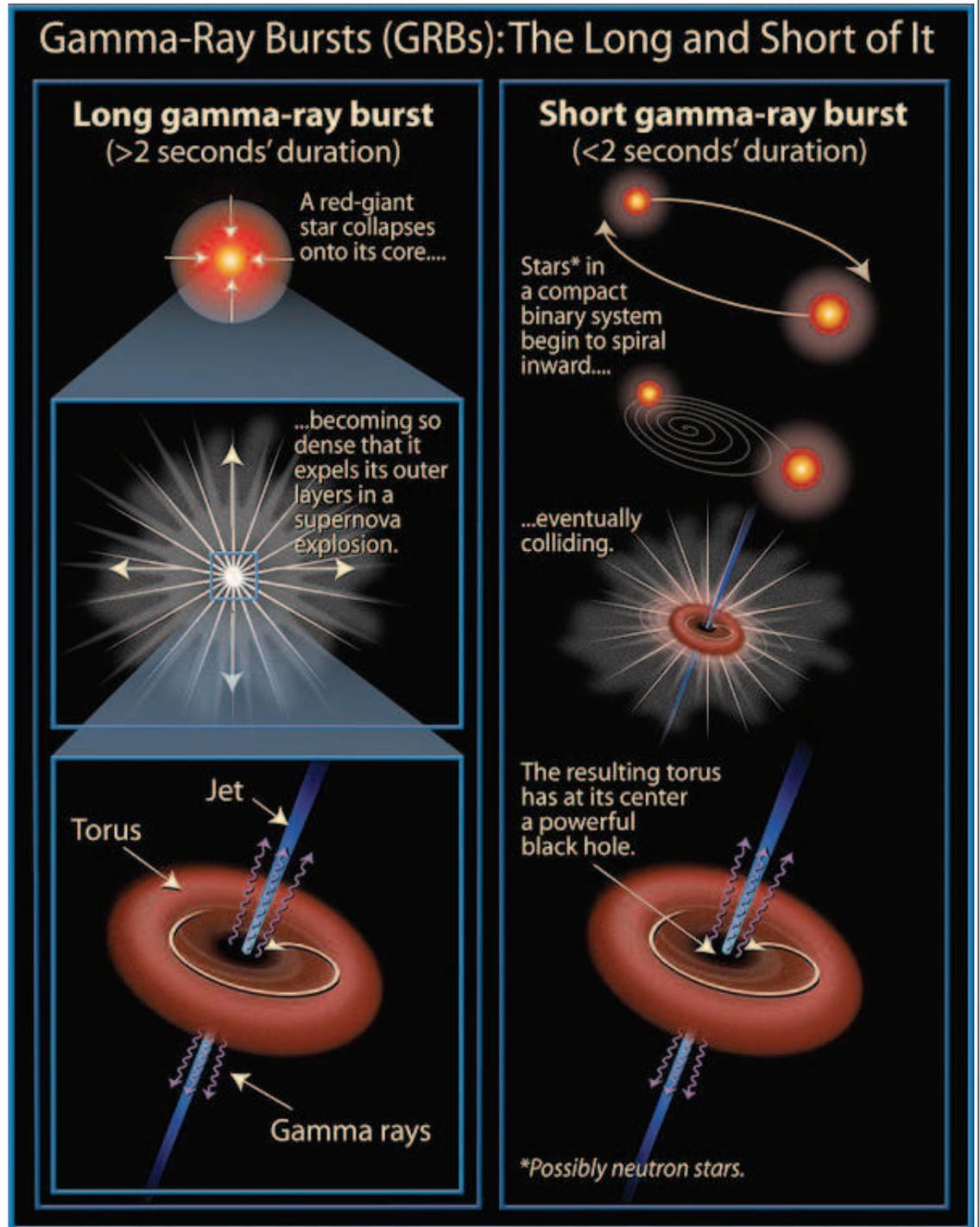
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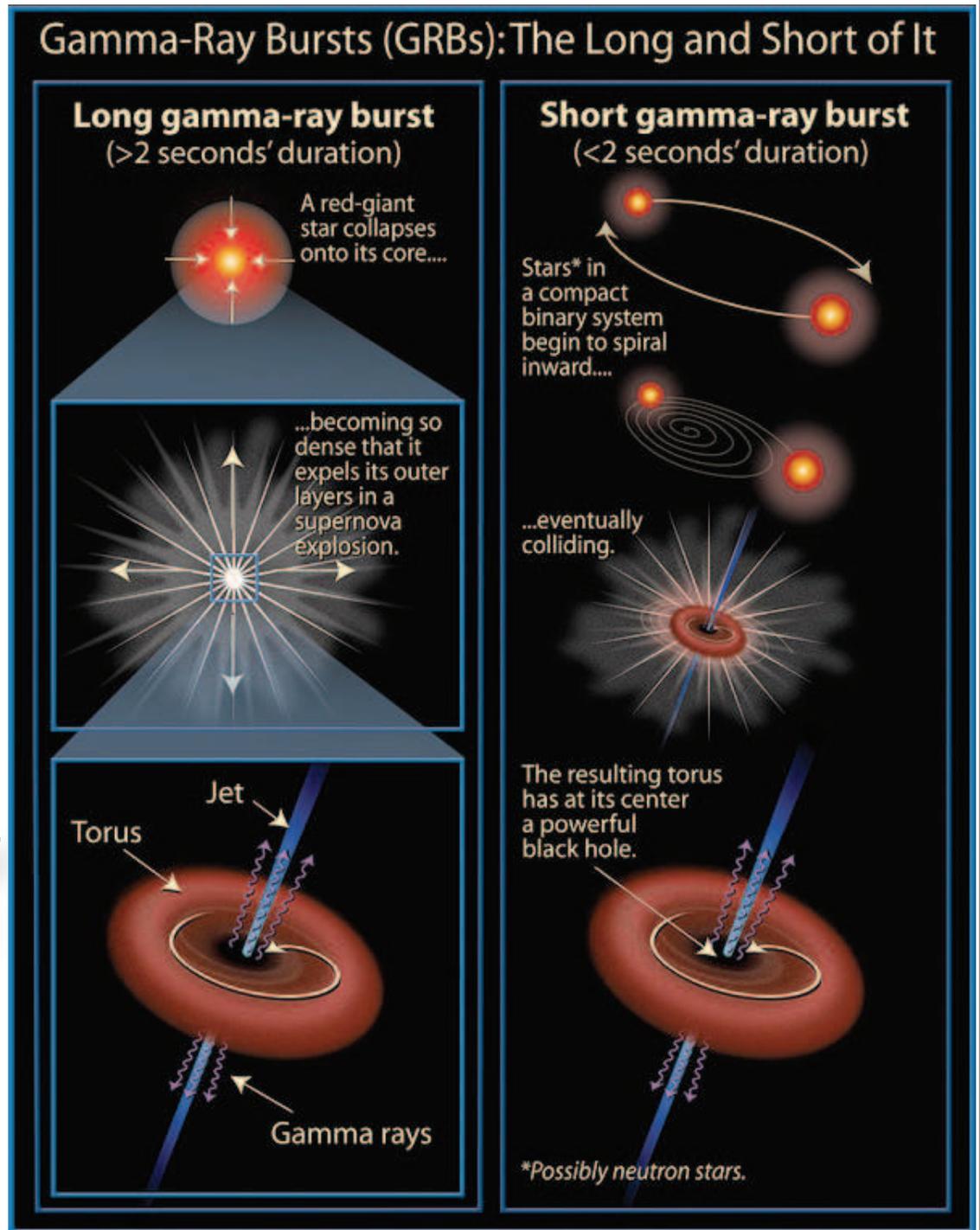
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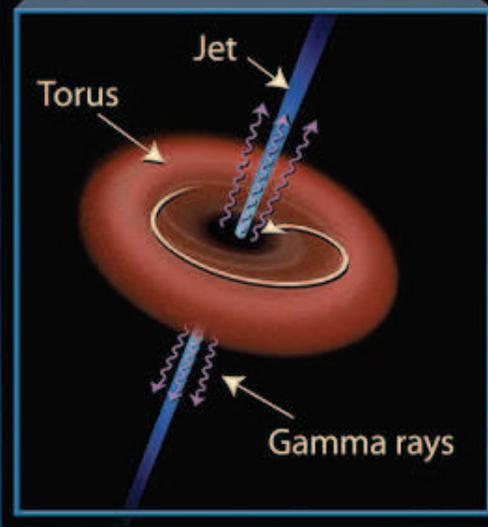
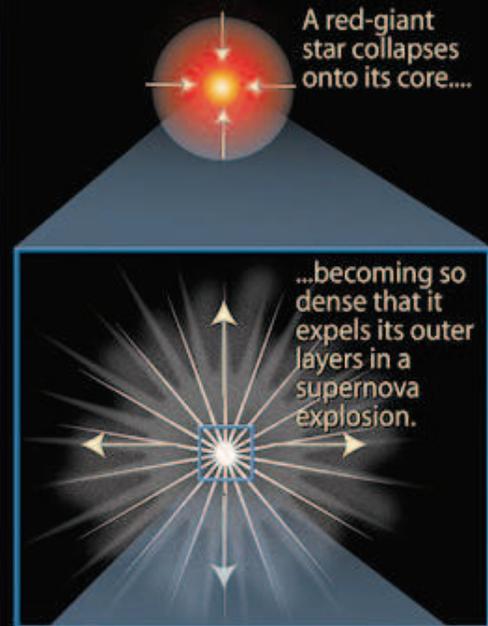
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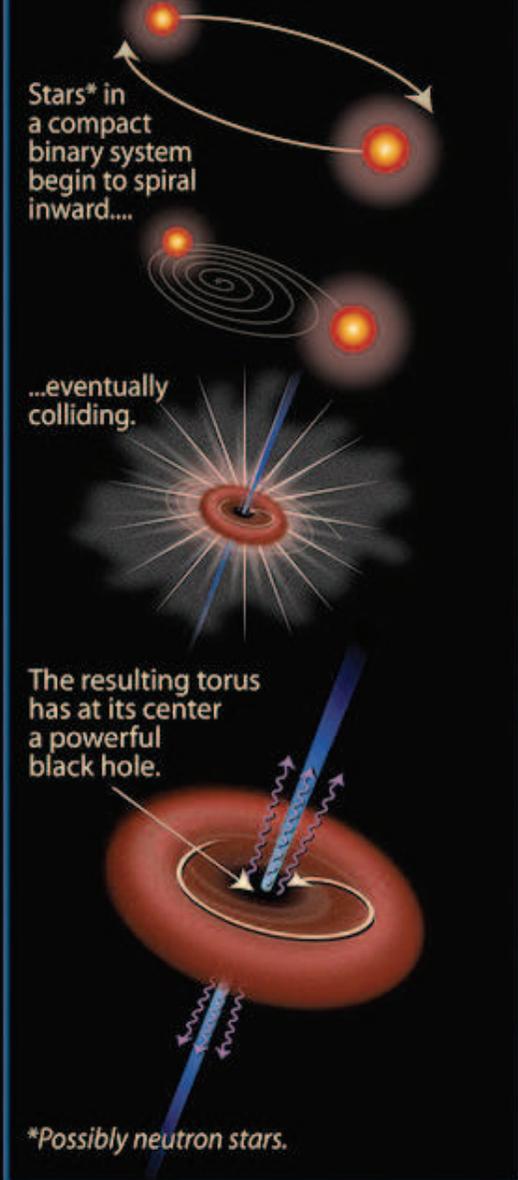
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Long gamma-ray burst (>2 seconds' duration)

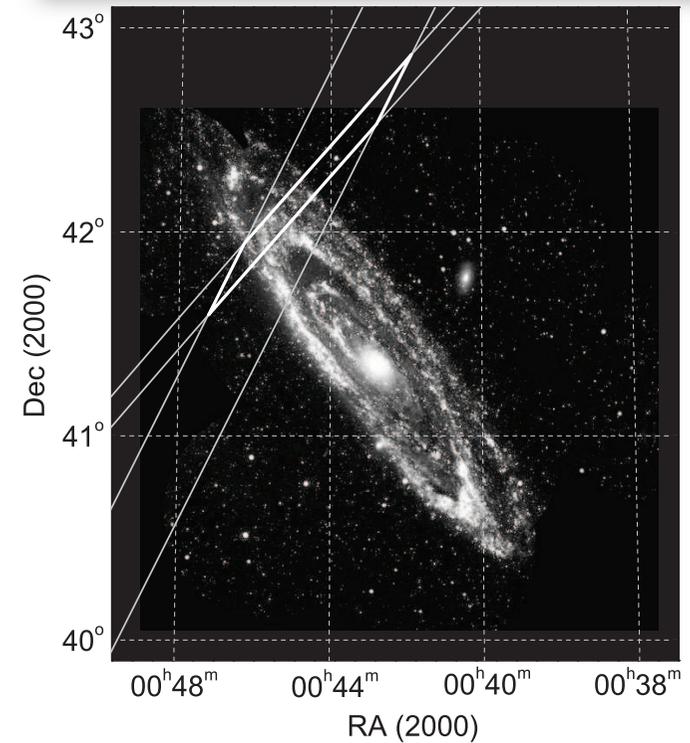
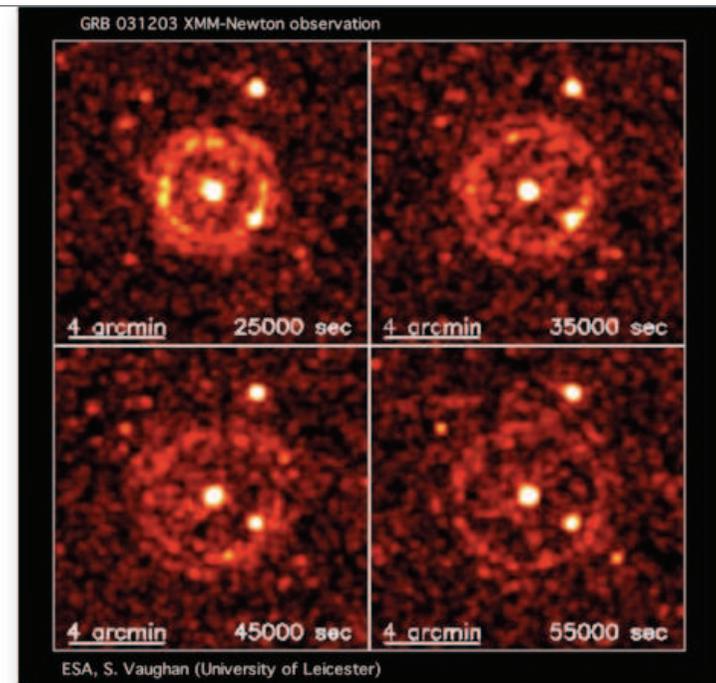


Short gamma-ray burst (<2 seconds' duration)



Origin of GRB 070201 from LIGO Observations

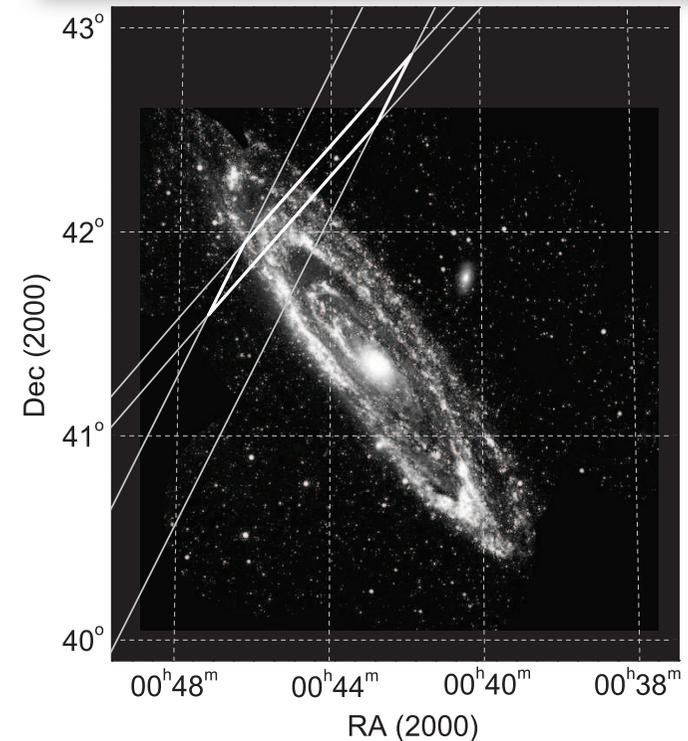
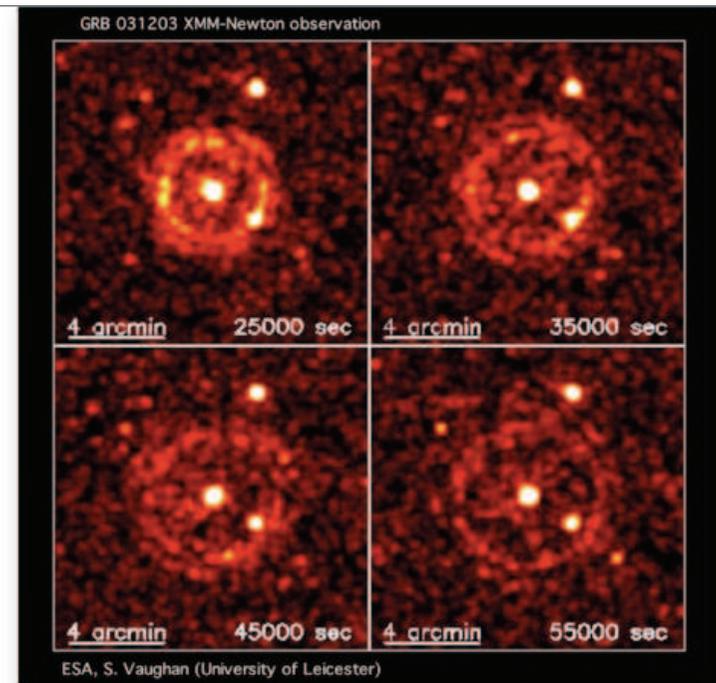
LSC, *Astrophys. J.* **681**, (2008) 1419



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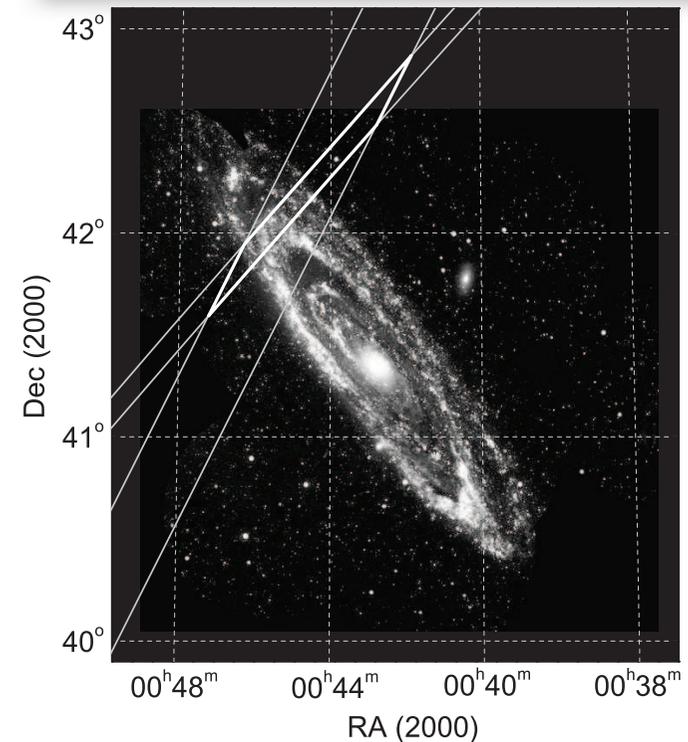
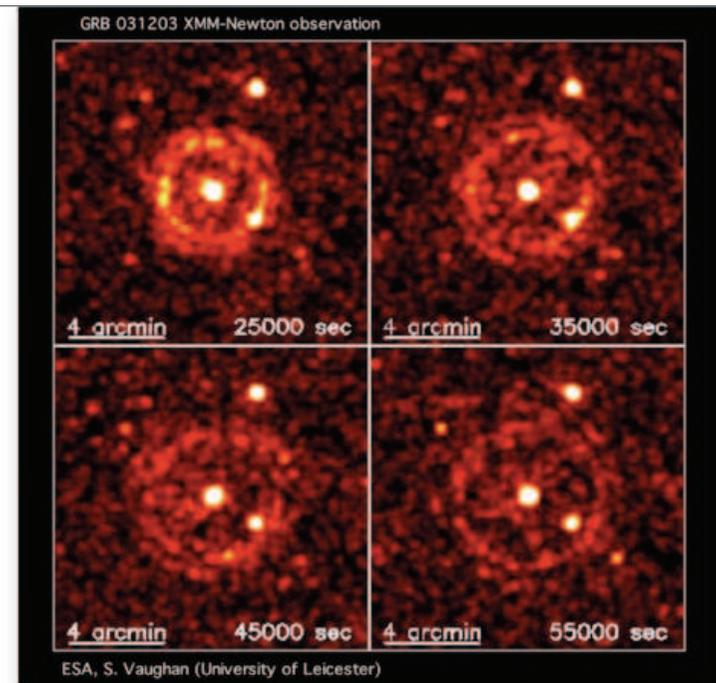
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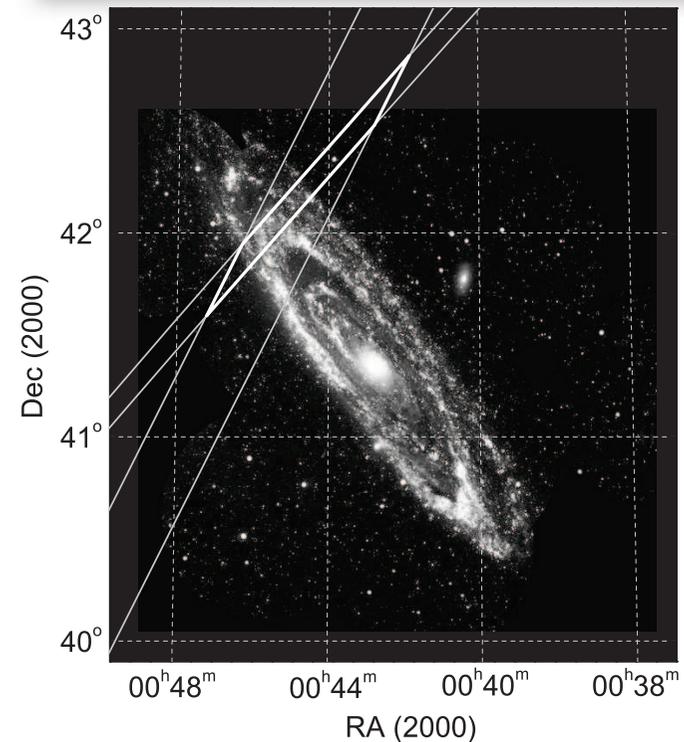
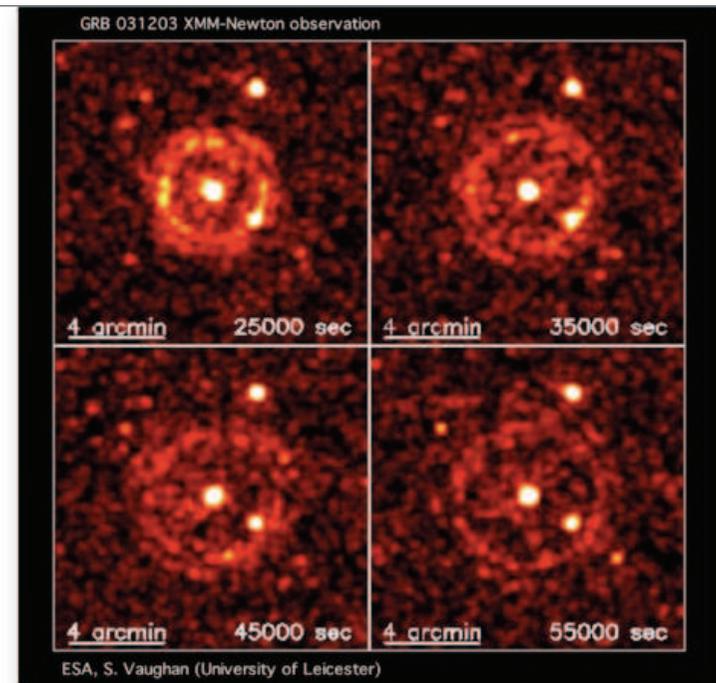
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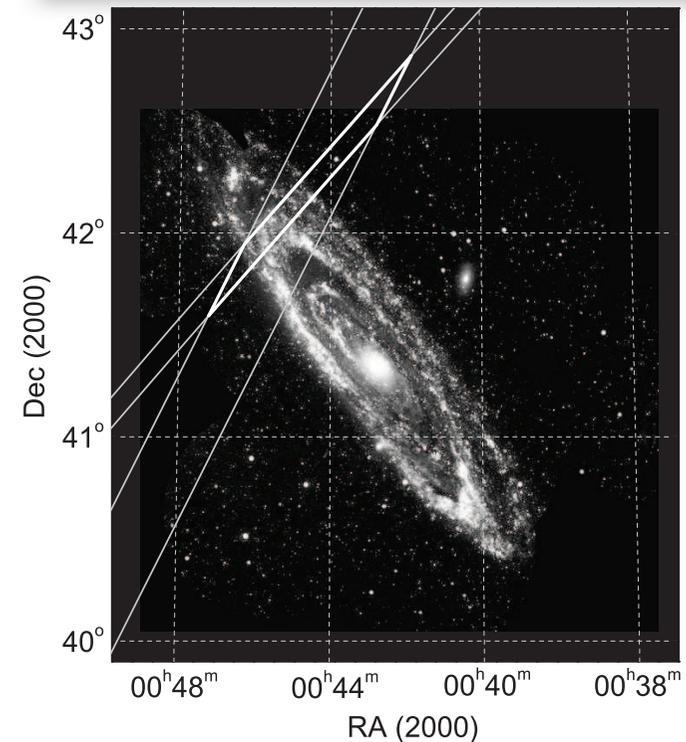
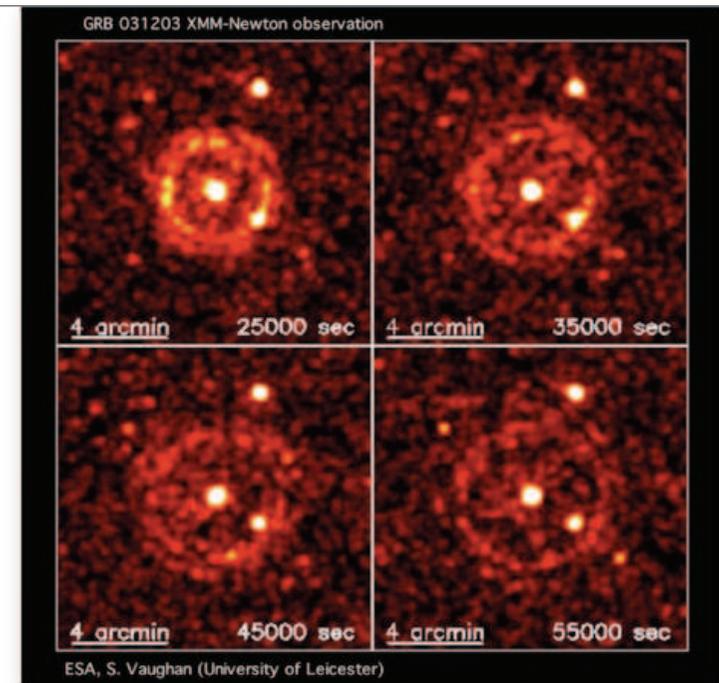
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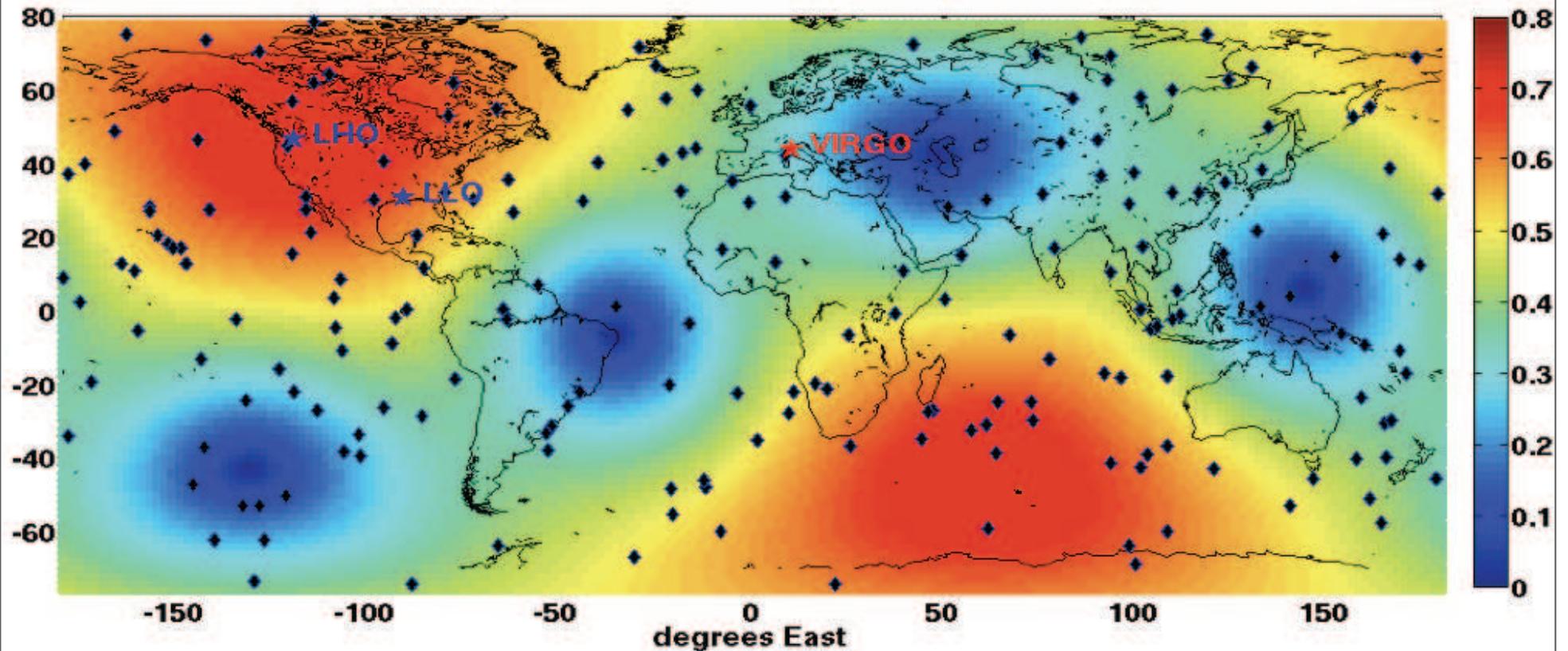
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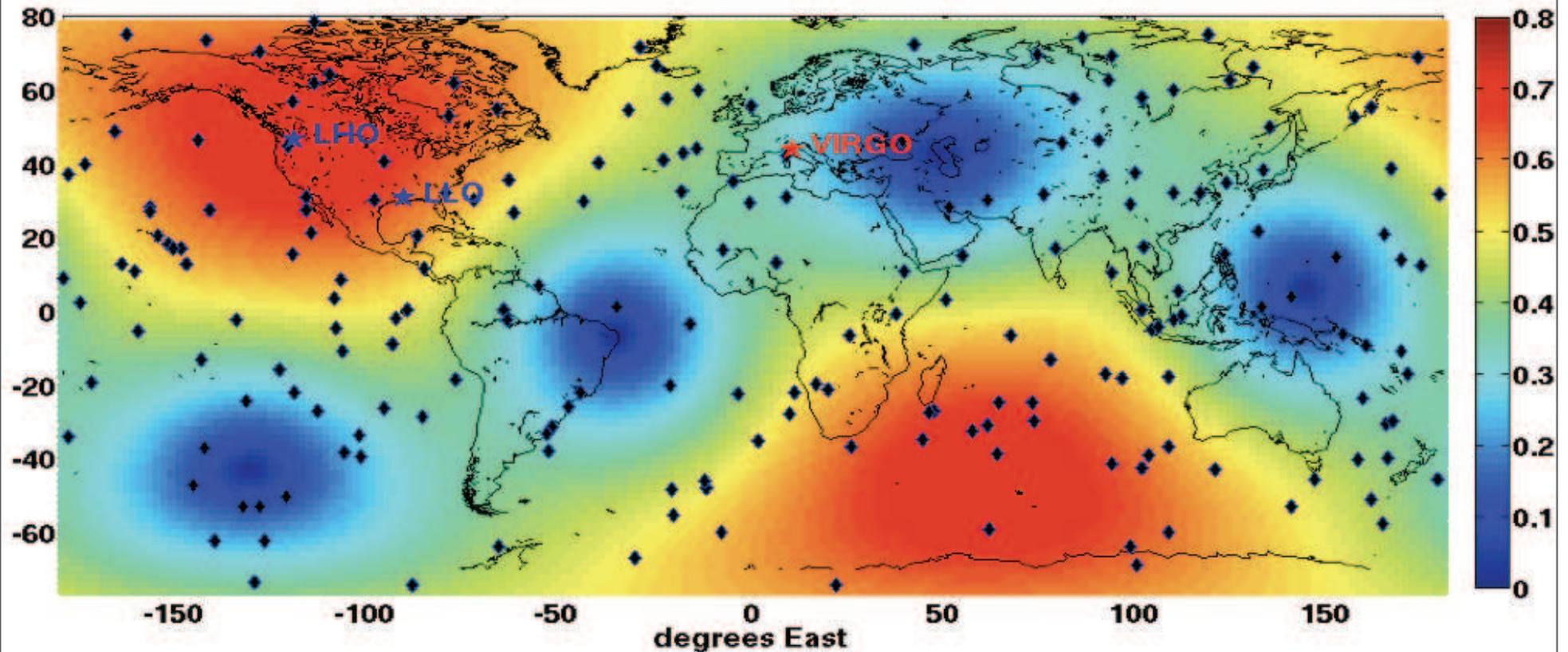
Search for GRBs during all of S5



Tuesday, 14 December 2010

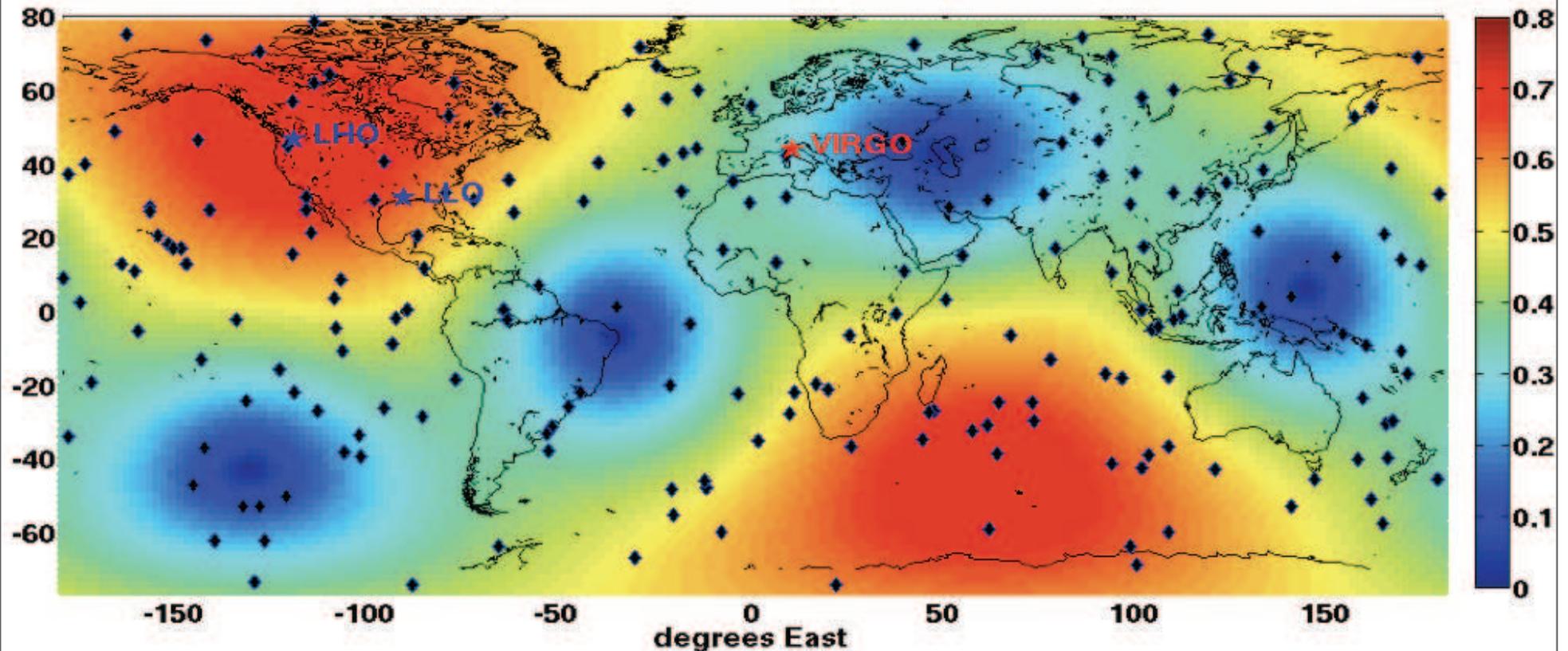
Search for GRBs during all of S5

• Nov 2005 - Oct 2007: **212** GRBs



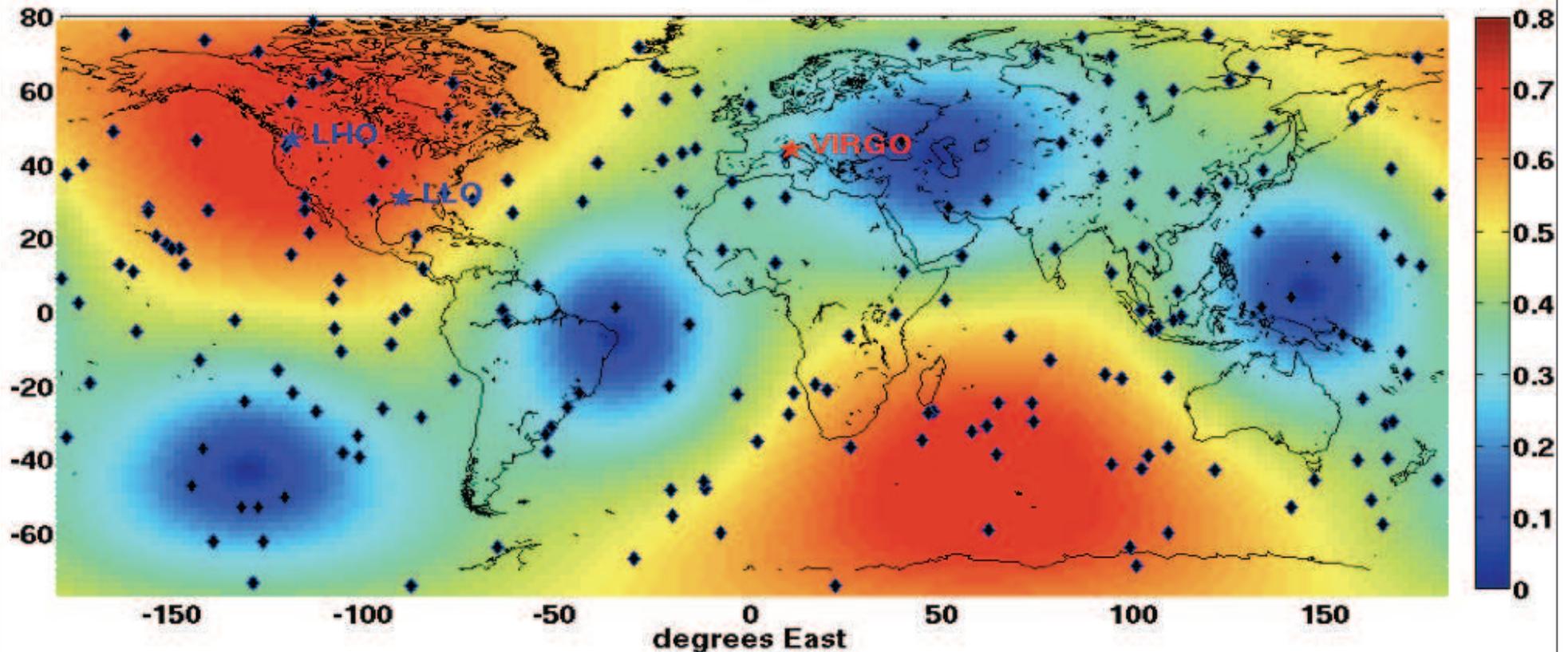
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Spin-down limit on the Crab pulsar

LSC, ApJ Lett., **683**, (2008) 45



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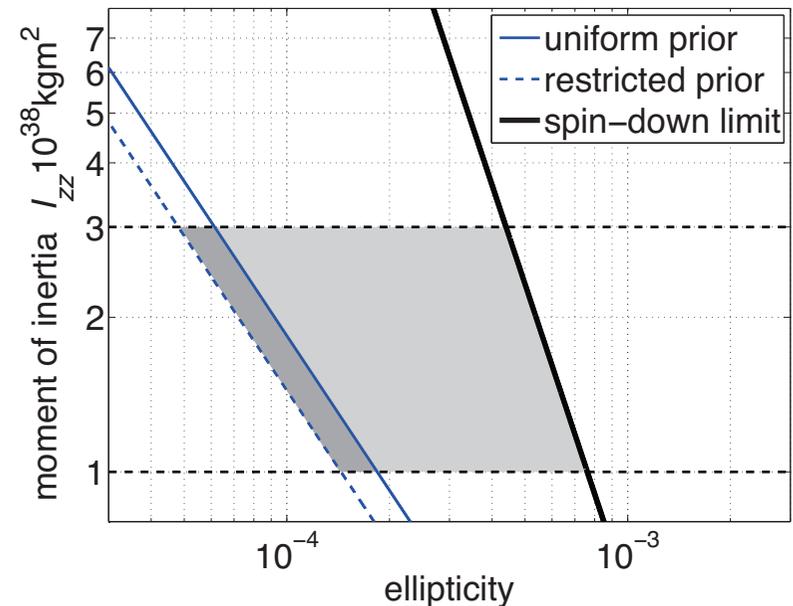
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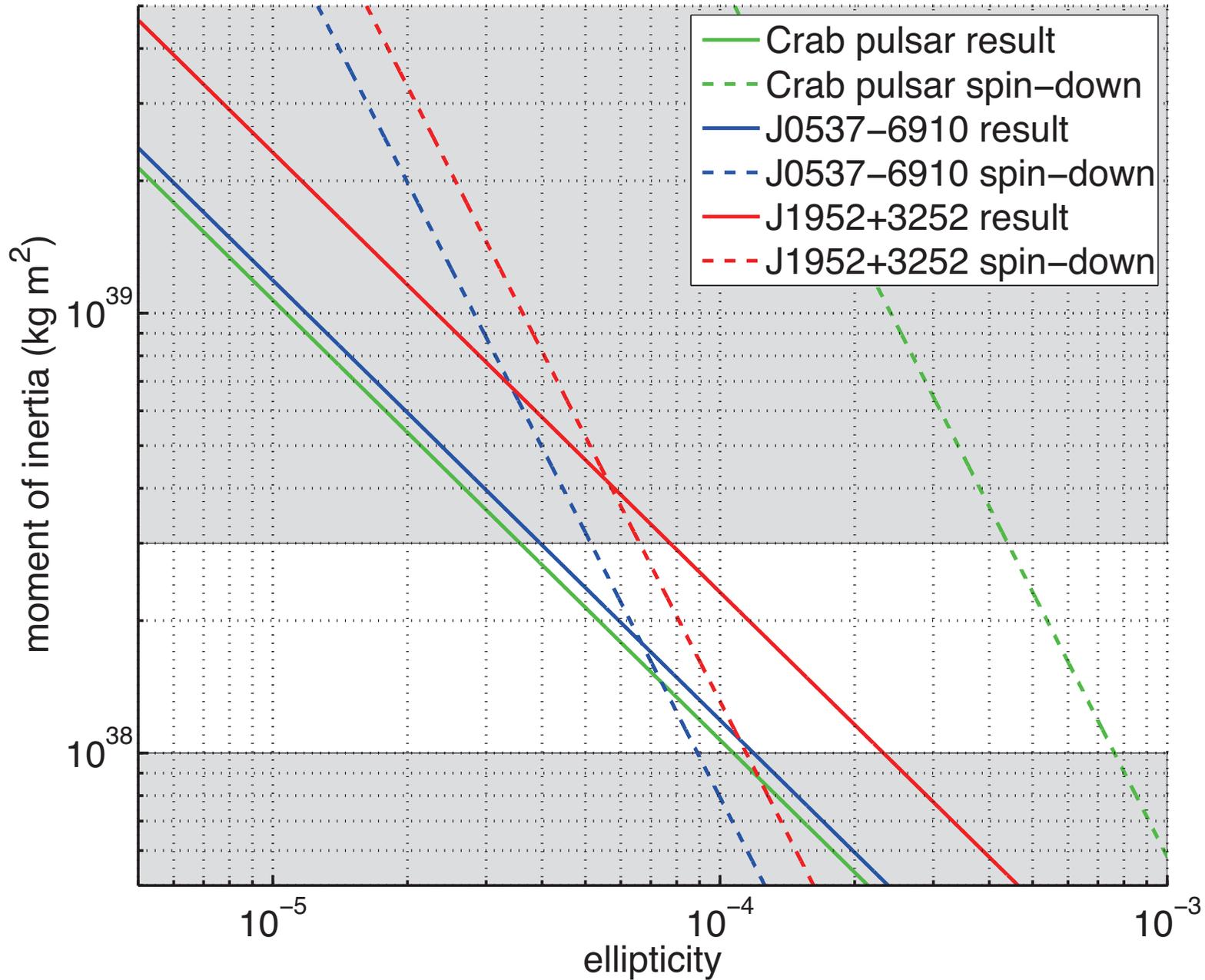
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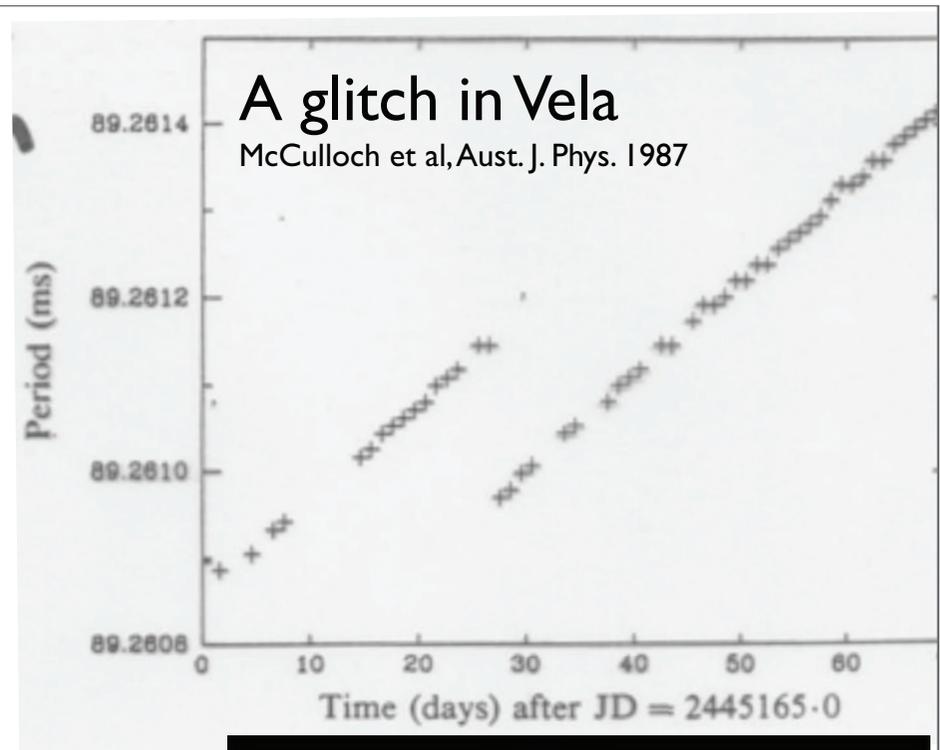
S5 Key Results



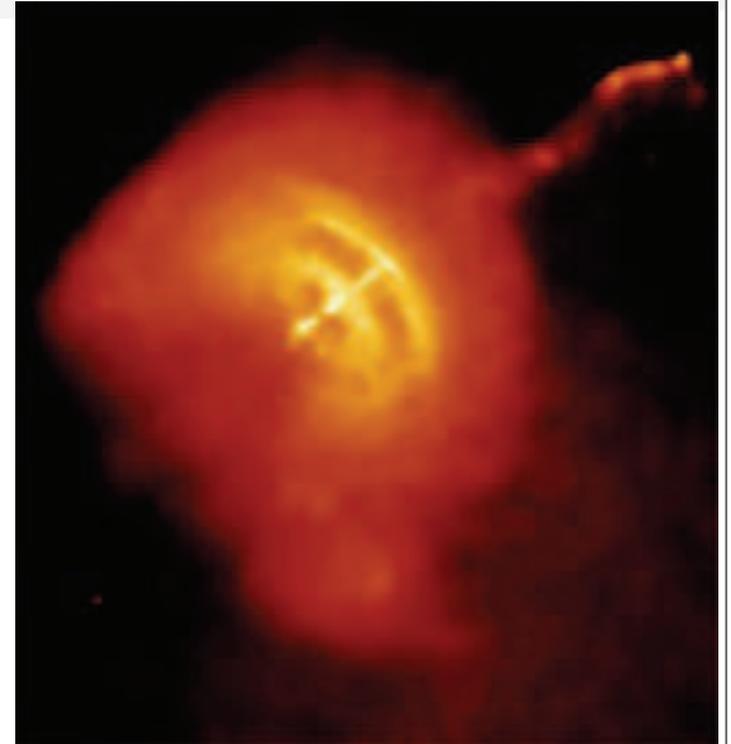
Some Interesting Upper Limits

| JJD) | ν (Hz) | $\dot{\nu}$ (Hz s ⁻¹) | distance (kpc) | spin-down limit | joint $h_0^{95\%}$ | ellipticity | $h_0^{95\%}/h_0^{\text{sd}}$ |
|------|------------|-----------------------------------|----------------|------------------------|------------------------|-----------------------|------------------------------|
| 520 | 221.80 | $-6.1 \times 10^{-16}\dagger$ | 1.3 | 1.04×10^{-27} | 7.57×10^{-26} | 4.65×10^{-7} | 73 |
| 510 | 202.79 | $-5.1 \times 10^{-16}\dagger$ | 0.2 | 5.13×10^{-27} | 4.85×10^{-26} | 6.96×10^{-8} | 9.4 |
| 388 | 268.36 | $-2.0 \times 10^{-15}\dagger$ | 2.5 | 8.71×10^{-28} | 6.12×10^{-26} | 5.13×10^{-7} | 70 |

Pulsar Glitches

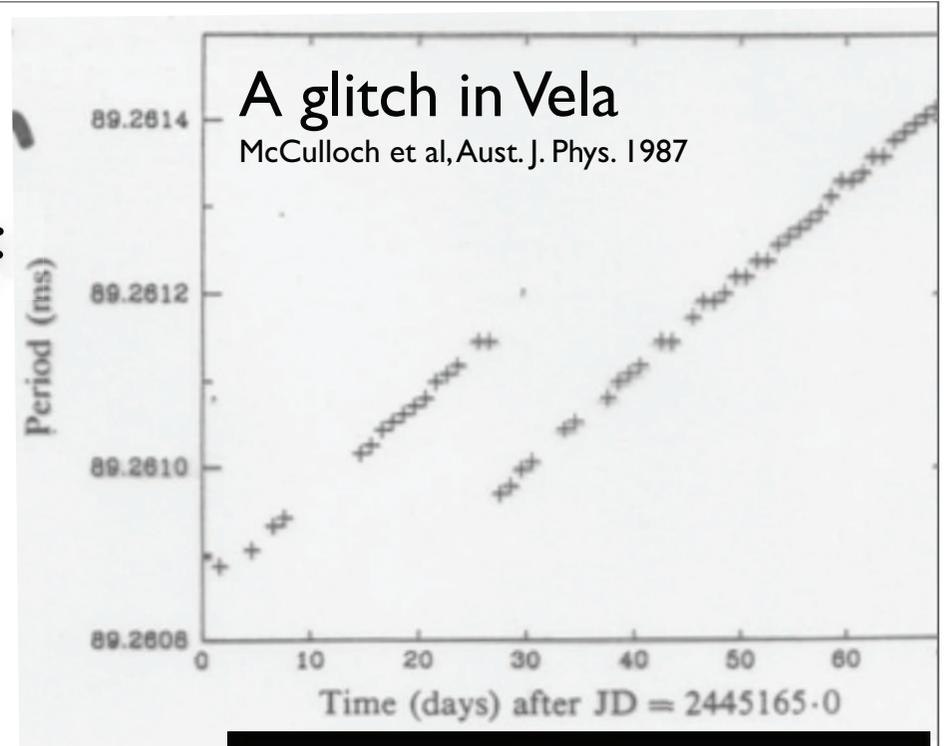


A composite Vela image

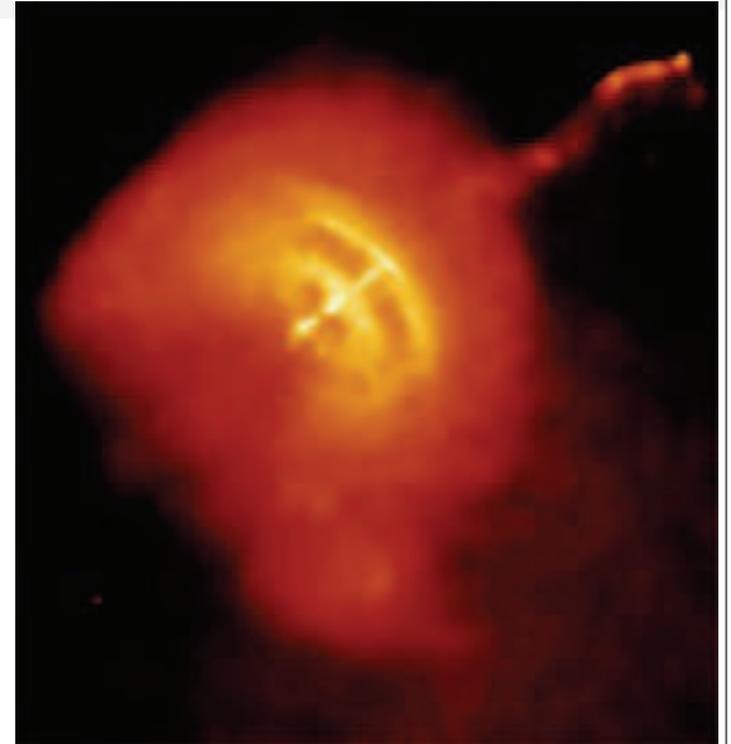


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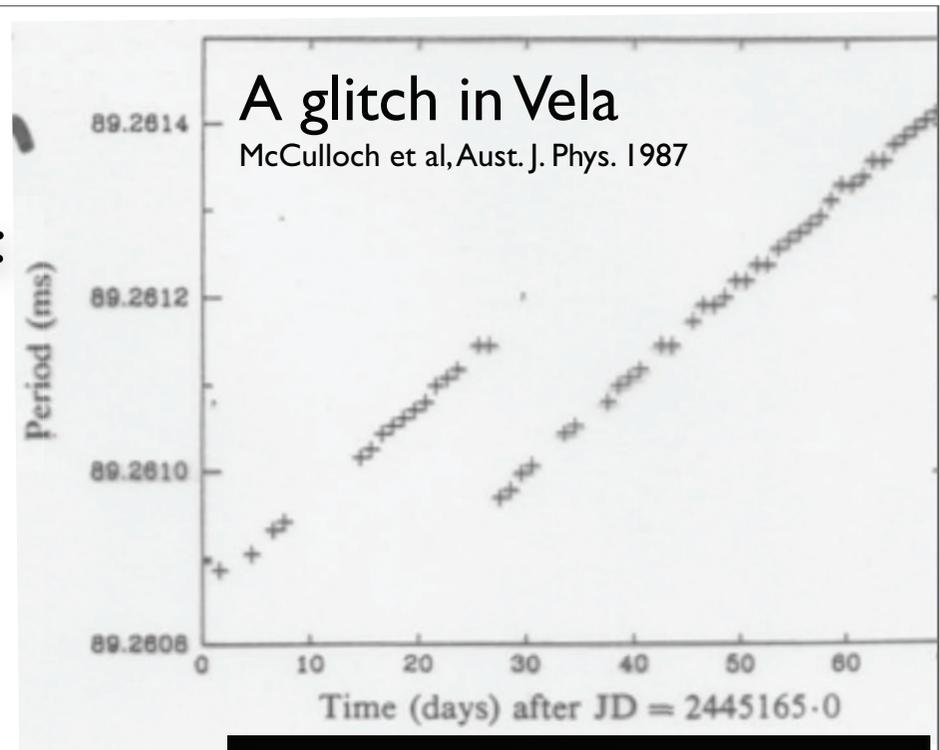


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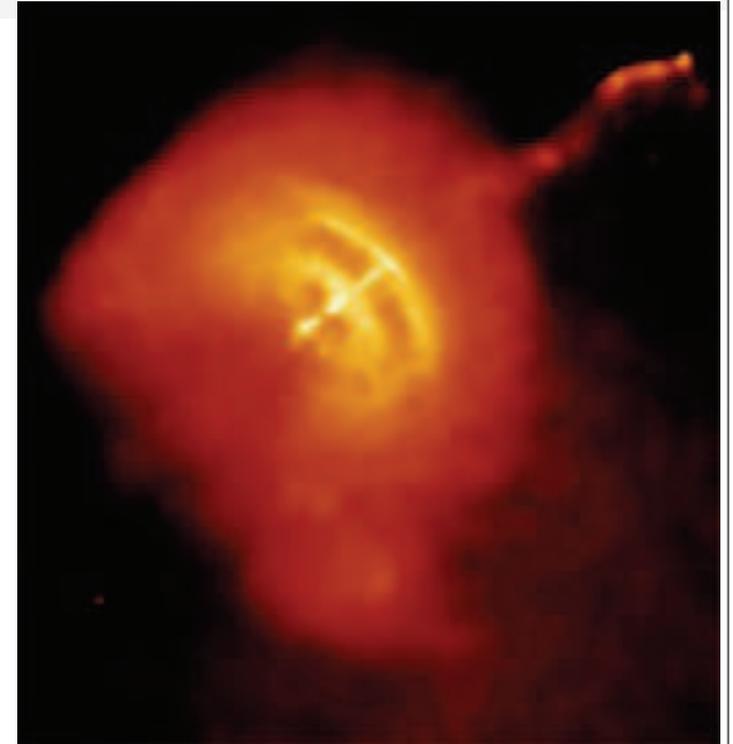


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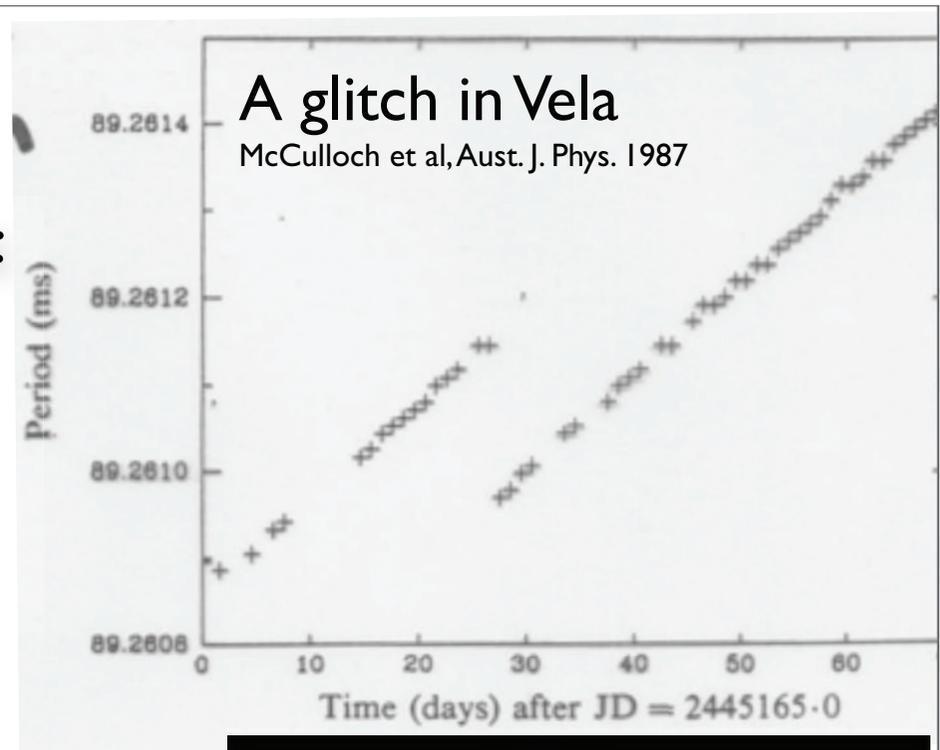


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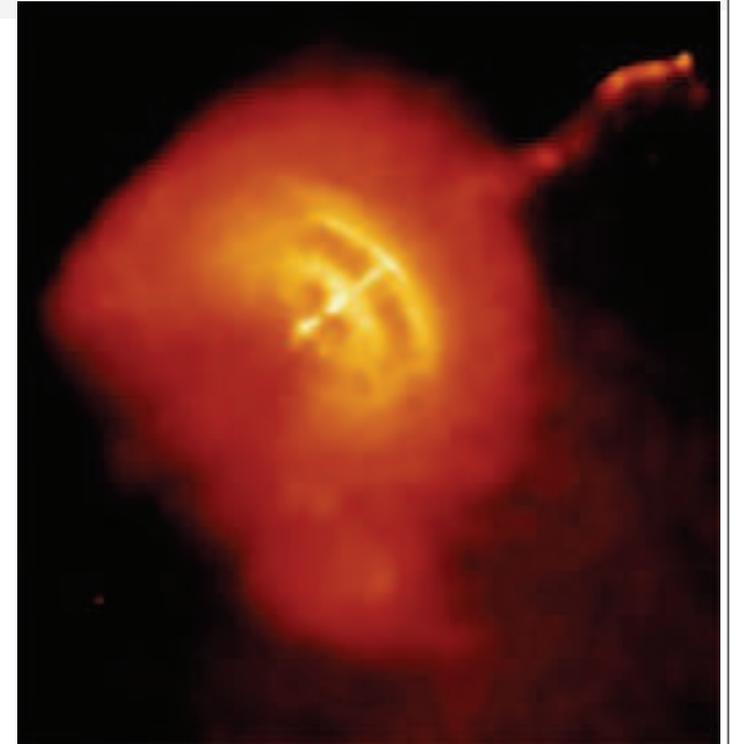


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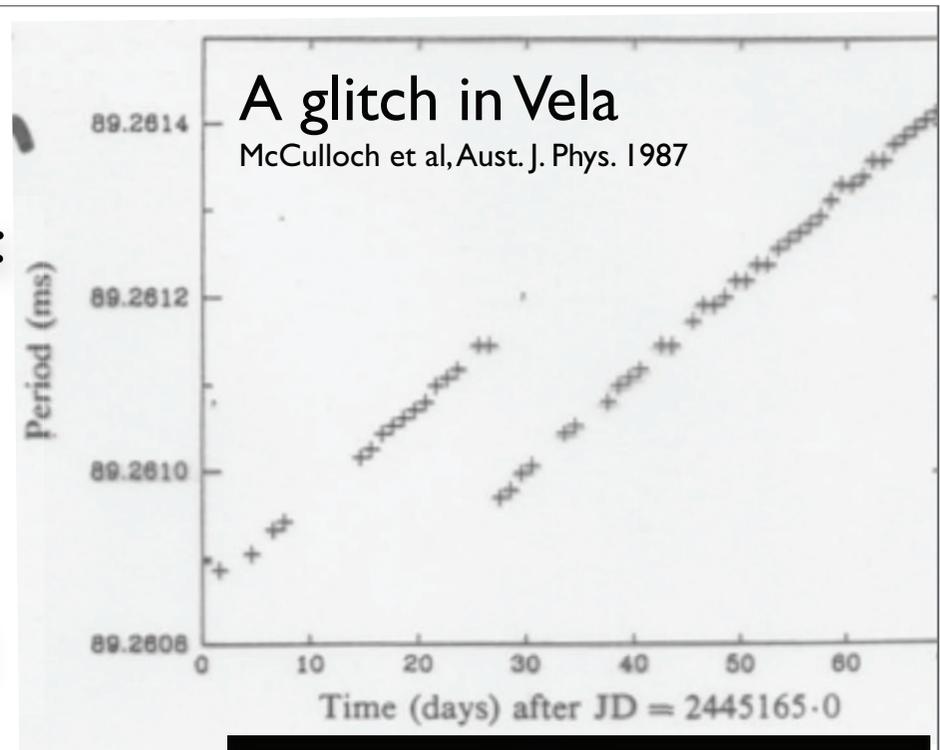


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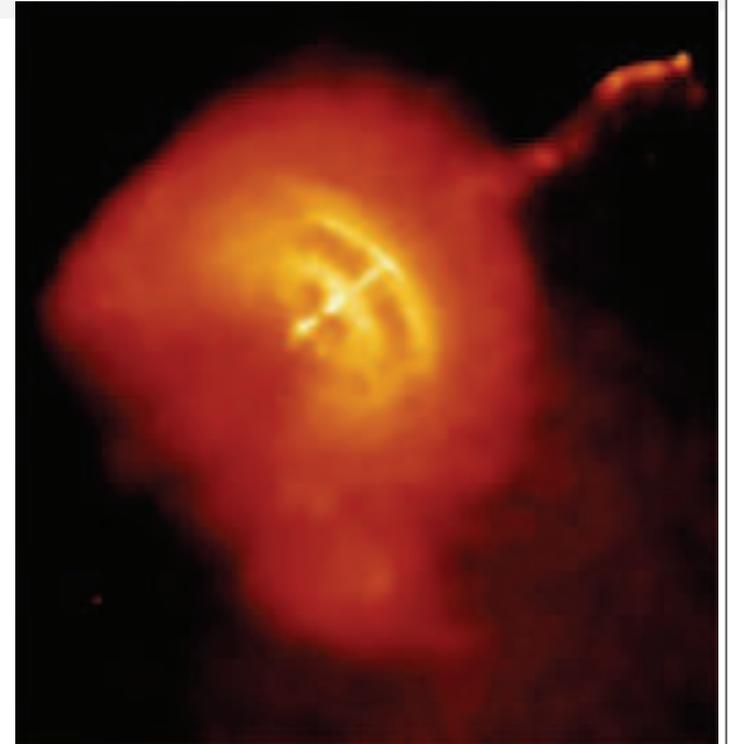


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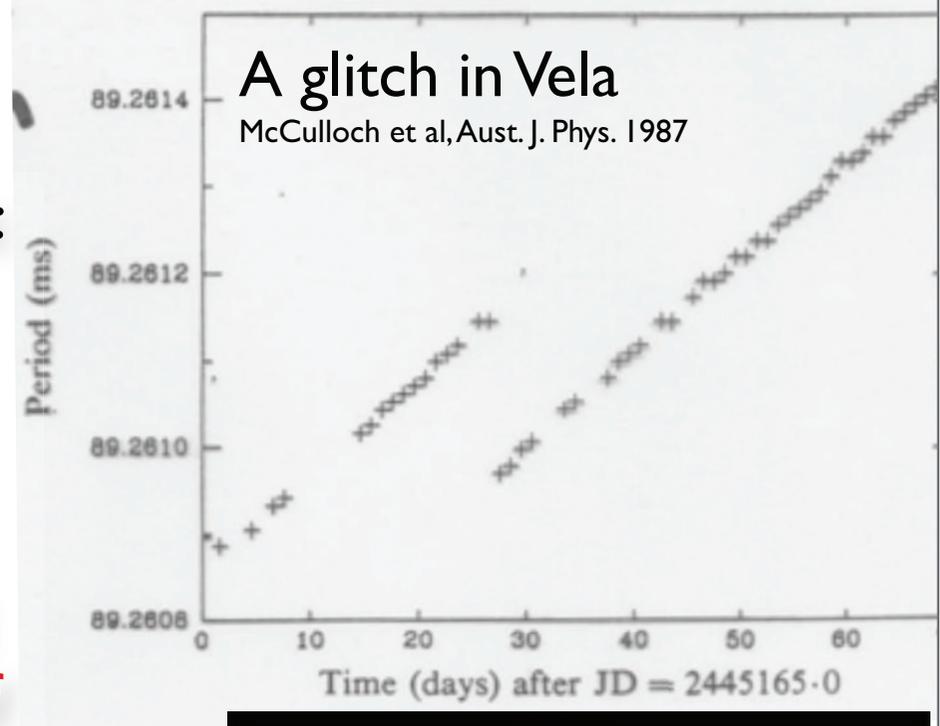


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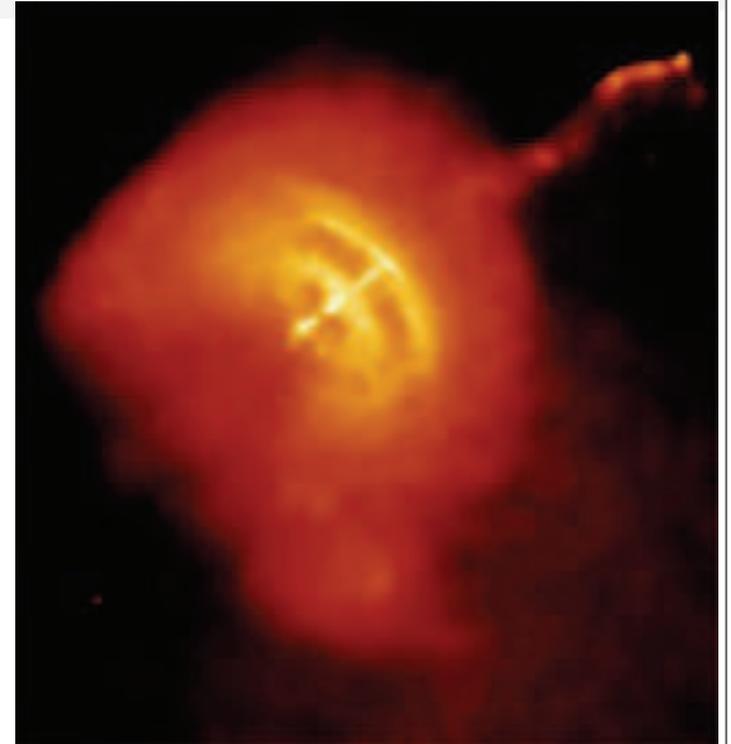


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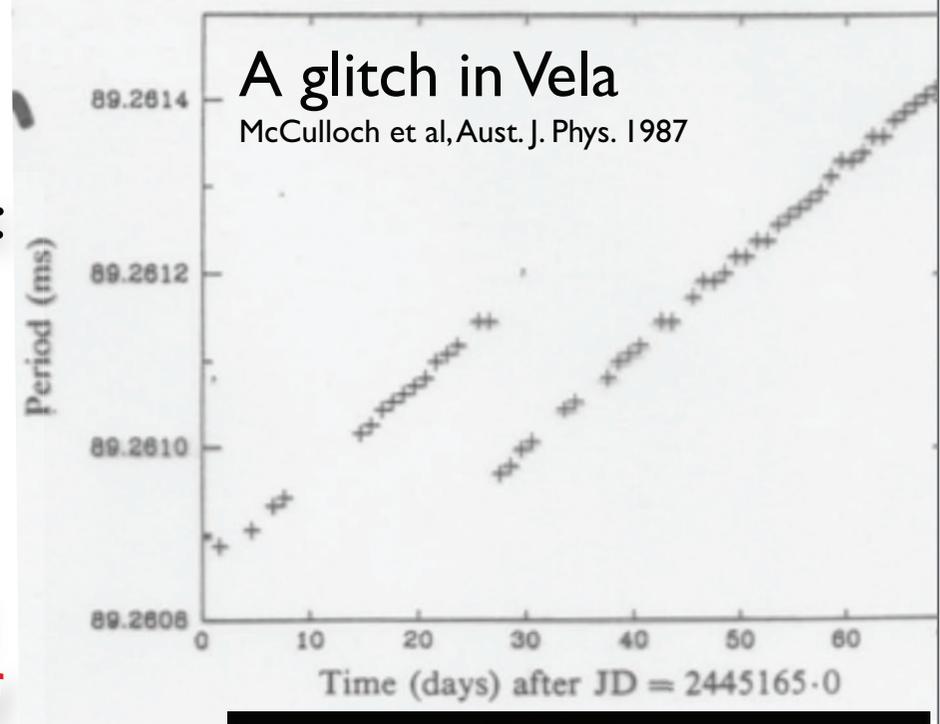


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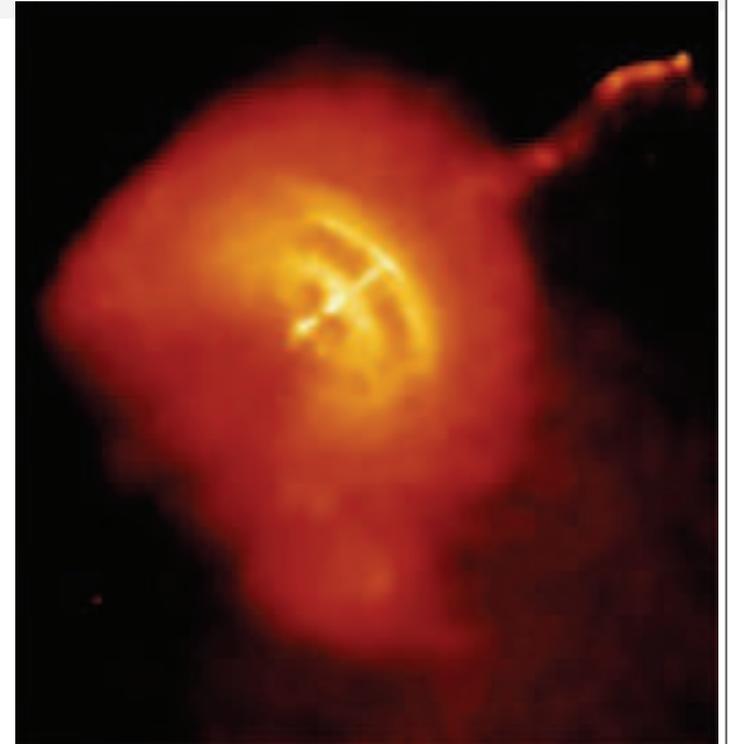


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- At some critical lag rotation rate superfluid core couples to the crust imparting energy to the crust



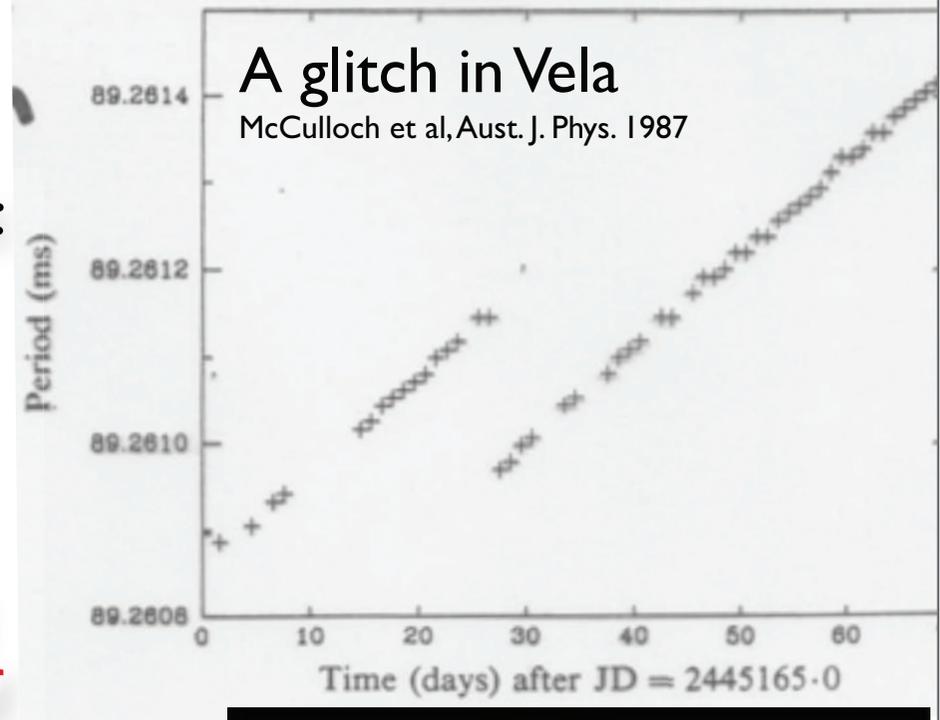
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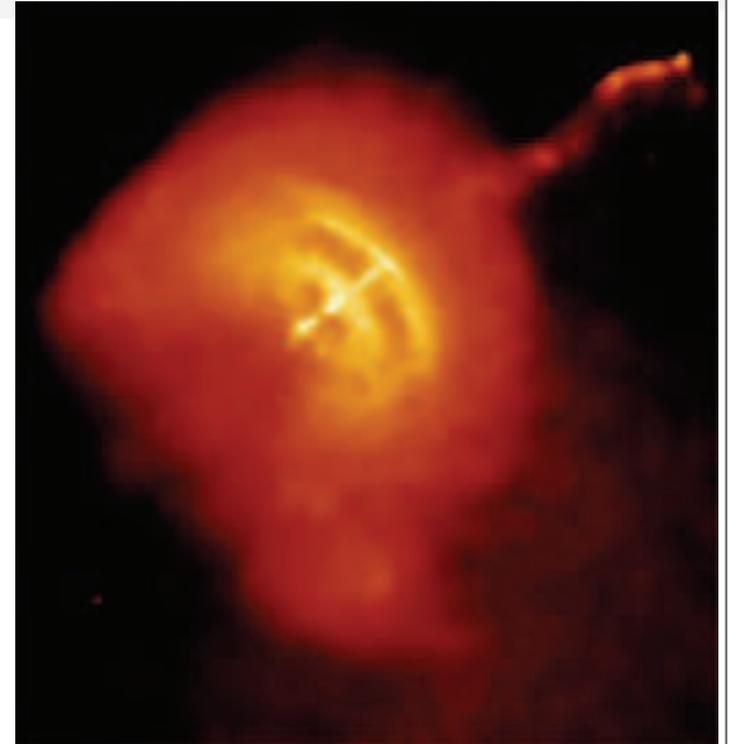
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- Could be the result of transfer of angular momentum from core to crust
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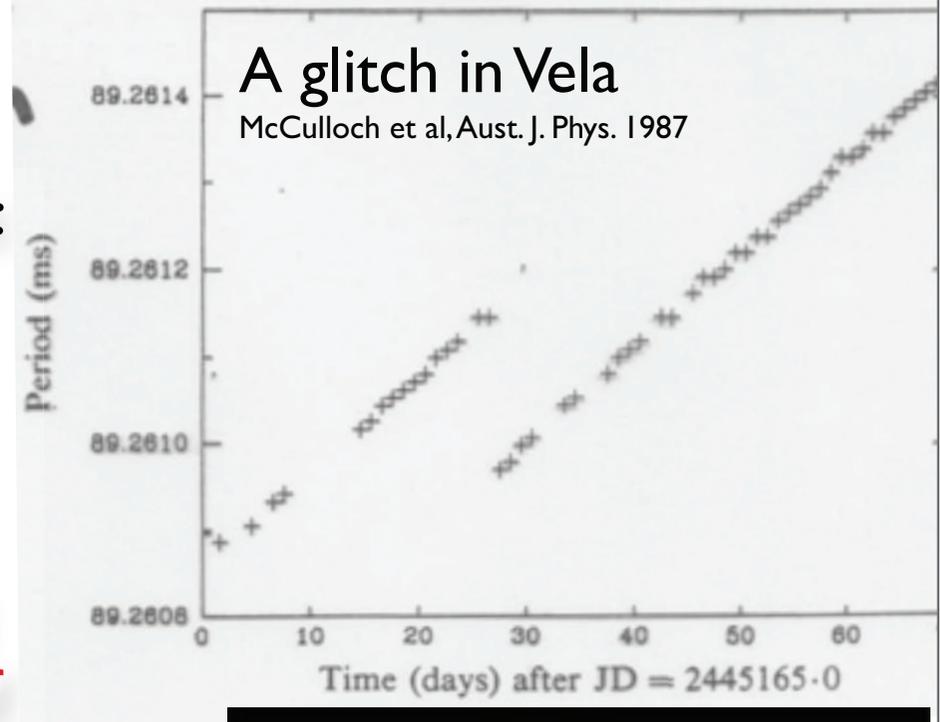
A composite Vela image



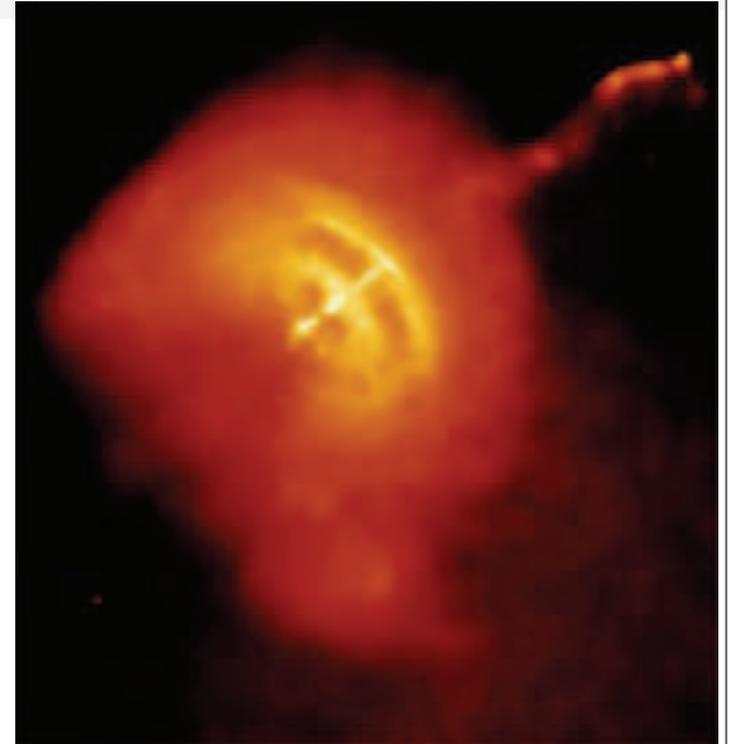
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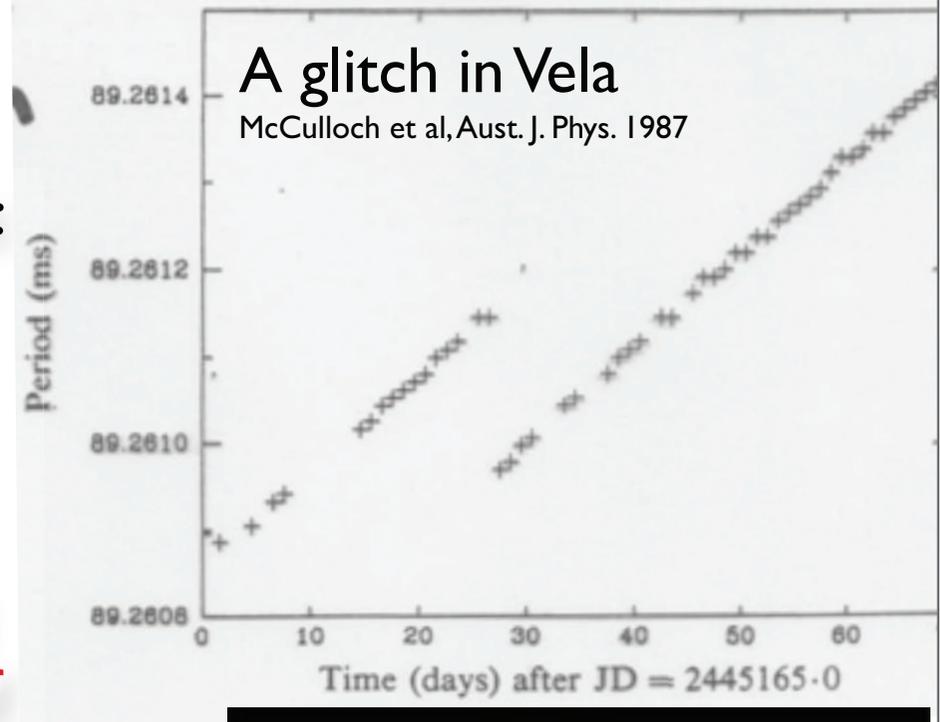
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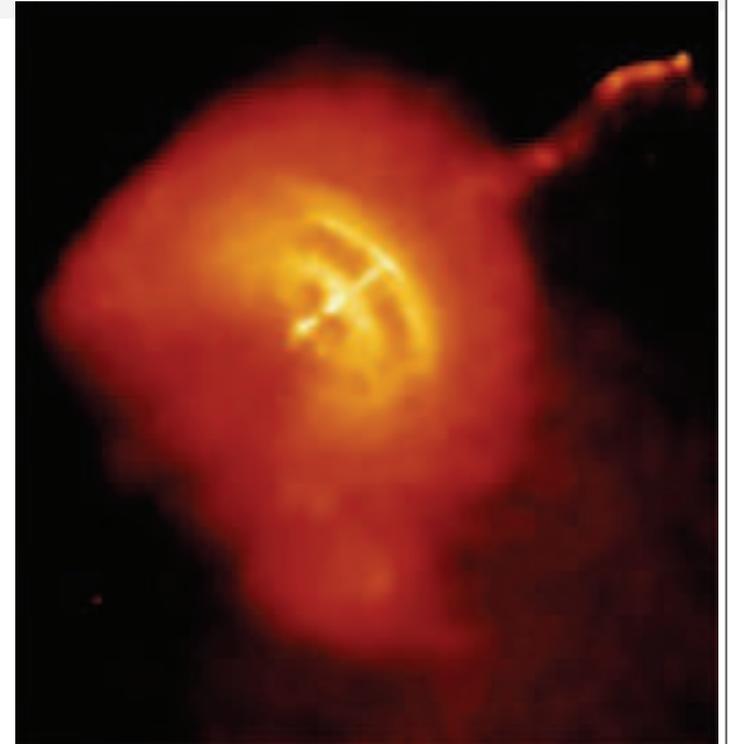
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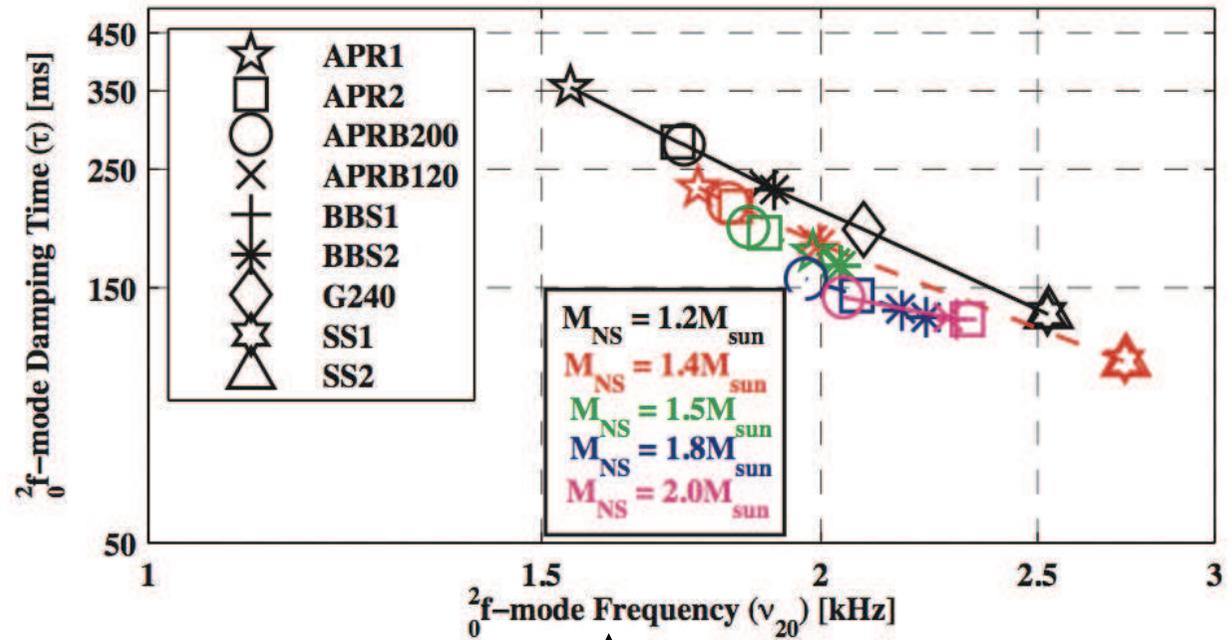
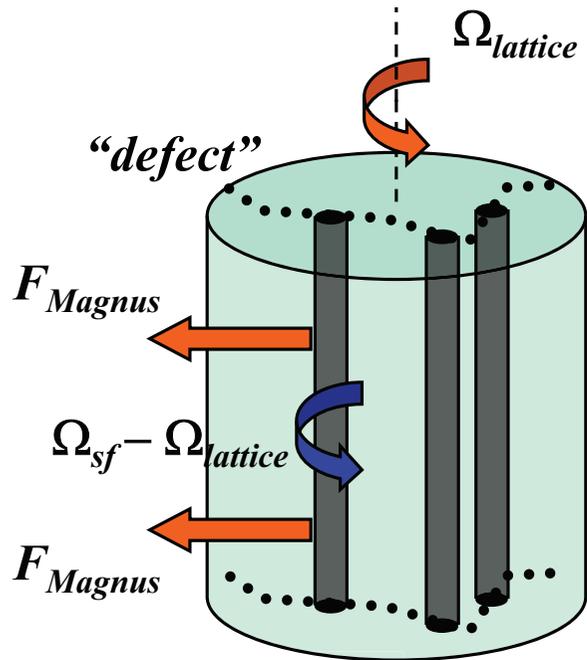
$$\Delta E \sim 10^{-13} - 10^{-11} M_{\odot} c^2$$



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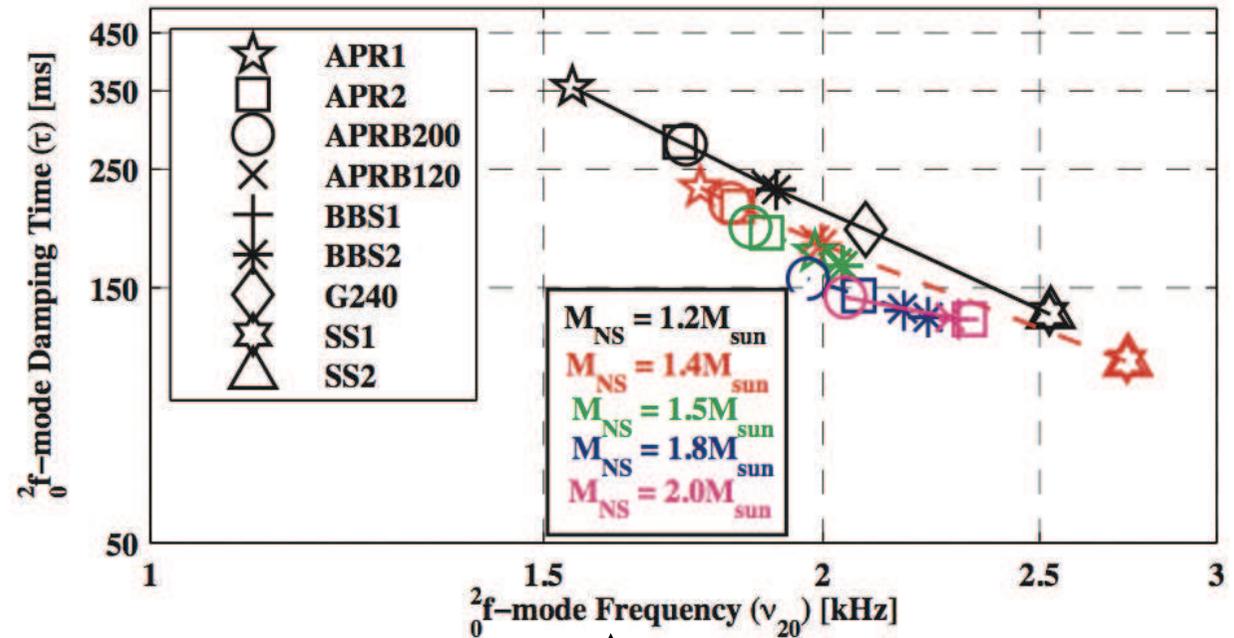
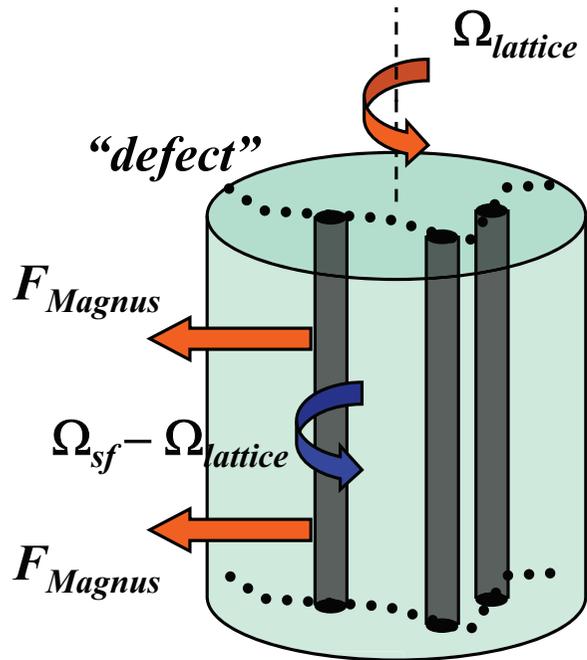


NS Normal Mode Oscillations



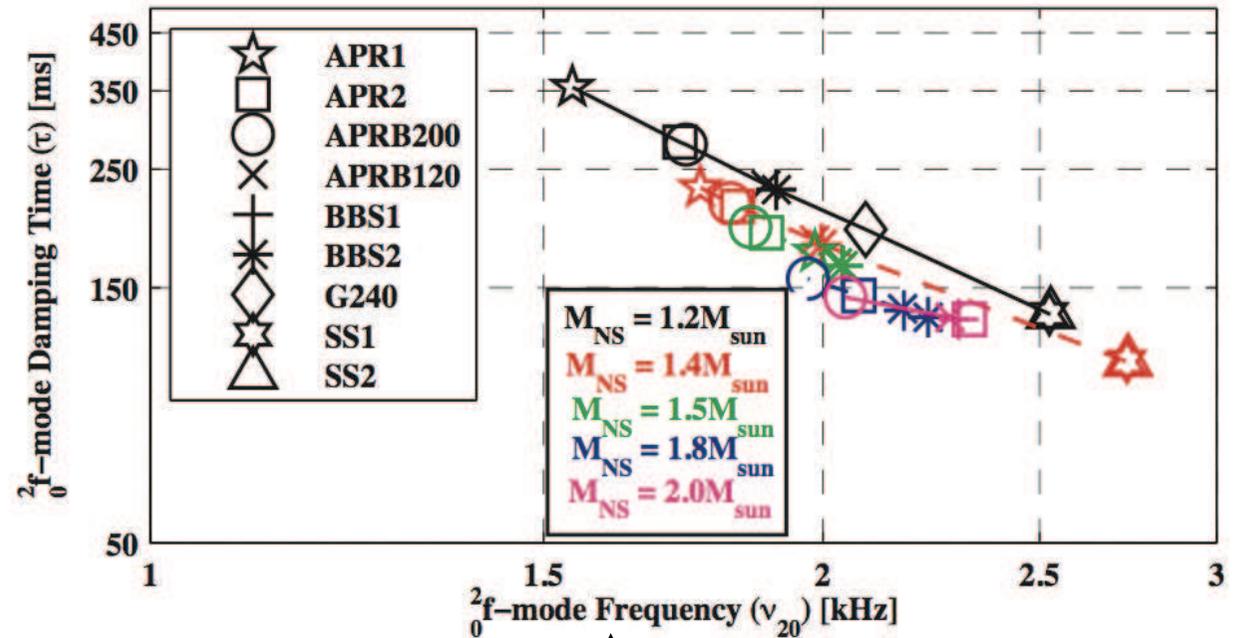
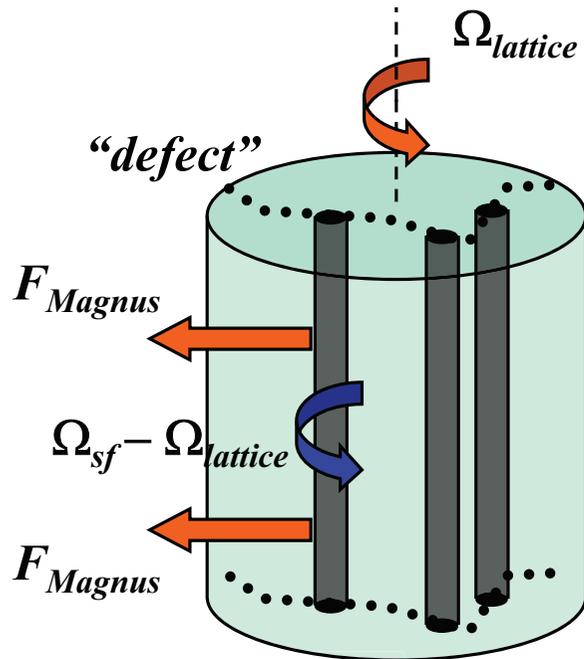
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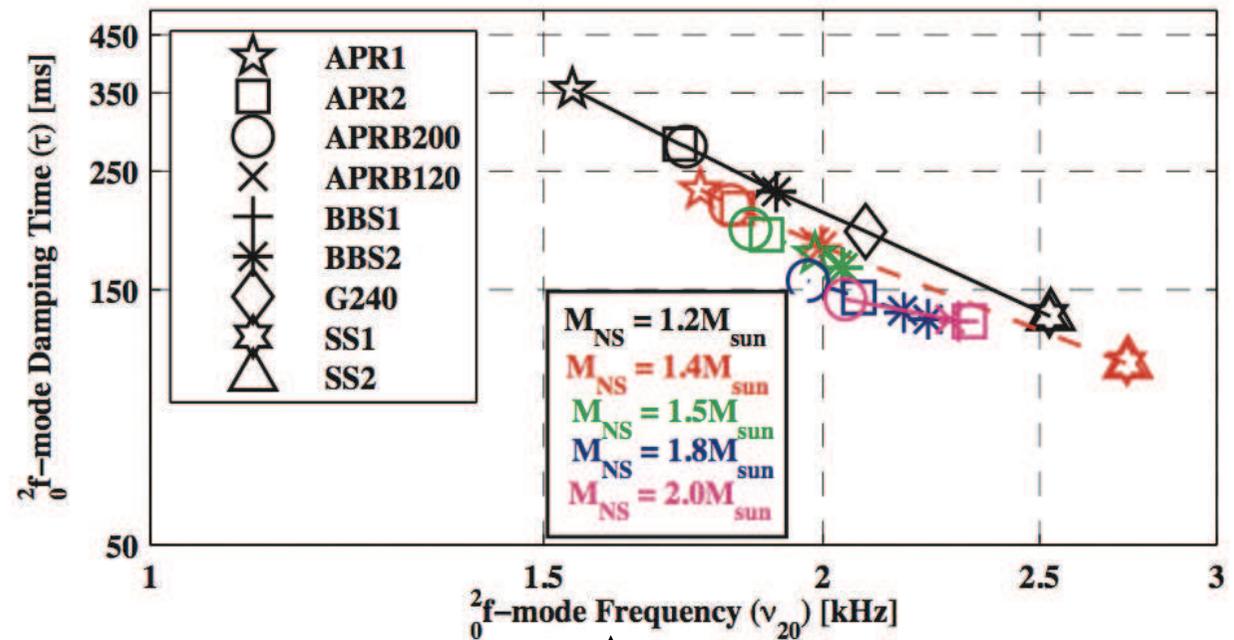
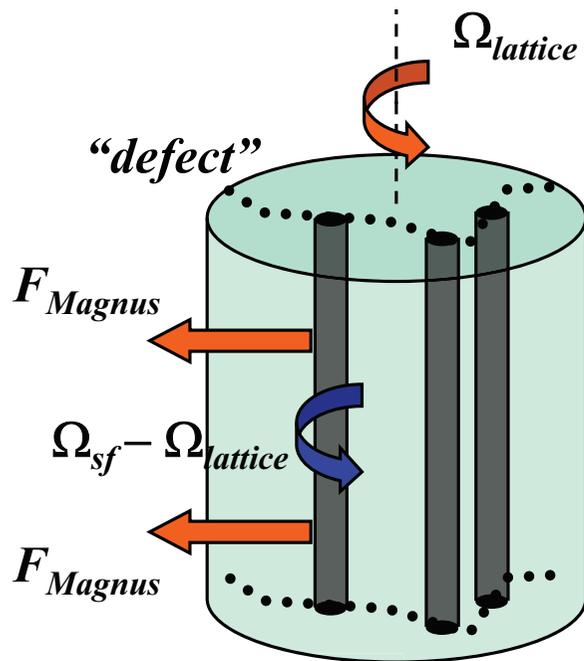
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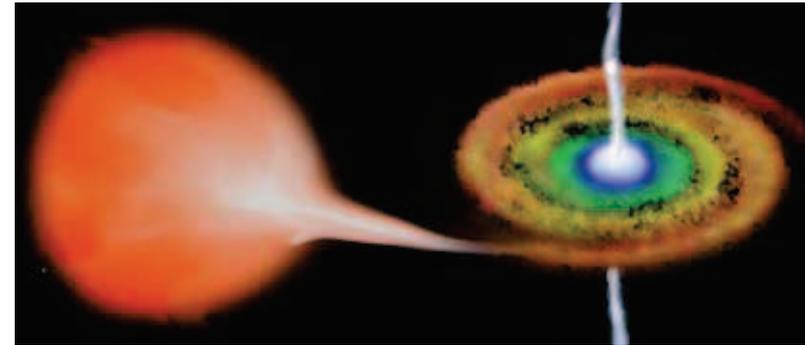


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- Detecting and measuring normal modes could reveal the equation-of-state of neutron stars and their internal structure

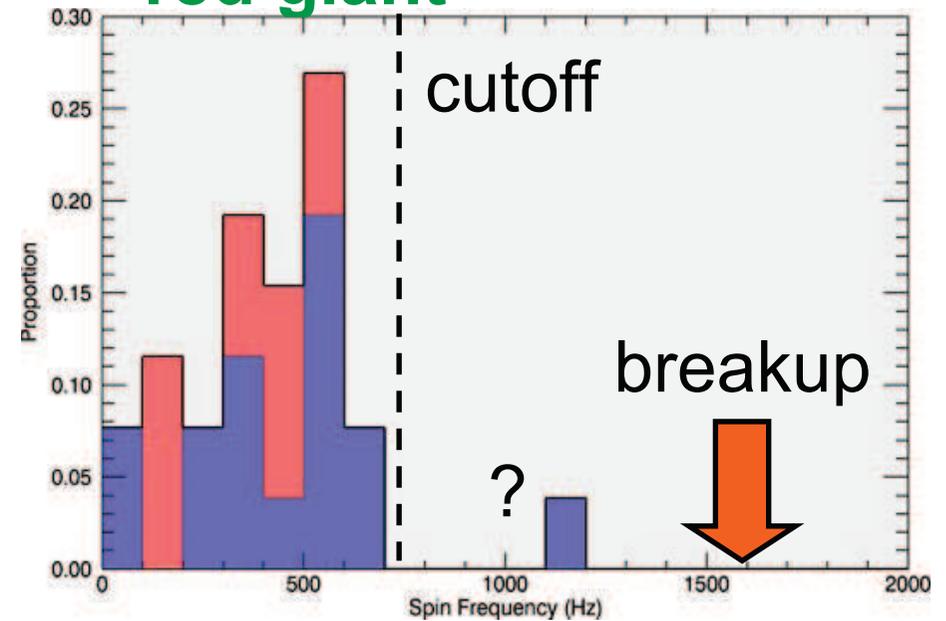


Accreting Neutron Stars



$< 1M_{\text{Sun}}$
red giant

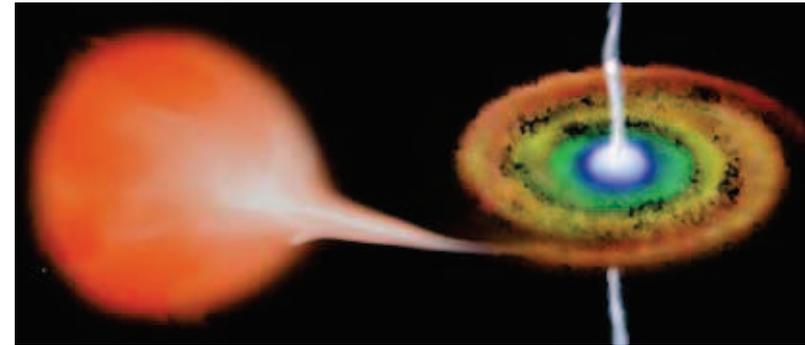
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pulses & burst oscillations

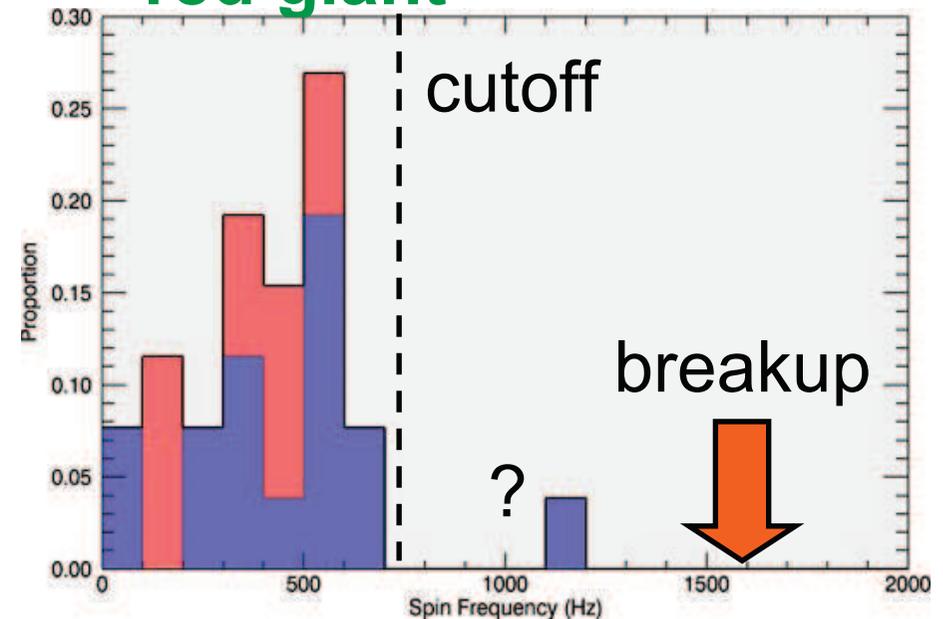
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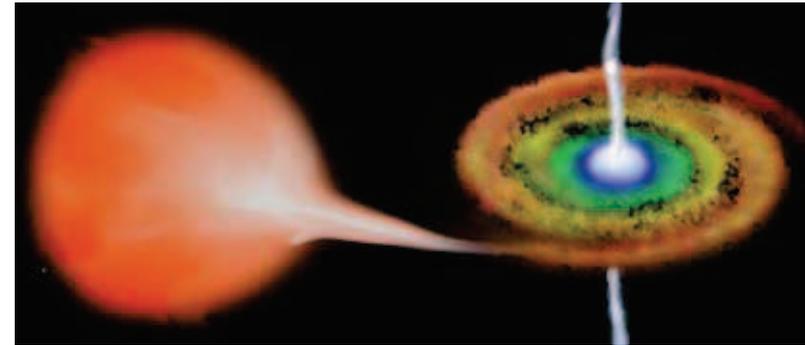
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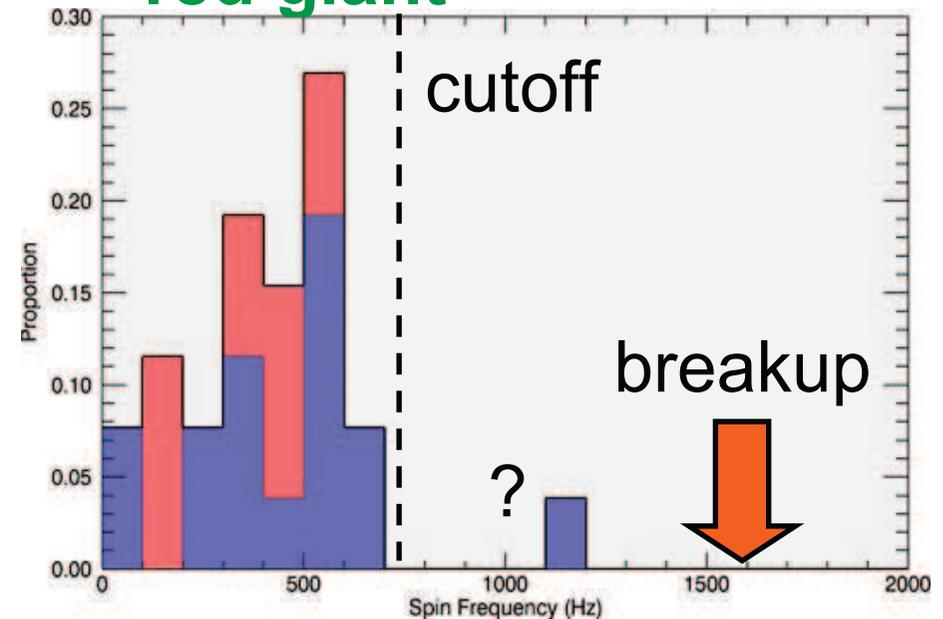
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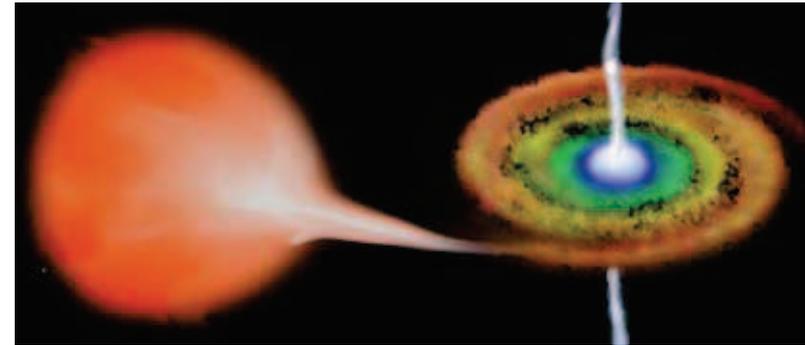
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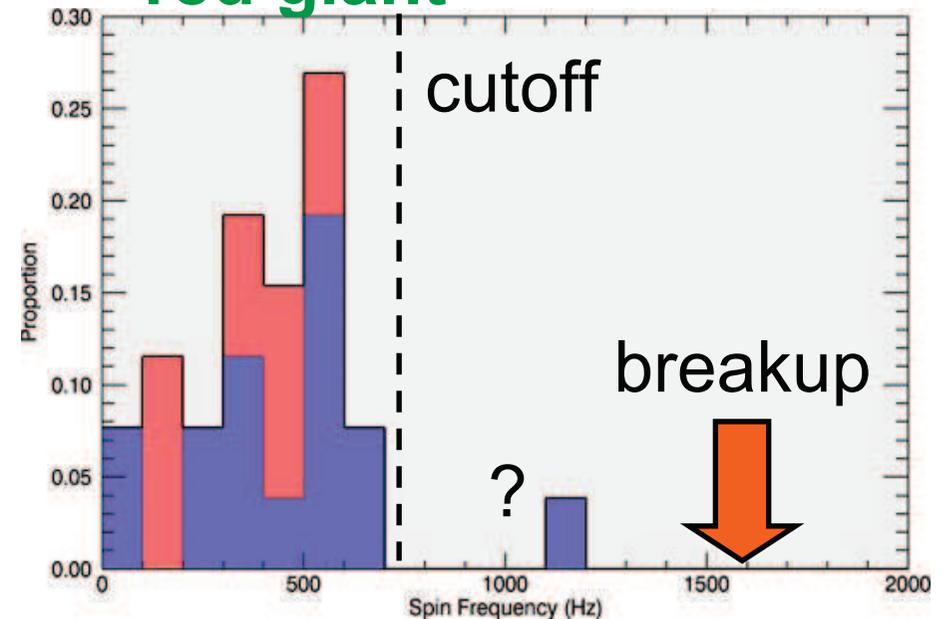
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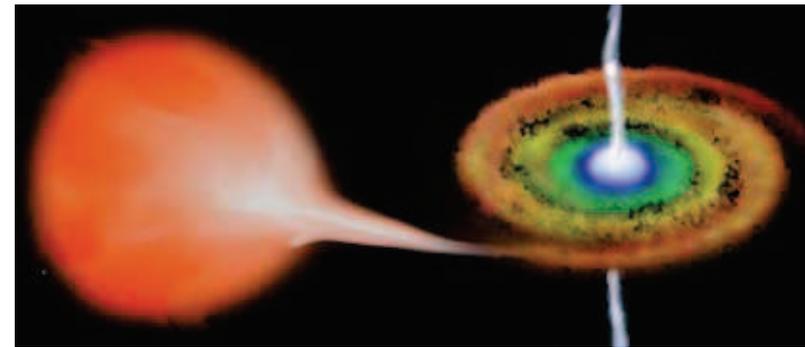
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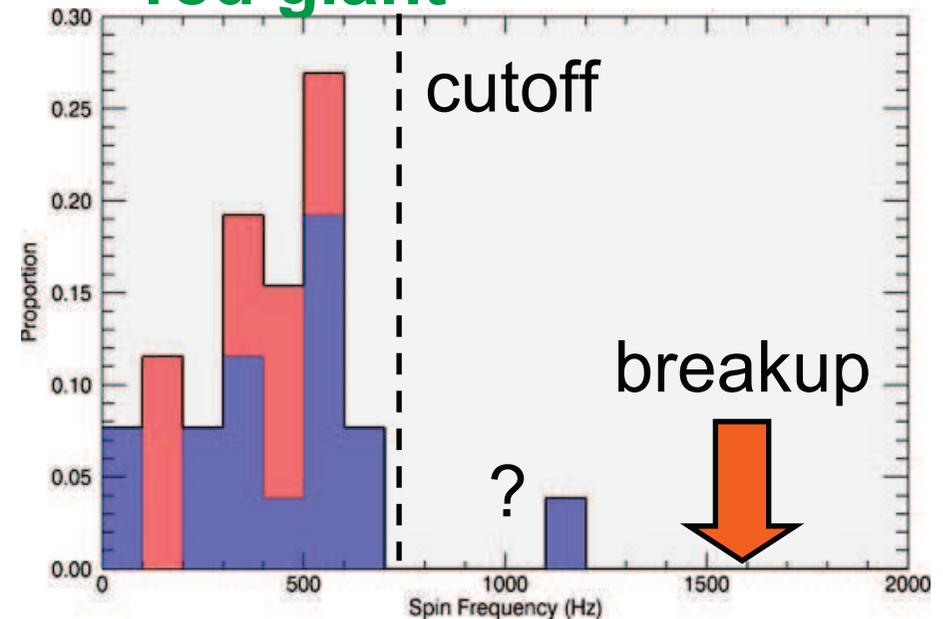
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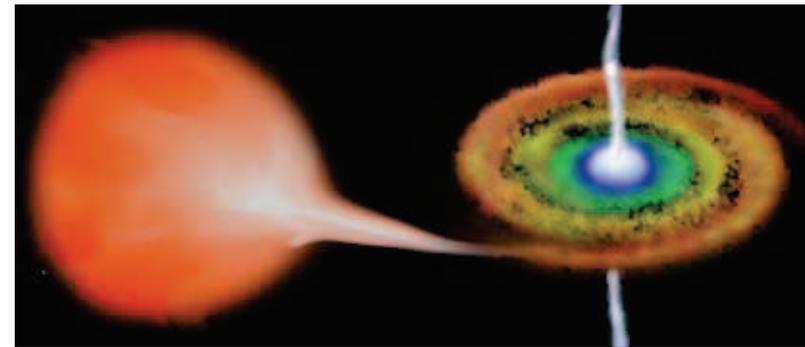
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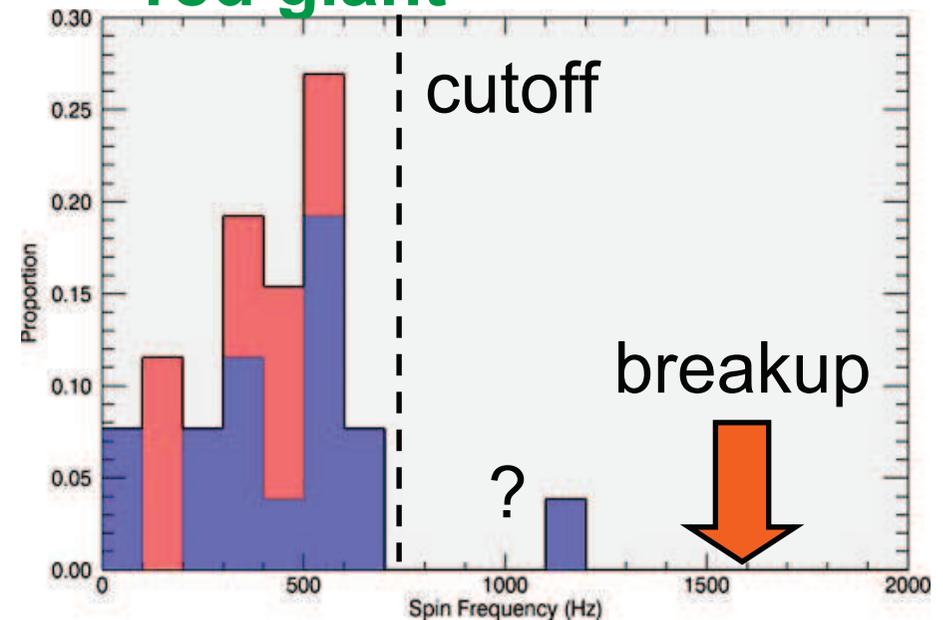
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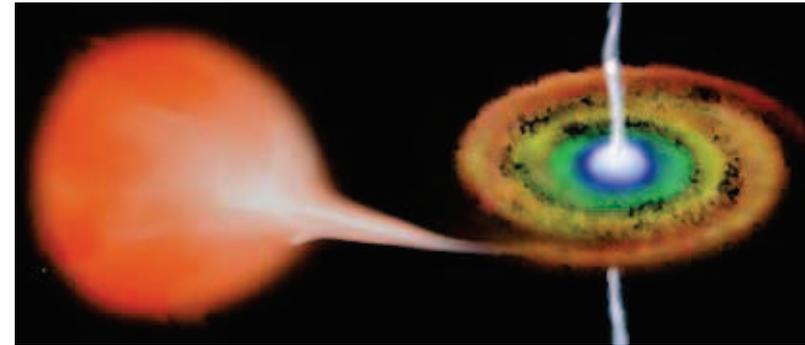
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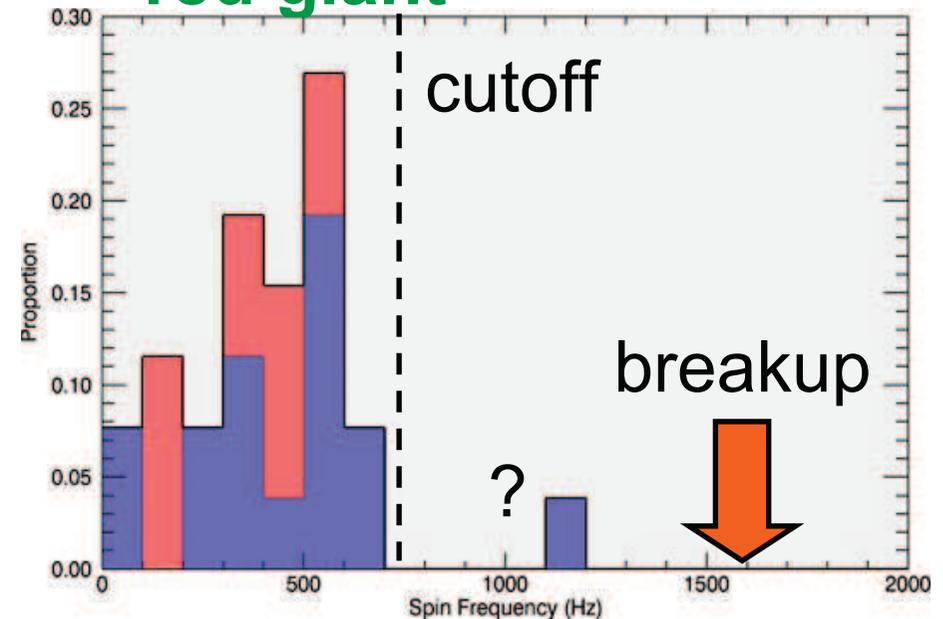
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 - Could be induced by mountains or relativistic instabilities, e.g. r-modes



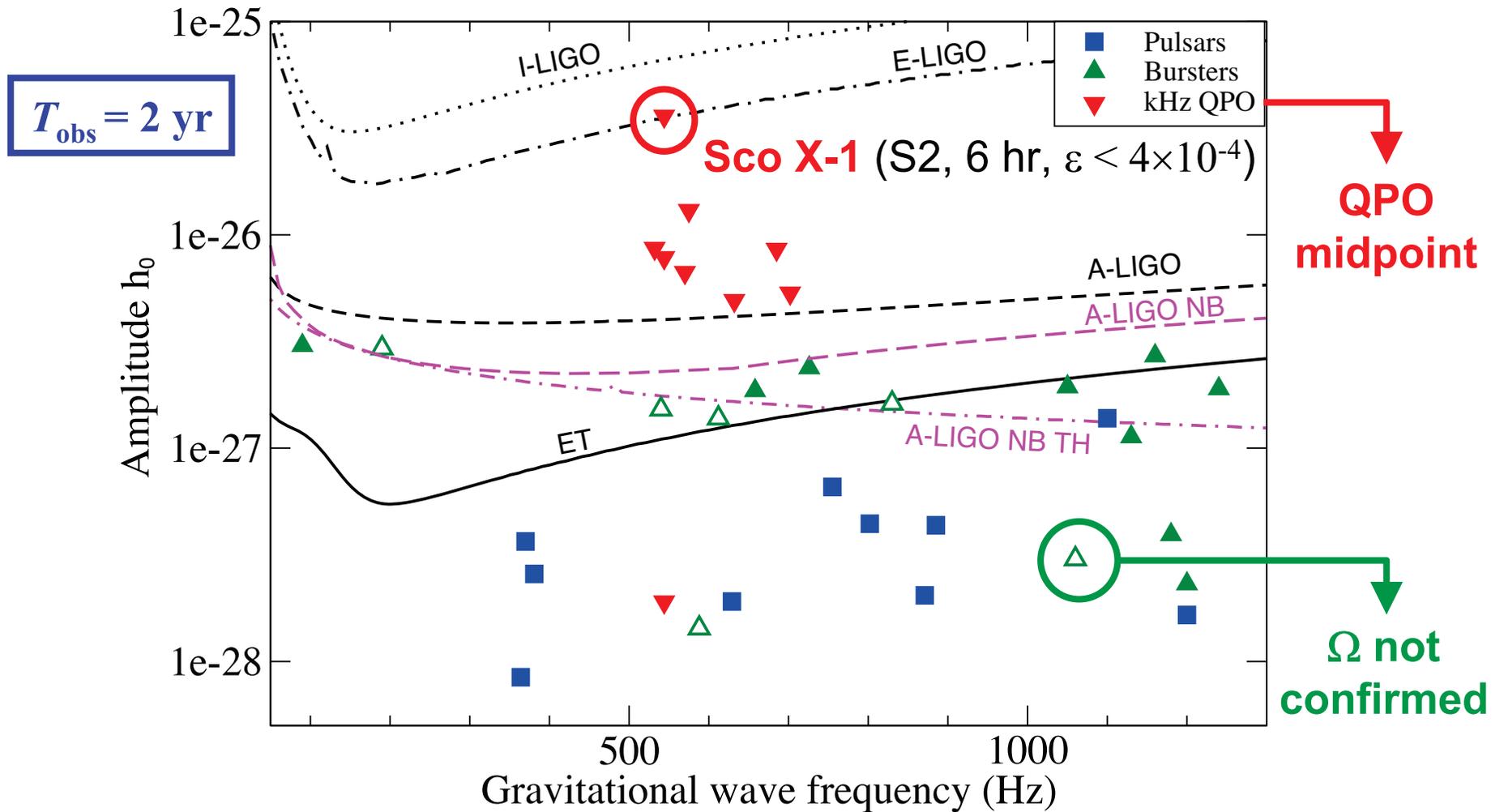
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pulses & burst oscillations

Sensitivity to Accreting NS



Cosmology

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•• Cosmography

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•• H_0 , dark matter and dark energy densities, dark energy EoS w

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- Phase transitions, pre-heating, re-heating, etc.

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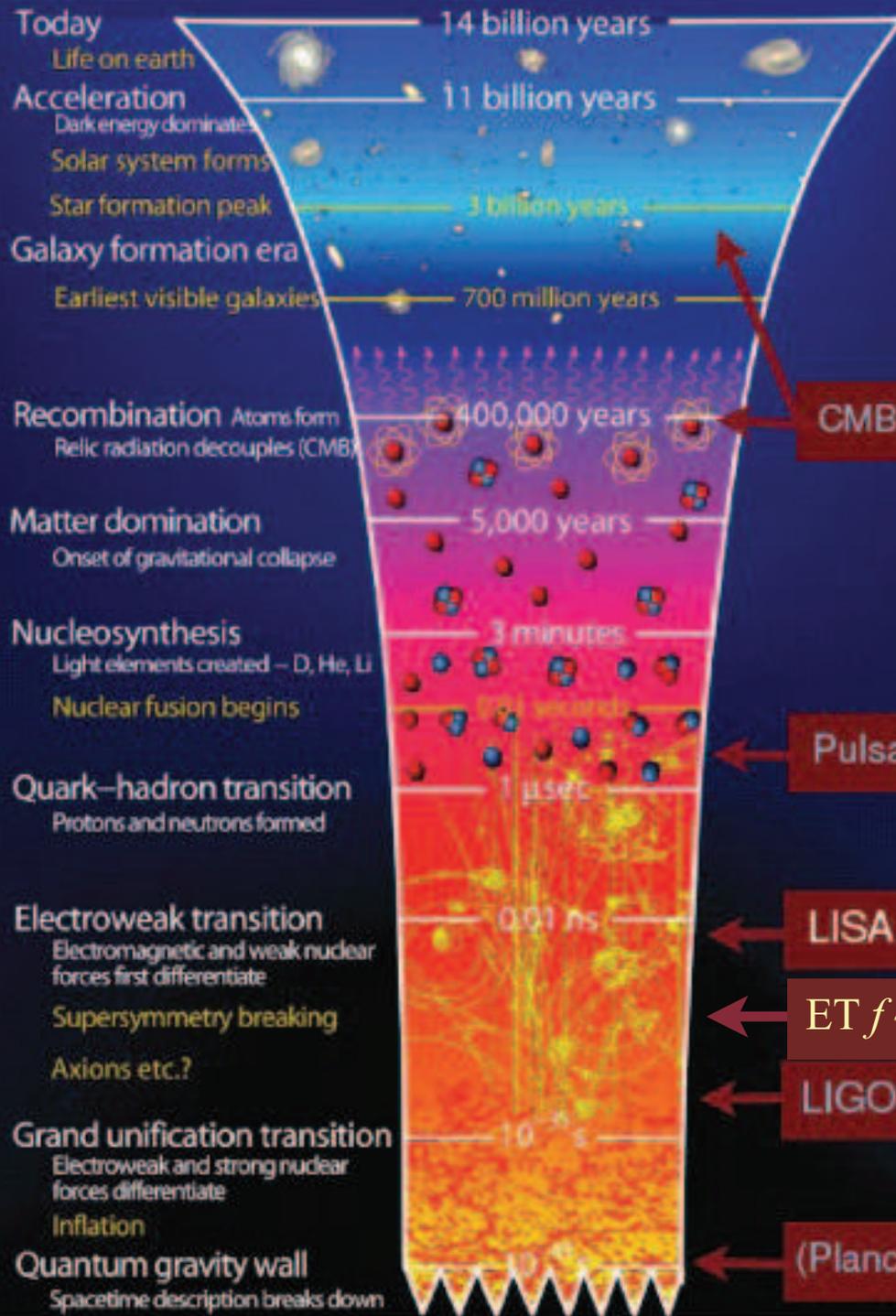
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 - A population of Galactic white-dwarf binaries produces a background above instrumental noise in LISA

A brief history of the Universe



CMB $f < 3 \times 10^{-17} \text{ Hz}$ probes $300,000 \text{ yrs} < t_e < 14 \text{ Gyrs}$

Pulsars $f \sim 10^{-8} \text{ Hz}$ probe $t_e \sim 10^{-4} \text{ s}$ ($T \sim 50 \text{ MeV}$)

LISA $f \sim 10^{-3} \text{ Hz}$ probes $t_e \sim 10^{-14} \text{ s}$ ($T \sim 10 \text{ TeV}$)

ET $f \sim 10 \text{ Hz}$ probes $t_e \sim 10^{-20} \text{ s}$ ($T \sim 10^6 \text{ GeV}$)

LIGO $f \sim 100 \text{ Hz}$ probes $t_e \sim 10^{-24} \text{ s}$ ($T \sim 10^8 \text{ GeV}$)

(Planck scale $f \sim 10^{11} \text{ Hz}$ has $t_e \sim 10^{-43} \text{ s}$ ($T \sim 10^{19} \text{ GeV}$))

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LSC, *Astrophys.J.* 659 (2007) 918

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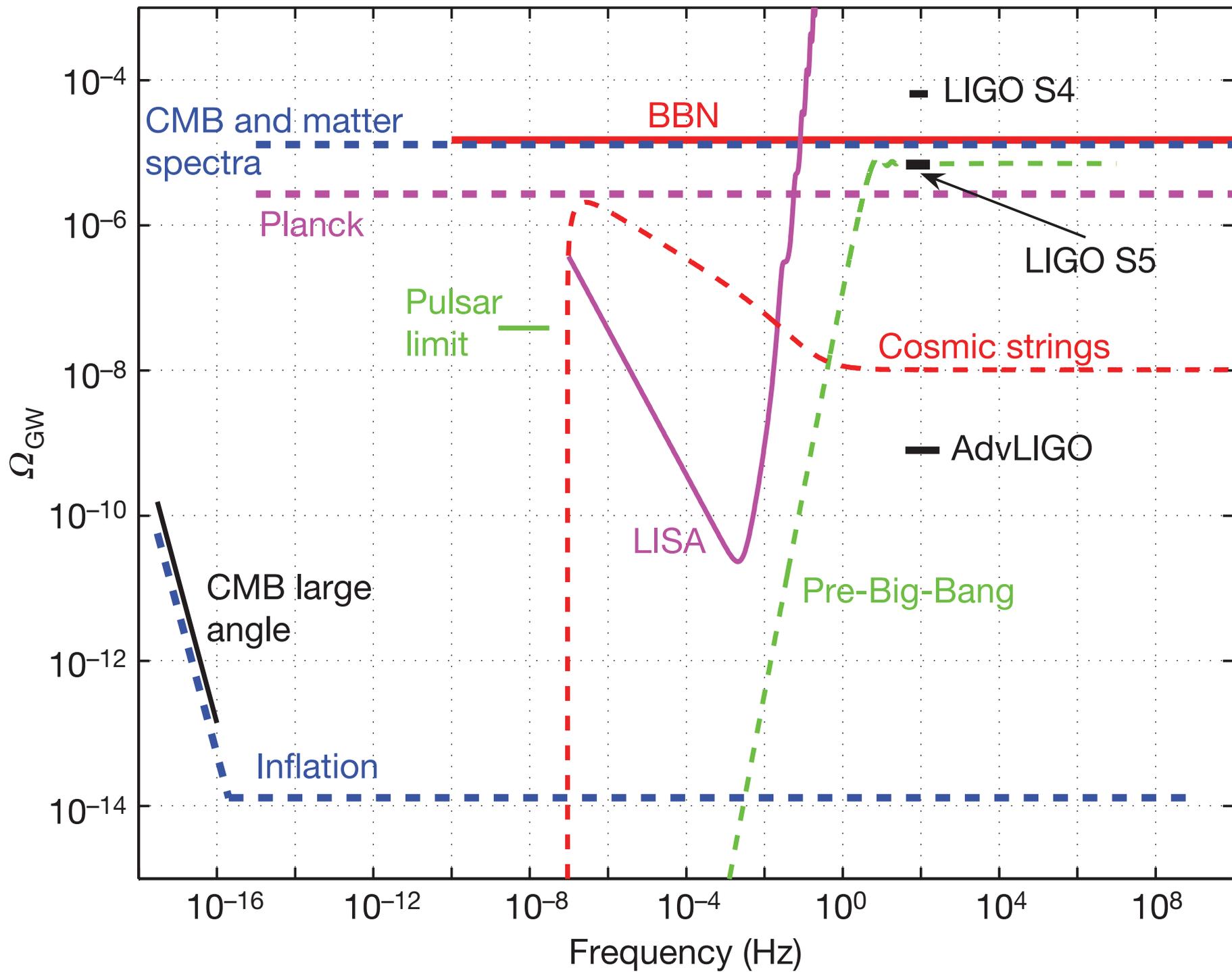
nature

Vol 460 | 20 August 2009 | doi:10.1038/nature08278

LETTERS

An upper limit on the stochastic gravitational-wave background of cosmological origin

The LIGO Scientific Collaboration* & The Virgo Collaboration*



Cosmological parameters

$$D_L(z) = \frac{c(1+z)}{H_0} \int_0^z \frac{dz}{[\Omega_M(1+z)^3 + \Omega_\Lambda(1+z)^{3(1+w)}]^{1/2}}$$

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- Einstein Telescope will detect 1000's of compact binary mergers for which the source can be identified (e.g. GRB) and red-shift measured.
- A fit to such observations can determine the cosmological parameters to better than a few percent.

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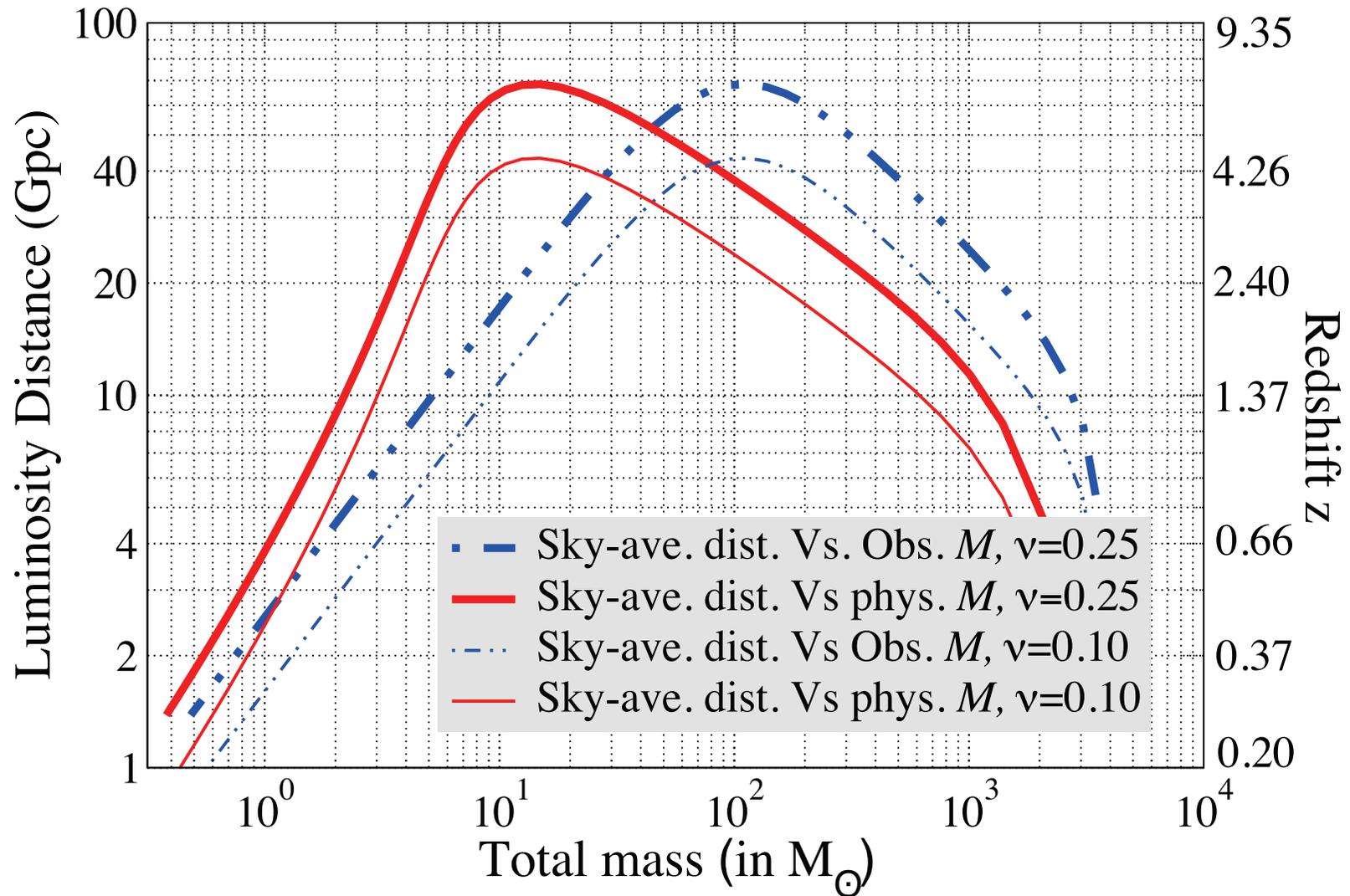
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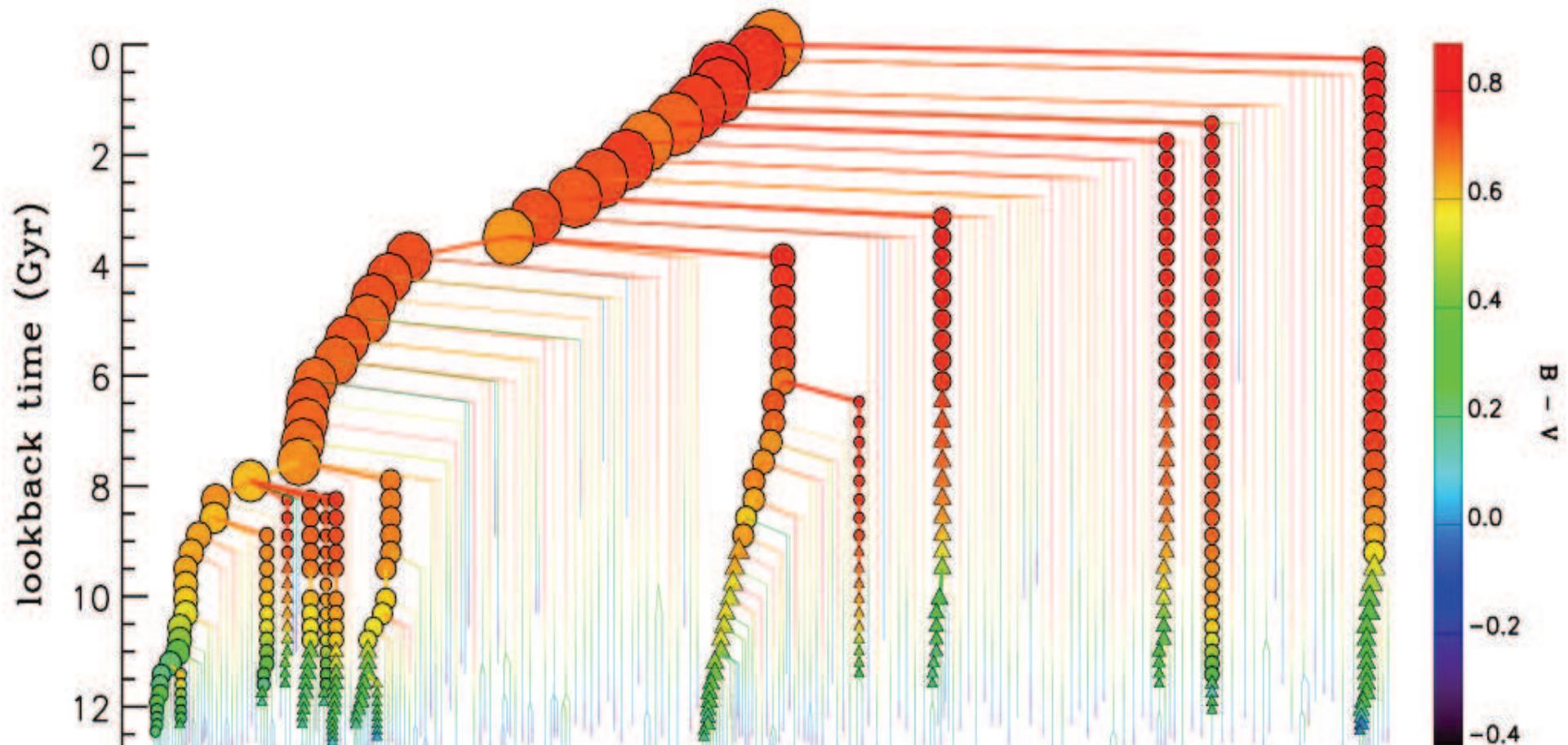
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- Joint gravitational-wave and optical observations can facilitate a new cosmological tool

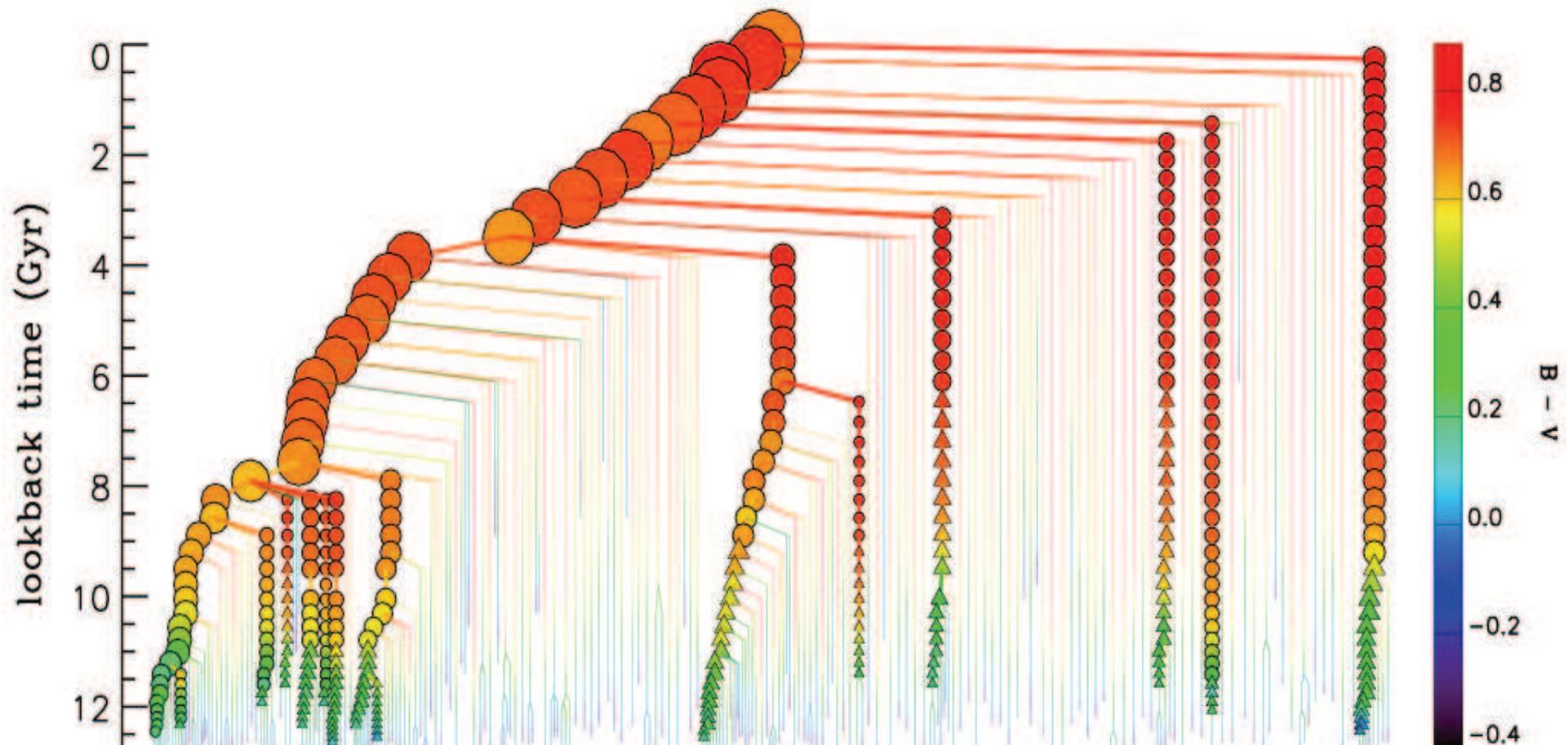
Distance Reach of ET



Hierarchical Growth of Black Holes in Galactic Nuclei

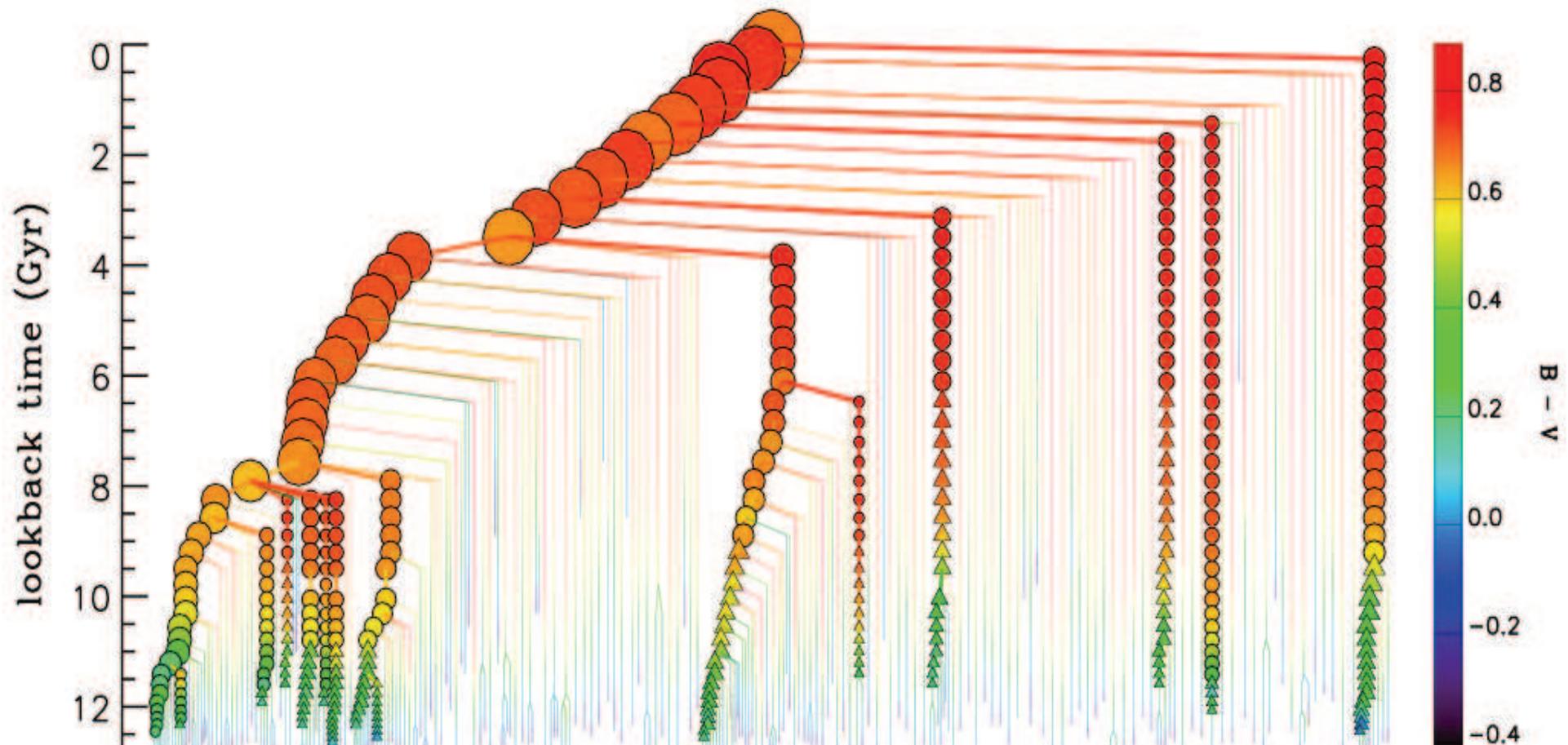


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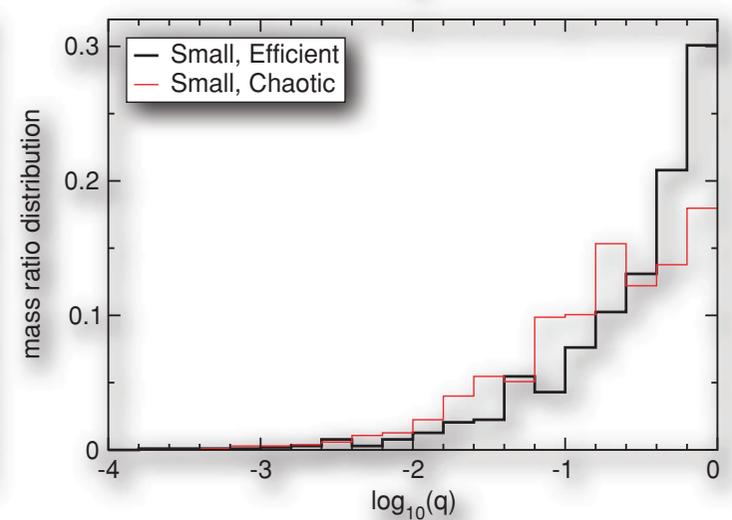
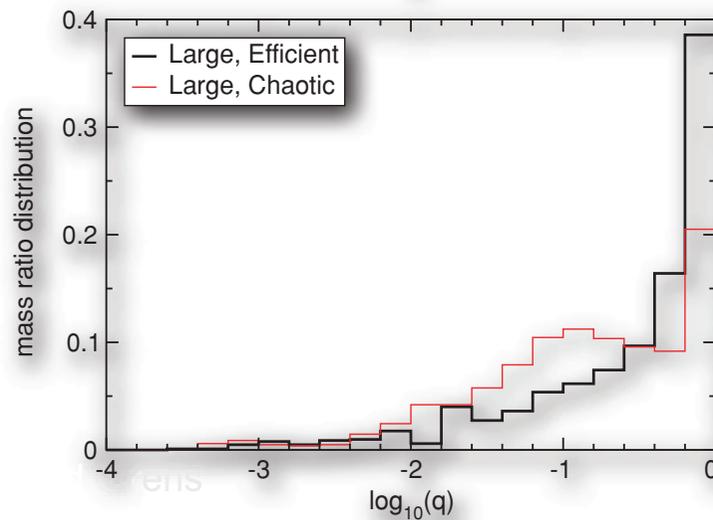
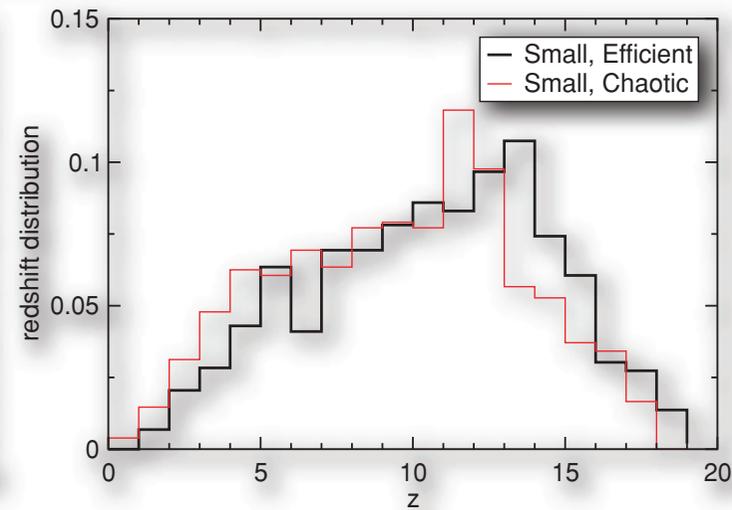
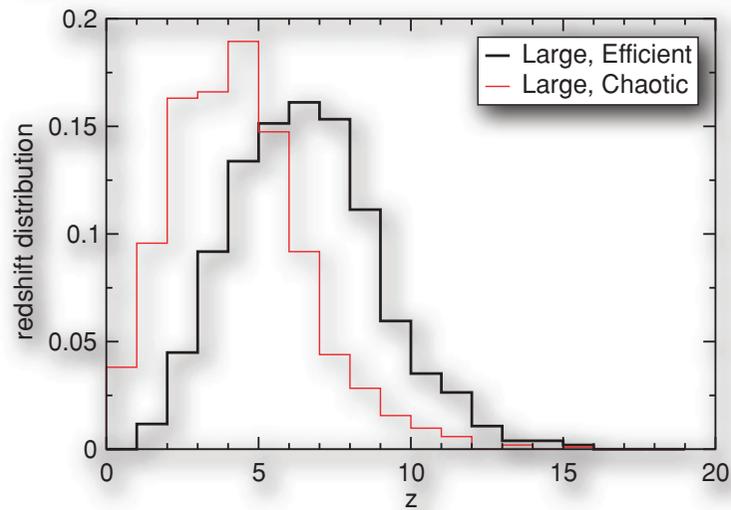


- Initially small black holes may grow by hierarchical merger
- ET could observe seed black holes if they are of order 1000 solar mass

Models of Black Hole Seeds and Their Evolution

Class. Quantum Grav. 26 (2009) 094027

K G Arun *et al*



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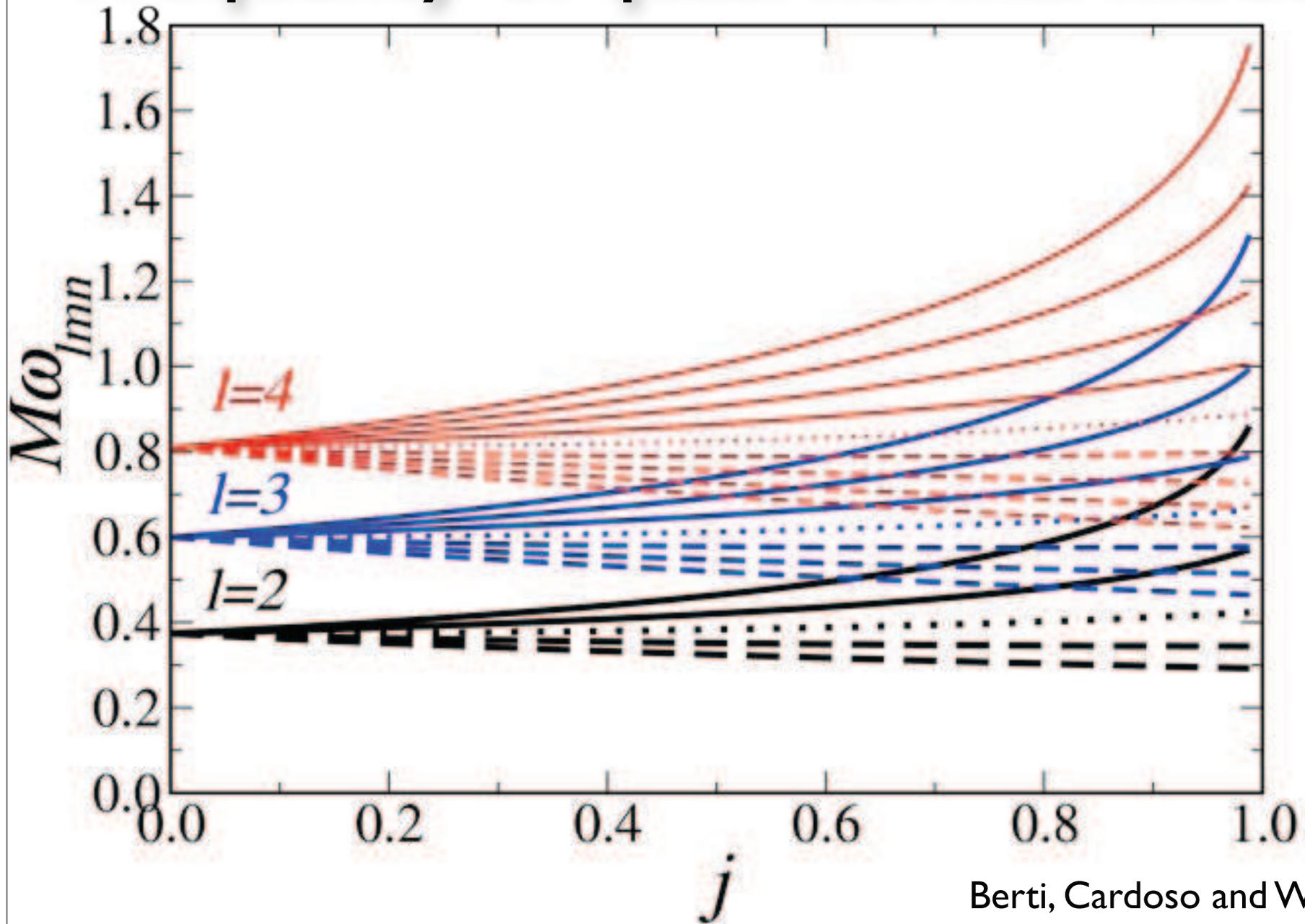
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- If modes depend on other parameters (e.g., the structure of the central object), then test of the consistency between different mode frequencies and damping times would fail

Frequency of quasi normal modes



Tests with QNM

Kamaretsos, Hannam, Husa, Sathyaprakash, 2010

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 - Polarization of ringdown modes can measure the spin axis of merged BH

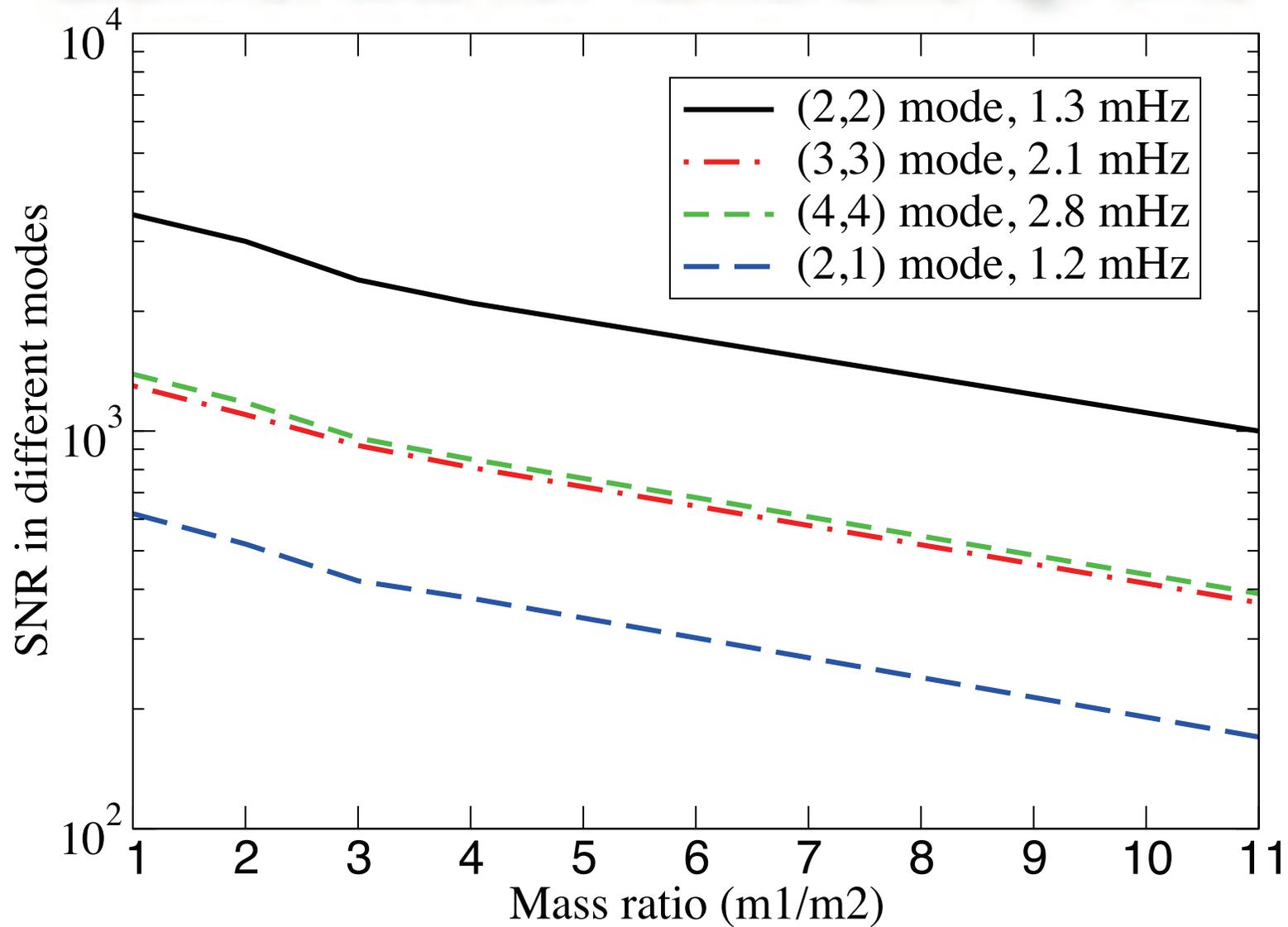
Emitted energy and relative amplitudes of different quasi-normal modes

Kamaretsos, Hannam, Husa, Sathyaprakash, 2010

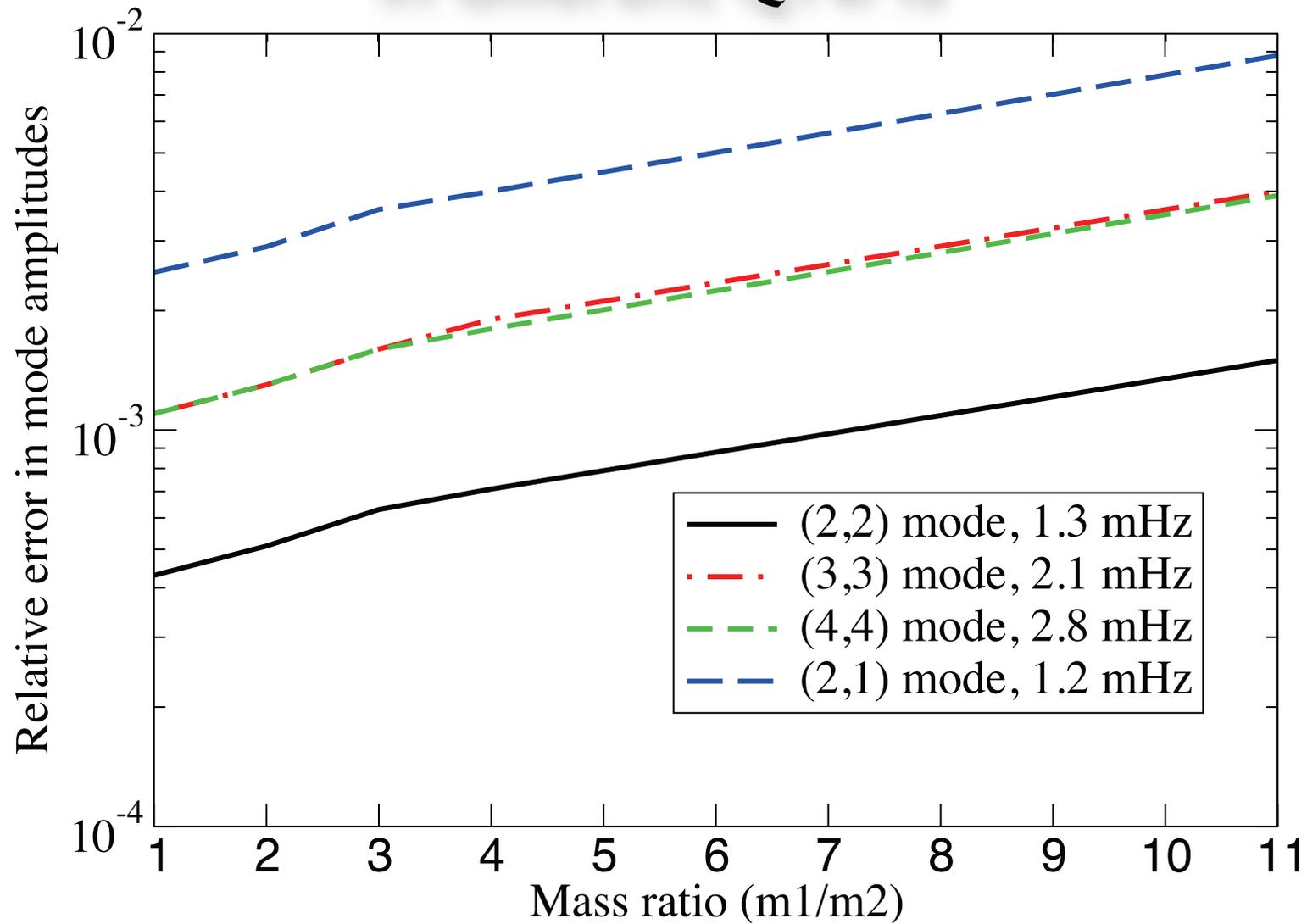
Table 1: For different mass ratios ($q=1, 2, 3, 4, 11$), we show the final spin of the black hole, percent of energy in the radiation, amplitude of (2,1), (3,3), (4,4) modes relative to (2,2) mode.

| q | j | % total energy | A_{21}/A_{22} | A_{33}/A_{22} | A_{44}/A_{22} |
|-----|------|----------------|-----------------|-----------------|-----------------|
| 1 | 0.69 | 4.9 | 0.04 | 0.00 | 0.05 |
| 2 | 0.62 | 3.8 | 0.05 | 0.13 | 0.06 |
| 3 | 0.54 | 2.8 | 0.07 | 0.21 | 0.08 |
| 4 | 0.47 | 2.2 | 0.08 | 0.25 | 0.09 |
| 11 | 0.25 | 0.7 | 0.14 | 0.31 | 0.14 |

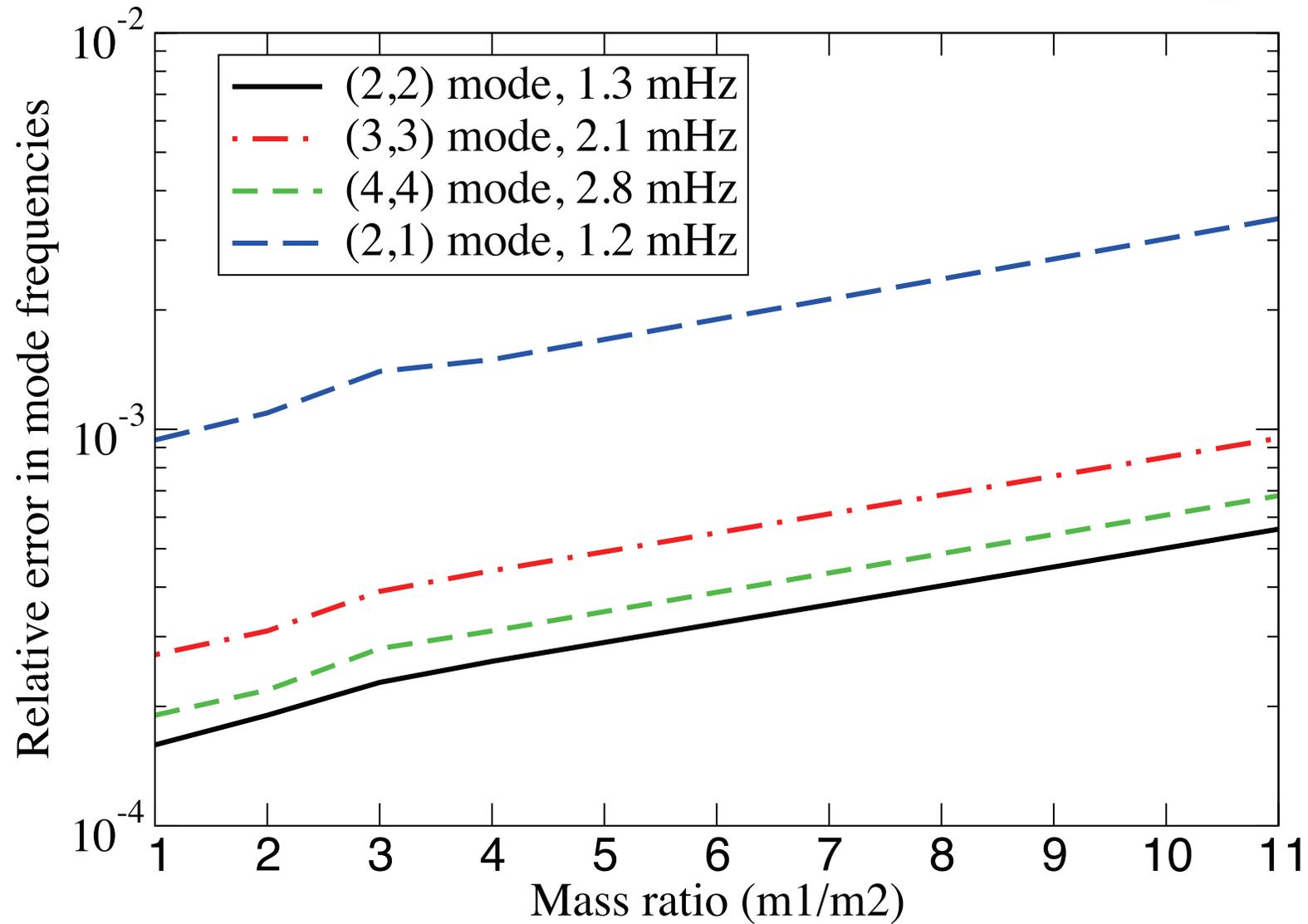
LISA SNRs for different QNMs



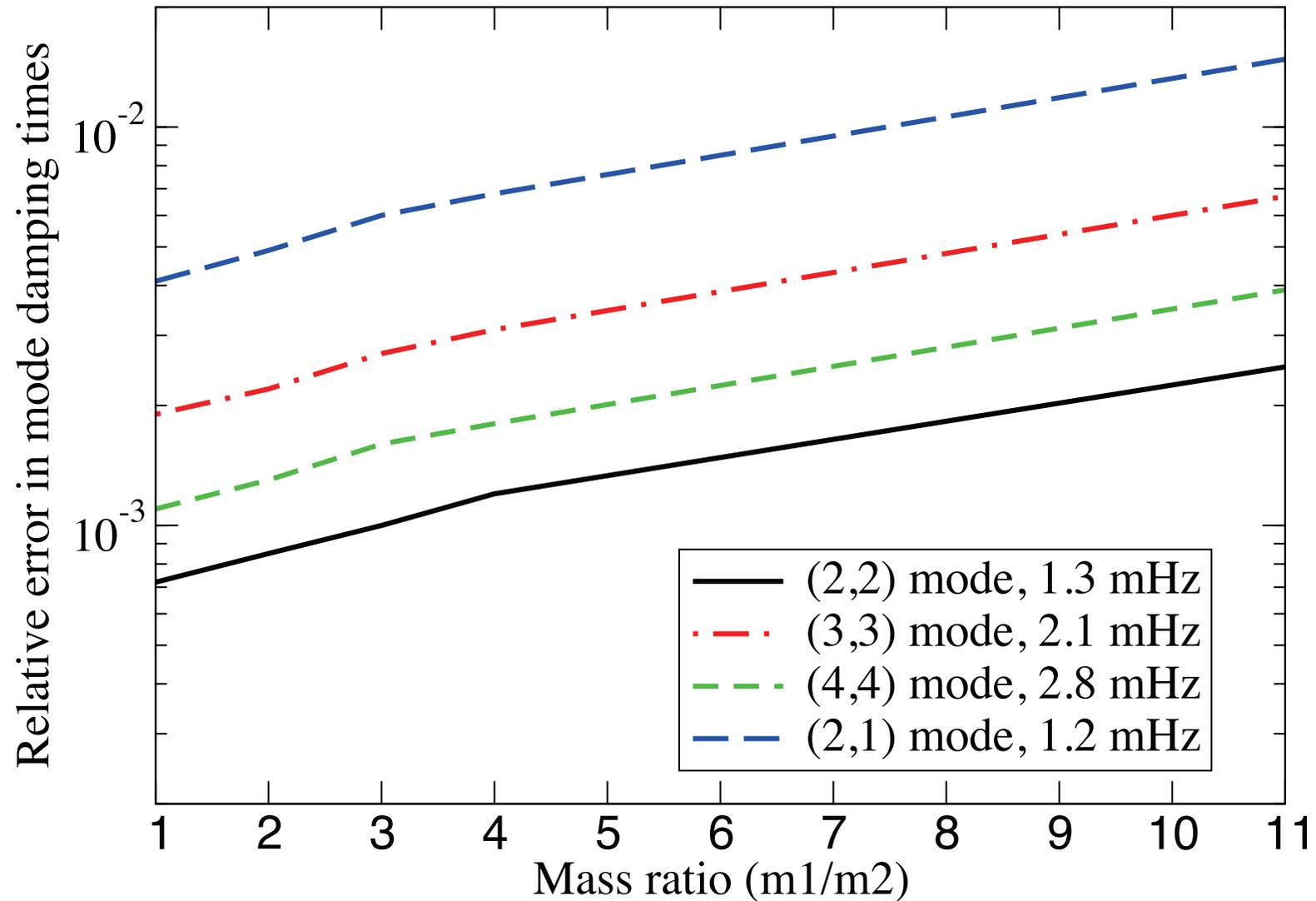
LISA measurement accuracies of amplitudes in different QNMs



LISA measurement accuracies of mode frequencies

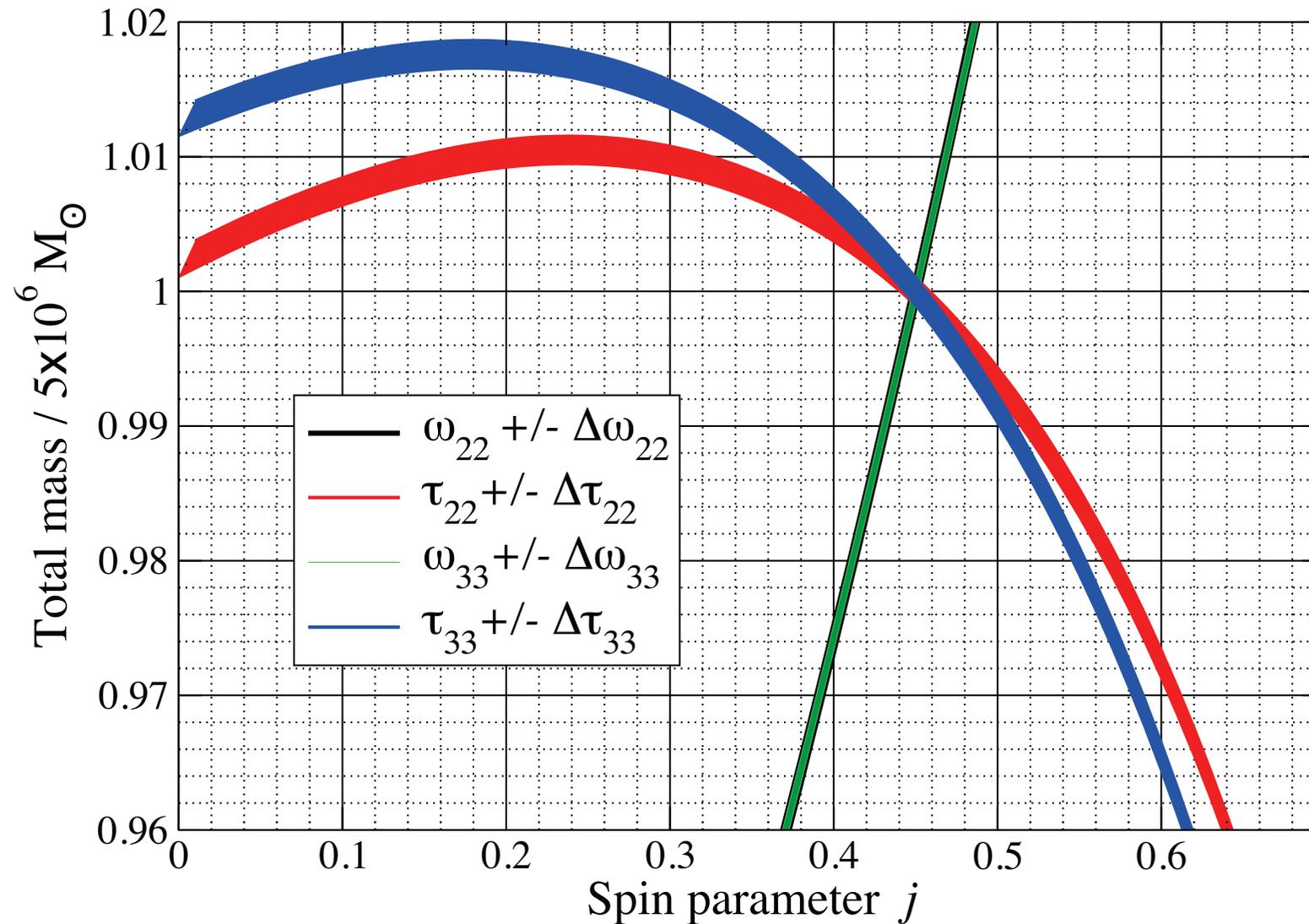


LISA measurement accuracies damping times



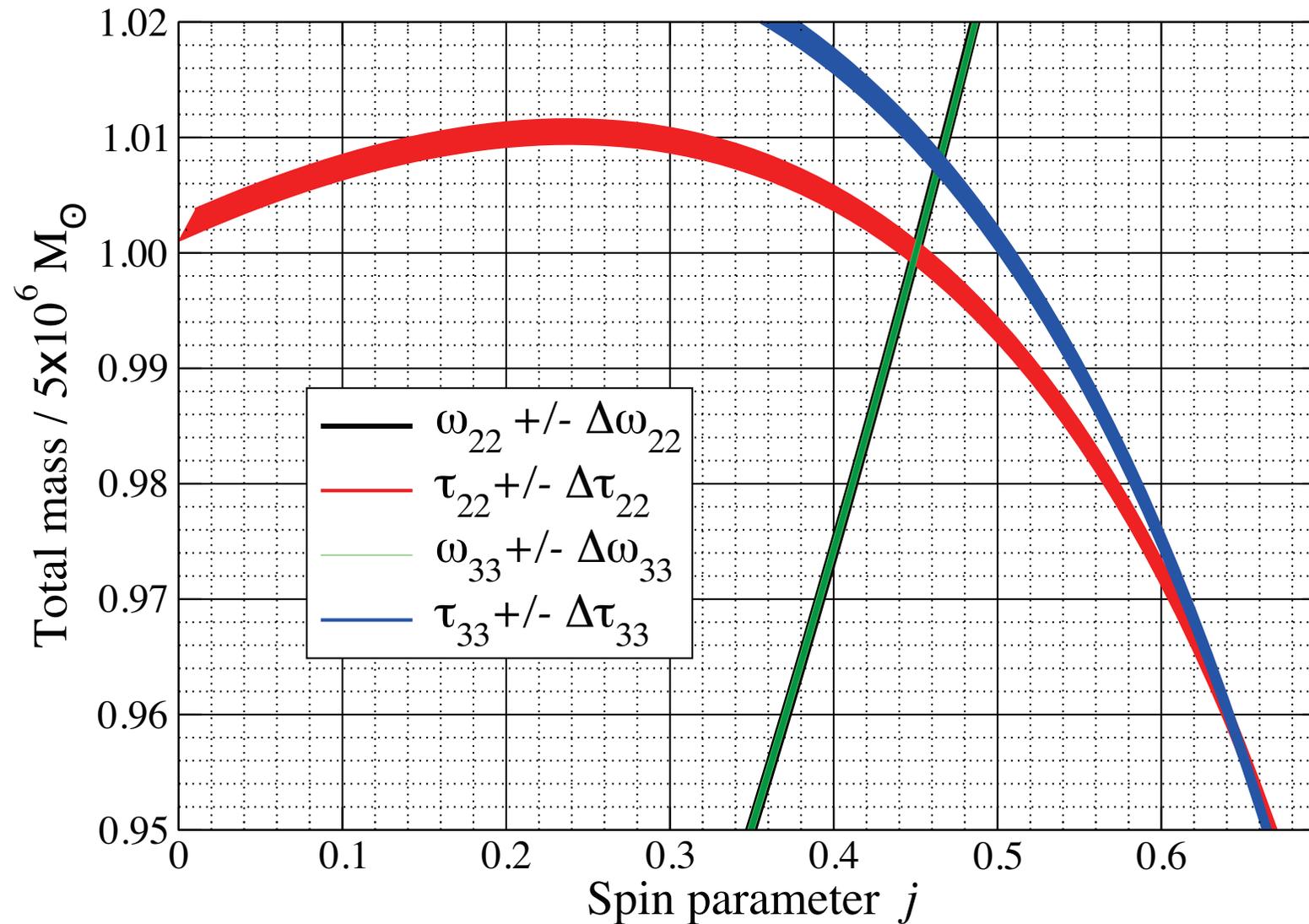
How can QNMs help test GR

Consistency in M-j plane from
QNM frequencies and damping times



How can QNMs help test GR

Inconsistency in M-j plane resulting from a 1% departure in τ_{22} from the GR value



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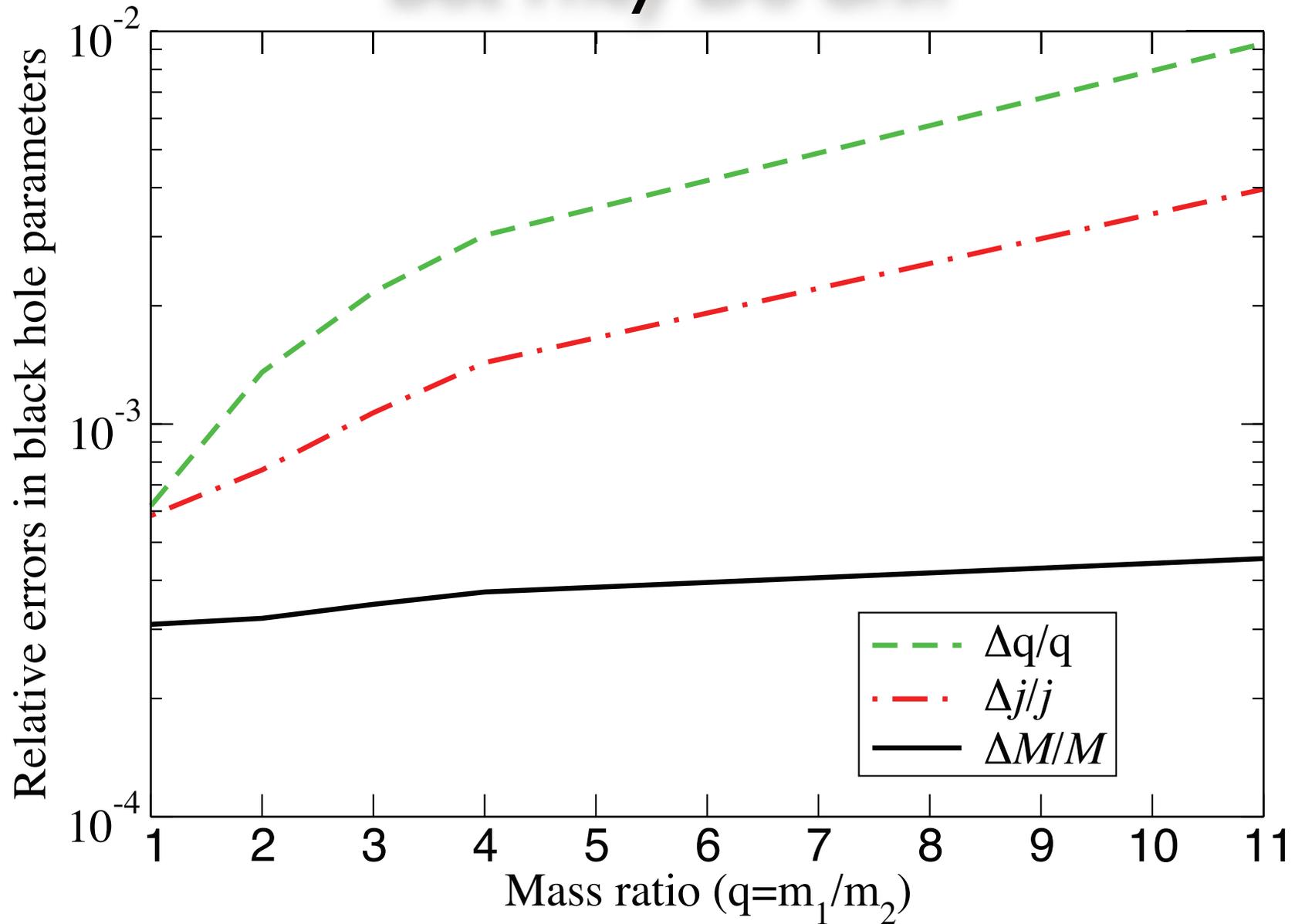
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- From the ringdown signals it should in principle be possible to infer the nature of the perturber
- In the case of binary mergers it should be possible to measure the masses and spins of the component stars that resulted in the final black hole

Black Holes Ain't Got No Hair But They Do *Grin*



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